

EXPERIMENTAL AND THEORETICAL INVESTIGATION  
OF A SHALLOW FLEXIBLE ARCH/

By

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# NOTATIONS

$D_s, D_s^2$	First and second derivatives with respect to $s$
$D_x, D_x^2$	First and second derivatives with respect to $x$
$D_z, D_z^2$	First and second derivatives with respect to $z$
$E$	Young's modulus of the arch material
$f$	Rise of the arch
$g$	A parameter, $g^2 = \frac{H_a L^2}{EI}$
$H$	True horizontal reaction
$H_a$	Assumed horizontal reaction
$I$	Moment of inertia of the cross section
$L$	Span length
$M$	Bending moment
$M_o$	Bending moment under the load in a simply supported beam having the same span as that of the arch
$M_a, M_b$	Fixed end moment for ends A and B respectively
$n$	Non-dimensional parameter, $n = \frac{f}{L}$
$N$	Influence line for thrust force
$q(x)$	A loading function characterizing the intensity of a distributed load
$R$	Initial radius of curvature of the arch axis
$\rho$	Radius of curvature of the arch axis after deformation
$s$	Arc length along the arch axis
$\theta$	Angle between the horizontal and the tangent to the arch axis
$u_q, u_h$	Non-dimensional functions
$v$	Total vertical displacement (+ve downward)
$v_h$	$v$ due to unit horizontal reaction $H$ , with respect to the equilibrium position attained after the application of $H_a$
$v_q$	$v$ due to external load, with respect to the equilibrium position attained after the application of $H_a$

w	Radial displacement
X,Y	Rectangular coordinates
y(x)	The function describing the shape of the arch axis
z	Non-dimensional parameter, $z = \frac{x}{L}$

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## INTRODUCTION

Elastic theory <sup>[1]</sup> has been in use for many years in the design of structures. In general, this theory neglects any change in geometry of the structure due to strain. When the elastic displacements and axial forces are small, the error involved is usually small. But, when the elastic displacements are appreciable, or when the axial force is not a small fraction of its buckling value, the error introduced may be an important factor in the design. This awareness calls for a more refined method that could reduce the error in the analysis. Deflection theory <sup>[2]</sup>, the subject matter, is one such method. Since the coefficients of equilibrium equations in this theory depend on the displacements, the governing equations are not linear and hence principle of superposition is not applicable without special treatment.

Deflection theory, applied to a number of structures in the past, has shown that the behaviour of a structure can be predicted with much higher accuracy as compared to the elastic theory <sup>[3]</sup>. The theory was used in the design of the Rainbow arch bridge across the Niagara. Analysis of the arch rib showed that the quarter point deflection of 12 inches as computed by the elastic theory, increased to 21 inches by deflection theory. At the same time, it was observed that the unit stresses hiked up by 28%.

In long spanned arches, the thrust due to dead load becomes an important consideration when determining the moments with the use of deflection theory. The present work is an attempt to test the applicability of a linearized deflection theory for a fixed-fixed

parabolic flexible arch. The stresses induced in a long span arch due to the deflection of the arch axis are very much significant. This fact solidifies our belief that the change in geometry cannot be neglected. Wang<sup>[4]</sup>, in his Masters report, has put forward the deflection theory as applied to a parabolic arch of variable moment of inertia. It should be mentioned that Wang's work has been taken as the basis of this thesis.

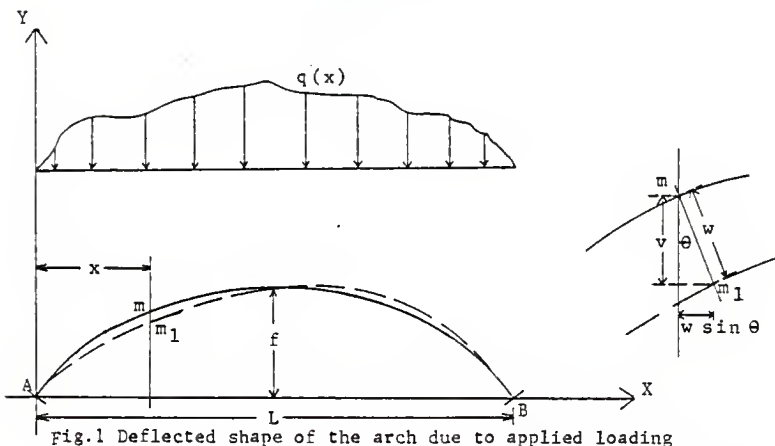
If one uses iterative method of analysis, the internal forces of the arch determined by the elastic theory is used as the first approximation and are applied to calculate an approximate resulting deflected shape. Additional bending moments due to the deflection is calculated and used for the determination of the second approximate deflected position of the arch axis. If the loaded arch is stable, the deflection is finite and repetition of this procedure will yield the equilibrium position of the arch at which the forces and deflections are consistent<sup>[3]</sup>.

The derived governing differential equation is nonlinear, because one of the coefficients is the horizontal reaction which is a functional of deflection. To remove the difficulty, a linearization technique is employed. This linearization enabled the applicability of the principle of superposition under a preassigned horizontal thrust  $H$ . The resultant internal forces were expressed as a combination of effects due to transverse load on a beam and that due to the horizontal reaction and curvature of the arch. Shooting method was used to determine the influence lines of sectional forces for a set of carefully selected flexibility parameters. Using these influence lines, relationship between the variation of a stress at any section of

the arch to the variation of assumed horizontal reaction can be obtained. At the same time, the relationship between the corresponding computed horizontal reaction and the assumed horizontal reaction forces are obtained. By the use of the second relationship, the correct horizontal reaction force component can be calculated and used to find the correct value of the force of interest from the first relationship.



## Derivation of the Governing Differential Equation



In the derivation of the equation, the following assumptions are being made.

1. Stresses and strains are within proportional limits.
2. The influence of the horizontal component of the deflection is small and can be neglected.
3. The change in slope of the axis of the arch due to the applied load, at any point, is so small that the differential length can be assumed as  $ds = dx \sec \theta$ .
4. The load is assumed to act directly on the arch axis.
5. The radius of curvature is large compared to the thickness of the arch rib so that the straight beam formula is applicable.
6. The arch axis is assumed to be inextensible, thus neglecting the axial effects due to deformation.
7. The effects due to shearing strain is small.

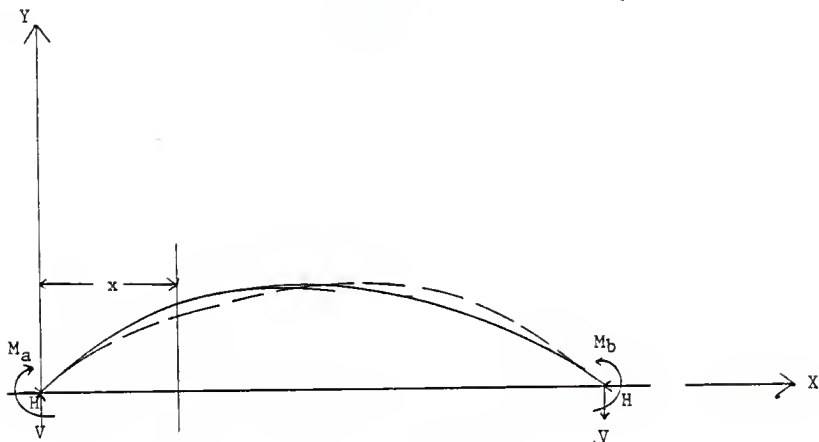


Fig.2 Reaction forces due to applied load

Based on the assumptions made, the bending moment at any point  $m$ , distant  $x$  from the left end of the fixed-fixed arch can be written as,

$$M_x = M_0 - H(y - v) + (M_b - M_a) \frac{x}{L} + M_a \quad (1)$$

Equation (1) can be rewritten as,

$$M_x = M_0 - H(y - v) + M_a \left(1 - \frac{x}{L}\right) + M_b \frac{x}{L} \quad (2)$$

We can express the relation between change in curvature and magnitude of bending moment  $M$  by the equation,

$$EI \left( \frac{1}{\rho} - \frac{1}{R} \right) = -M \quad (3)$$

$M$  is taken positive when it produces a decrease in the initial curvature of the arch axis. Note that, in the above case the moment is increasing the curvature.

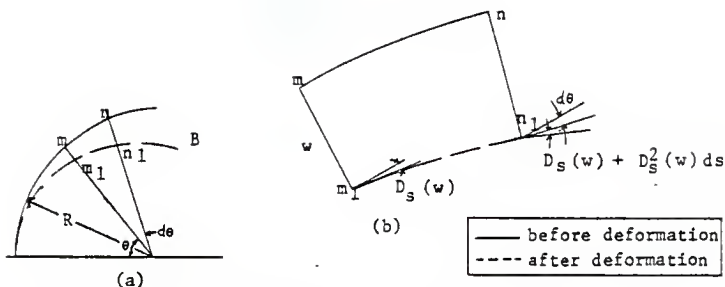


Fig.3 Change in curvature of arch axis

The change in curvature of the arch axis during bending will be found from a consideration of the deformation of a small element  $mn$  included between two radii with an angle  $d\theta$  between them.

The initial length and curvature of the small element  $mn$  are,

$$ds = R d\theta \quad \text{and} \quad \frac{1}{R} = D_s(\theta) \quad (4)$$

The curvature of the arch axis after bending is,

$$\frac{1}{\rho} = \frac{(d\theta + \Delta d\theta)}{(ds + \Delta ds)} \quad (5)$$

where,  $d\theta + \Delta d\theta$  = Angle between normal cross sections at  $m_1$  and  $n_1$ .

$ds + \Delta ds$  = Length of element  $m_1 n_1$

The angle between the tangent to the centerline at  $m_1$  and the perpendicular to the radius  $mo$  is  $D_s(w)$ . The corresponding angle at cross section  $n_1$  is  $D_s(w) + D_s^2(w) ds$

$$\begin{aligned} \text{Hence,} \quad d\theta &= D_s(w) + D_s^2(w) ds - D_s(w) \\ &= D_s^2(w) ds \end{aligned} \quad (6)$$

As the angle  $D_s(w)$  is very small, we could neglect the same

while calculating the length of  $m_1 n_1$ .

$$\text{Length of } mn = R d\theta$$

$$\text{Length of } m_1 n_1 = (R - w) d\theta$$

$$\text{Hence } ds = (R - w) d\theta - R d\theta$$

$$ds = -w d\theta$$

But from ( 4 ),

$$d\theta = \frac{1}{R} ds$$

Therefore,

$$ds = -w \frac{1}{R} ds$$

Hence ( 5 ) can be rewritten as,

$$\begin{aligned} \frac{1}{\rho} &= \frac{[ D_s(\theta) + D_s^2(w) ds ]}{[ ds - \frac{w}{R} ds ]} \\ &= \frac{ds [ D_s(\theta) + D_s^2(w) ]}{ds [ 1 - \frac{w}{R} ]} \\ &= \frac{(1/R) + D_s^2(w)}{1 - \frac{w}{R}} \quad ( 7 ) \end{aligned}$$

For  $r < 1$ ,

$$\frac{1}{1-r} = 1 + r + r^2 + \dots$$

Thus for  $w \ll R$ , one has,

$$\frac{1}{1 - (w/R)} = 1 + (w/R) + (w/R)^2 + \dots$$

Neglecting small terms of higher order,

$$\frac{1}{\rho} = \left(1 + \left(\frac{w}{R}\right)\right) \frac{1}{R} + D_s^2(w)$$

Substituting for  $\frac{1}{\rho}$  in (3),

$$EI \left[ \frac{1}{R} \left(1 + \left(\frac{w}{R}\right)\right) + D_s^2(w) - \frac{1}{R} \right] = -M$$

$$EI \left[ \left(\frac{w}{R^2}\right) + \{D_s^2(w)\} \right] = -M$$

Equation (2) will therefore become,

$$-EI \left[ \frac{w}{R^2} + D_s^2(w) \right] = M_o - H(y - v) + M_a \left(1 - \frac{x}{L}\right) + M_b \frac{x}{L}$$

As the radius of curvature is large compared to the radial displacement  $w$ ,

$$-EI D_s^2(w) = M_o - H(y - v) + M_a \left(1 - \frac{x}{L}\right) + M_b \frac{x}{L} \quad (8)$$

The vertical displacement of the arch axis is,

$$v = w \cos \theta$$

$$\text{or, } w = v \sec \theta$$

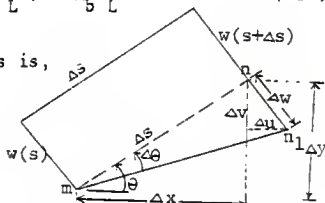


Fig (3c) Elemental displacement

With reference to the sketch shown alongside,

$$D_s(w) \approx D_x(v)$$

$$\begin{aligned}
\text{and, } D_s^2 (w) &= D_s \{D_x(v)\} \\
&= \cos\theta D_x \{D_x(v)\} \\
&= \cos\theta D_x^2(v)
\end{aligned}$$

As moment of inertia of the arch is constant, ( 8 ) can therefore be written as,

$$- EI \cos\theta D_x^2 (v) = M_o - H y + H v + M_a (1 - \frac{x}{L}) + M_b (\frac{x}{L})$$

Defining  $G(x) = \cos\theta$ ,

$$G(x) D_x^2(v) = - \frac{H}{EI} v + \frac{H}{EI} y + f(x)$$

$$\text{where, } f(x) = - \frac{1}{EI} [ M_o(x) + M_a (1 - \frac{x}{L}) + M_b (\frac{x}{L}) ]$$

or,

$$G(x) D_x^2 (v) = - \frac{1}{L^2} \left( \frac{HL^2}{EI} \right) v + \frac{H}{EI} y + f(x) \quad ( 9 )$$

The first term on the right hand side of equation ( 9 ) is the moment due to deflection and horizontal thrust ; the second term is the moment due to the action of the arch profile ; and last term is the end moment.

( 9 ) can be rewritten as,

$$G(x) D_x^2(v) + \frac{1}{L^2} \left( \frac{HL^2}{EI} \right) v = \frac{H}{EI} y + f(x)$$

Differentiating twice and rearranging,

$$G(x) D_x^4 (v) + 2 G'(x) D_x^3 (v) + [G''(x) + \frac{1}{L^2} \frac{(HL)^2}{EI}] D_x^2 (v) = \frac{H}{EI} y'' + \frac{q(x)}{EI} \quad (10)$$

For a fixed ended arch, the vertical deflection and slope at the two ends are zero. Hence,

$$\begin{aligned} v(0) &= v(L) = 0 \\ v'(0) &= v'(L) = 0 \end{aligned} \quad (10a)$$

To solve the fourth order differential equation (10), one more constraint condition is required, as H is also an unknown. The condition that the sum of horizontal displacements, through the span length L, is zero will give us this additional condition.

$$\int_0^L v' y' dx = 0 \quad (10b)$$

This consists of horizontal displacements due to both external load and horizontal force

$$\text{i.e. } \int_0^L v'_q y' dx + \int_0^L H v'_h y' dx = 0$$

## Linearization of the differential equation

The fourth order differential equation ( 10 ) has unknown coefficients. Also as  $H$  is a functional of  $v$ , this poses to be a nonlinear problem. Solving this nonlinear problem directly is going to be a tedious job. In order to simplify this, a linearization technique is adopted, thus avoiding the multiplication of  $H$  with the functional of  $v$ , by assuming a parameter,

$$g^2 = \frac{H a L^2}{EI} \quad (10c)$$

Substitution of this into eqn.( 10 ) yields a fourth order linear differential equation, with one unknown value  $g$ .

Since, for any proper value of  $g$  assigned, the equation is transformed into a linear form, the superposition principle is applicable. Therefore, the vertical deflection  $v$  can be split up as,

$$v = v_q + H v_h \quad (10d)$$

where,  $v_q$  = total vert. disp. due to ext. load  
 $v_h$  = total vert. disp. due to unit hor. reaction  $H$

Equation ( 10 ) therefore becomes,

$$\begin{aligned} G(x) D_x^4 (v_q + v_h H) + 2 G'(x) D_x^3 (v_q + v_h H) \\ + [G''(x) + \frac{g^2}{L^2}] D_x^2 (v_q + v_h H) \\ = \frac{H}{EI} y'' + \frac{q(x)}{EI} \end{aligned} \quad (10e)$$

This allows to find the solution in two simpler cases :

$$G(x) D_x^4 (v_q) + 2 G'(x) D_x^3 (v_q) + [G''(x) + \frac{g^2}{L^2}] D_x^2 (v_q) = \frac{q(x)}{EI}$$

and ..... ( 11 )

$$G(x) D_x^4 (v_h) + 2 G'(x) D_x^3 (v_h) + [G''(x) + \frac{g^2}{L^2}] D_x^2 (v_h) = \frac{y''}{EI}$$

..... ( 12 )

The boundary conditions are,

$$\begin{aligned} v_q(0) = v_q'(0) = v_q(L) = v_q'(L) = 0 \\ \text{and} \quad v_h(0) = v_h'(0) = v_h(L) = v_h'(L) = 0 \end{aligned}$$



# Differential equation for a parabolic arch

In case of a parabolic arch, profile is characterized by,

$$y = \frac{4f}{L} \left( x - \frac{x^2}{L} \right) \quad (12a)$$

Its first and second derivatives with respect to x are,

$$y' = \frac{4f}{L} \left( 1 - \frac{2x}{L} \right) = \tan \theta \quad (12b)$$

and  $y'' = -\frac{8f}{L^2}$ , respectively. (12c)

As defined earlier,

$$G(x) = \cos \theta = \frac{1}{(1 + y'^2)^{1/2}} \quad (12d)$$

Differentiating this successively, we can get  $G'(x)$  and  $G''(x)$

For simplicity, some of the nondimensional terms are defined as follows.

$$z = \frac{x}{L}$$

$$n = \frac{f}{L}$$

$$u_q = -\frac{v_q}{L} \quad (13)$$

$$Q(z) = \frac{q(x) L^3}{EI}$$

$$u_h = -\frac{v_h}{L}$$

The differential equations (11) and (12) can therefore be written as,

$$G(z) D_z^4 (u_q) + 2 G'(z) D_z^3 (u_q) + (G''(z) + g^2) D_z^2 (u_q) = Q(z) \quad \dots\dots\dots (14)$$

and its boundary conditions are,

$$u_q(0) = u_q(L) = u'_q(0) = u'_q(L) = 0$$

$$G(z) D_z^4(u_h) + 2 G'(z) D_z^3(u_h) + (G''(z) + g^2) D_z^2(u_h) = -8nr \quad \dots\dots\dots (15)$$

and the corresponding boundary conditions are,

$$u_h(0) = u_h(L) = u_h'(0) = u_h'(L) = 0 \quad (15a)$$

where,

$$G(z) = \frac{1}{[1 + \{4n(1-2z)\}^2]^{0.5}}$$

$$G'(z) = \frac{32n^2(1-2z)}{[1 + \{4n(1-2z)\}^2]^{0.5}}$$

$$G''(z) = \frac{64n^2}{[1 + \{4n(1-2z)\}^2]^{1.5}} \left[ \frac{3(4n(1-2z))^2}{[1 + \{4n(1-2z)\}^2]^2} \right]$$

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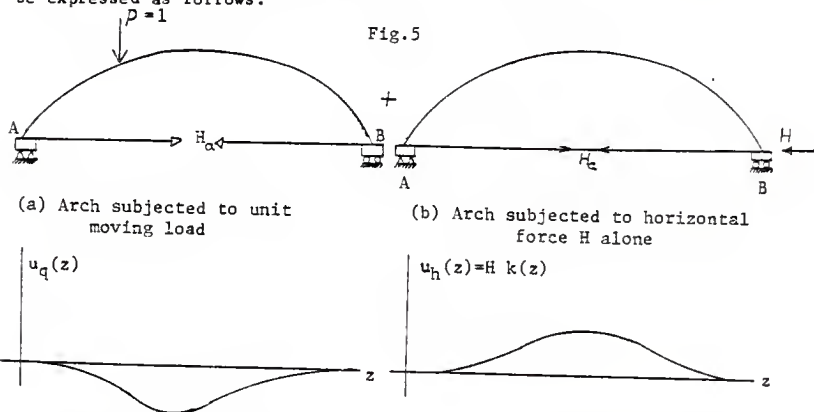
$$r = \frac{L^2}{EI}$$

Knowing the boundary values for the solution of a differential equation, an approximate solution at any section can be determined using the Runge-Kutta method of integration.

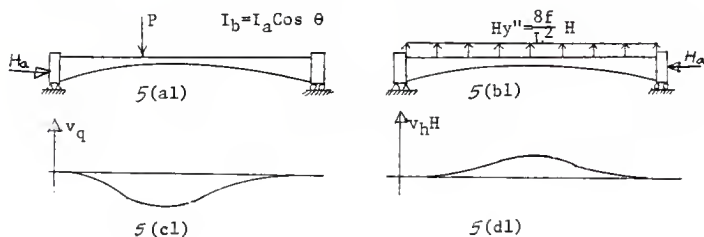
## Numerical solution of the differential equation

The solution for the deflection of a flexible fixed ended arch under the application of a unit force is discussed in this section.

An arch with a preassigned horizontal reaction force  $H_a$  can be visualized as a prestressed elastic arch as shown below. Our interest is in finding the deflection under a unit vertical force applied at  $z = z_0$ . The decomposition of the deflection functions can be expressed as follows.



The mathematical model, presented above, can also be seen as a beam with varying moment of inertia  $I_b = I_a \cos \theta$ , where  $I_a$  is the  $MI$  of the arch.



The value of H can be obtained by making the relative displacement between A and B equal to zero, as given by eqn ( 10b ).

In order to use Runge-Kutta method of integration the fourth order differential equations of ( 14 ) and ( 15 ) can be transformed into two equivalent systems of four first order differential equations as follows.

#### 1. Effects due to a unit external load

$$\text{Letting } [u_q, u'_q, u''_q, u'''_q] = [\theta_1, \theta_2, \theta_3, \theta_4] = \theta$$

Equation (14) yields the following system.

$$D_z(\theta_1) = \theta_2$$

$$D_z(\theta_2) = \theta_3$$

$$D_z(\theta_3) = \theta_4$$

$$G \{D_z(\theta_4)\} = - [(G'' + g^2) \theta_3 + 2 G' \theta_4 - Q] \quad (16)$$

$$\text{BC } \theta_1(0) = \theta_2(0) = \theta_1(1) = \theta_2(1) = 0$$

Choosing the loading location  $z = z_0$  as the shooting point, the following sets of initial values of  $\theta$  for two homogeneous solutions are assumed.

$$\theta^1(0) = \begin{Bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{Bmatrix}, \theta^2(0) = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{Bmatrix}, \theta^3(1) = \begin{Bmatrix} 0 \\ 0 \\ 1 \\ 0 \end{Bmatrix}, \theta^4(1) = \begin{Bmatrix} 0 \\ 0 \\ 0 \\ 1 \end{Bmatrix} \quad (16a)$$

By integrating from the two ends, the solutions for equation ( 14 ) can be expressed as the superposition of the two homogeneous solutions.

$$\text{For } z < z_0, \quad \theta(z) = C_1 \theta^1 L + C_2 \theta^2 L \quad (17)$$

$$\text{For } z > z_0, \quad \theta(z) = C_3 \theta^3 R + C_4 \theta^4 R \quad (18)$$

L and R in the superscript indicate left or right of the section under consideration.

The constants  $C_1, C_2, C_3, C_4$  are determined from the condition that, at the loading point, deflection, slope, moment and shear difference obtained by integration from the two ends should match with the load.

Hence at the loading point  $z = z_0$ , each component of the solution vectors should satisfy the following conditions of continuity.

$$\begin{aligned}\theta_1^L &= \theta_1^R \\ \theta_2^L &= \theta_2^R \\ \theta_3^L &= \theta_3^R\end{aligned}\quad (18a)$$

The fourth condition for determination of the solution is to use the equilibrium condition  $F_y = 0$ ,

$$-(G' \theta_3^L + G \theta_4^L) + (G' \theta_3^R + G \theta_4^R) = 1$$

at the loading point.

Substituting the obtained coefficients into equations (17) and (18), we can get the solution for equation (14).

## 2. Effects due to unit horizontal arch reaction

In order to find the required horizontal reaction force  $H$ , the deflection of the structure under the application of a unit horizontal force is used for calculating the deflection of the structure.

$$\text{Letting } [u_h, u_h', u_h'', u_h'''] = [k_1, k_2, k_3, k_4] = k$$

Equation (15) yields the following system of first order differential equations.

$$D_z(k_1) = k_2$$

$$D_z(k_2) = k_3$$

$$D_z(k_3) = k_4$$

$$G \{D_z(k_4)\} = - [(G'' + g) k_3 + 2 G' k_4 + 8 n r] \quad (19)$$

and the boundary conditions at the ends are,

$$k_1(0) = k_2(0) = k_2(1) = k_4(1) = 0$$

Using the conditions of deformation for a symmetrical structure under the application of symmetric loading, the boundary conditions can be written as,

$$k_1(0) = k_2(0) = k_3(1/2) = k_4(1/2) = 0$$

The solution can now be obtained as a superposition of two homogeneous solutions and a particular integral.

The initial values of  $k^{(i)}$  are assumed as,

$$k^{(1)}(0) = \begin{matrix} 0 \\ 0 \\ 1 \\ 0 \end{matrix}, \quad k^{(2)}(0) = \begin{matrix} 0 \\ 0 \\ 0 \\ 1 \end{matrix}, \quad P(0) = \begin{matrix} 0 \\ 0 \\ 0 \\ 0 \end{matrix}$$

$P(z)$  is for the particular integral of the solution using homogeneous boundary conditions and,  $k^{(1)}(z)$  and  $k^{(2)}(z)$  are solutions of the homogeneous differential equation. Integrating from left end to the crown of the arch, the solution for equation (15) can be expressed as,

$$k(z) = P(z) + D_1 k^{(1)}(z) + D_2 k^{(2)}(z) \quad (19a)$$

Slope and shear at the center of the arch are,

$$\begin{aligned} k_2(1/2) &= P_2(1/2) + D_1 k_2^{(1)}(1/2) + D_2 k_2^{(2)}(1/2) \\ k_4(1/2) &= P_4(1/2) + D_1 k_4^{(1)}(1/2) + D_2 k_4^{(2)}(1/2) \end{aligned} \quad (19b)$$

Solving for  $D_1$  and  $D_2$  equations (19b) and substituting them into (19a) yields the solution of the deflection of arch under the application of a unit horizontal force.

# Calculation of influence line coefficients

The solutions for equations ( 16 ) and ( 19 ) are obtained by assuming the value of  $g$ , which is given by,

$$g^2 = \frac{H_a L^2}{EI}$$

The unknown horizontal arch reaction  $H$  can be determined by making use of the additional constraint condition,

$$\int_0^L v' y' dx = 0$$

As defined earlier,

$$v = v_q + H v_h$$

$$v' = v'_q + H v'_h$$

But,  $v_q = u_q L$

$$v_h = u_h L$$

Therefore,

$$v' = ( u'_q + H u'_h ) L$$

Also,  $y' = -\frac{4f}{L} \left[ 1 - \frac{2x}{L} \right]$

$$= [4f (1 - 2z)] \frac{1}{L}$$

$$= \frac{1}{L} y'(z)$$

Hence,

$$\int_0^L ( u'_q + H u'_h ) y'(z) dz = 0$$

The horizontal force can be obtained by,

$$H = \frac{\int_0^L u'_q y' dz}{\int_0^L u'_h y' dz}$$



The non-dimensional function for  $v$  and its derivatives can be expressed as,

$$u_i = \theta_i + H k_i$$

for,  $i = 1, 2, 3, 4$

The influence lines for the moment  $M$ , vertical shearing force  $V$  and thrust  $TH$  induced in the arch due to a moving unit load can therefore be written as,

$$M(z, \bar{z}, g) = -G(z) u_3(z, \bar{z}, g)$$

$$V(z, \bar{z}, g) = D_z(v) = -[G(z) u_4(z, \bar{z}, g) + G'(z) u_3(z, \bar{z}, g)]$$

$$N(z, \bar{z}, g) = H(z, g) \cos(\theta(z)) + V(z, \bar{z}, g) \sin(\theta(z))$$

Thus, for any assumed value of  $g$ , the influence line for internal force component at the section of interest can be obtained.

## Procedure for stress analysis

The stresses at any section of the arch due to the given set of loading can be determined as follows.

Using a set of influence line for  $M(z, \bar{z}, g)$ , a set of  $M$  for a given loading condition corresponding to the selected values of  $g$  are determined.

Under the same loading conditions, the values for horizontal reaction and the thrust force at the section are calculated corresponding to the  $g$  values selected.

Therefore a set of points for functions  $M(g)$ ,  $N(g)$  and  $H(g)$  over a selected  $g_1, g_2, \dots, g_n$  are obtained.

$$\text{Let } g^* = \frac{H_a L^2}{EI}$$

The correct value of  $g$ , say  $g_o$ , is obtained such that  $H_{\text{calculated}}$  and  $H_{\text{assumed}}$  agree with each other. The sectional moment of interest  $M$ , under any given loading condition, can be calculated by using  $H(g)$  such that,

$$g^*(g_o) = g_o$$

and is shown in Fig (1) of Appendix 1.

## Numerical analysis

The computer program written in FORTRAN, by Wang<sup>[4]</sup>, was converted to BASIC language and made to work on the mini-computer TRS 80 Model II. The program was suitably modified to find the numerical solution for the loaded model shown below.

A dead load of 5 lbs at each of the loading points, as in the experiment, is used. The ratio of rise to span is 0.1333 and values of 0, 0.318, 0.636 for  $g$  were assumed. Three types of moving loads 1 lb, 5 lbs and 10 lbs were considered. The computer program, in BASIC language, is listed in Appendix 2. The results obtained for the various loading cases are tabulated. The sketch given below illustrates the method of determining the stresses.

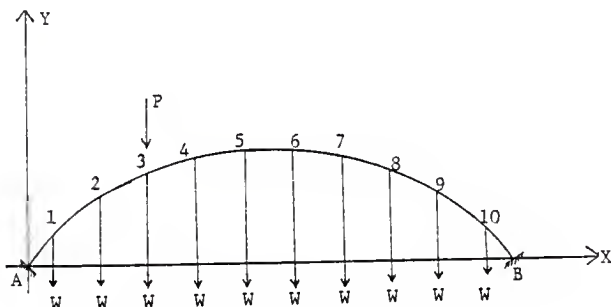


Fig.6 Loading points on the arch

W = Dead load

P = Moving load

## Experimental investigation

To verify the accuracy of the deflection theory, an experimental setup was designed. An arch model, made of steel, with fixed ends was built in the laboratory. The investigation was carried out for a number of loading conditions. Automatic data acquisition system, with an Apple - minicomputer, was used to record the strains registered by the strain gages. The strains were stored on a floppy disk.

It should be mentioned at this stage that, initially a rise of 12 inches and span of 60 inches was taken. But the strain induced in the middle third of the arch due to its profile was found to have crossed the yield strain of the arch material. This was also observed through the permanent strain set in the steel arch. Hence, another arch with a reduced rise of 8 inches and with the same span of 60 inches was built.

A series of experiments were conducted. Moving load was moved from one point to another and at each position the strains were read. There were totally ten loading points. Thus for each moving load there existed ten cases. On the outset, the experiment consisted of two phases. One phase was carried out with dead load and the other without the dead load. Application of dead load was achieved by hanging equal load at all the ten loading points.

Moving loads used, for the case without dead load, were 0.5, 1, 2, 4, 6, 8 and 10 lbs. It was observed that there was negligibly small response from the arch when the loads were below 2 lbs. Therefore, only five types of moving loads were considered for the

second case when the dead load was applied. The total dead loads considered in the experiment were 10 lbs through 80 lbs at intervals of 10 lbs. For each type of dead load, five tests were carried out for the five moving loads. The data got from all these experiments were stored on a floppy diskette to be retrieved at a later stage. But later on it was discovered that, not all the data had been saved on the disk. Failure of the efforts to retrieve all the data led to the repetition of the experiments.

This time the tests were repeated for dead loads ranging from 10 lbs to 90 lbs at intervals of 10 lbs. The five types of moving loads used were the same as those used previously. The computer was directed to print out the data as and when it received. A computer program was written to calculate the stresses, making use of the strains obtained from the experiment. These stresses were then compared with the stresses calculated from theory. This study showed a discrepancy of as high as 80% at some sections. In an attempt to understand the reason for this, all the stresses were normalized to a unit load. The normalized values were then compared with the corresponding calculated values. The comparison proved to be very much satisfactory, with an average accuracy of 90% , except for the cases when the moving loads were applied at the extreme two points.

This outcome called for a recheck of the experimental setup. Closer inspections indicated the possibility of frictional forces, offered by the pulleys, being the main reason for the discrepancy in the final stresses obtained for the extreme points. Several trial experiments confirmed that the moving loads being used were too small to overcome the frictional resistance coming from the pulleys. This fact led to another set of experiments with moving loads of higher

magnitude applied at the two outermost loading points.

A constant dead load of 50 lbs was maintained while the moving loads were varied from 2 lbs to 20 lbs at an interval of 2 lbs. Many sections of the arch were found to respond better when the moving load was above 10 lbs. Another BASIC program was written to make use of this new set of data and to compute the stresses for 1 lb, 5 lb and 10 lbs, by interpolation. The calculation of the stresses indicated an improvement with an accuracy of as high as 75% . The comparison between the experimental and theoretical stresses at the central span section, and the percentage accuracy achieved are given in the tables in Appendix 1. The stresses calculated for the other sections are given in Appendix 2.

## Construction of the flexible arch model

The experiment was conducted on a fixed-fixed parabolic arch of span 60 inches. A wooden formwork for bending the arch into the desired parabolic profile was prepared and bolted on to the steel baseplate. The model was built horizontally on the baseplate which in turn was placed on a table.

To achieve the fixity at the ends, the movement in the three directions was considered and taken care of. The horizontal motion was controlled by two channel sections placed on either side of the arch model. The two sections were securely bolted to the baseplate. In addition a hat section was designed to resist the rotational movement. To allow for free movement of the arch, when loaded, and also to restrict its movement in the transverse direction, rollers were provided underneath the model at five locations.

The loads were applied symmetrically on the arch model at ten points. Five sections were chosen for analysing the stresses induced due to the applied loading. Aluminium wires were made use of for transferring the loads onto the arch. The wire ran parallel to the table-top and over a pulley to be connected to cylindrical loading bowl, prepared for the purpose. Six strain gages, 3 on the topface and 3 on the bottom face, were mounted at each of the five locations.

## Material properties of the arch

Material : Cold rolled mild steel  
Dimensions : 1 inch wide and 0.125 inch thick  
Span of the arch : 60 inches  
Rise of the arch : 8 inches

Steel was selected as the material for making the arch. Three specimens were prepared for tension testing. Riehlers testing machine was made use for the purpose. Two specimens were tested using the extensometer and the automatic graphical ability available in the Riehlers machine. The other specimen was tested for tension on the Riehlers machine, with the help of a dial gage. The two tests yielded comparable results. Fig (2) in Appendix 1 shows the stress-strain curve for the arch material.

The following results were obtained.

Maximum load taken by the specimen = 3670 lbs  
Ultimate load = 2800 lbs  
Young's modulus =  $30 \times 10^6$  psi



## Fixity at the ends

Achieving fixity at the ends of the arch was one of the most important part in the experiment. As it can be visualized, the ends are said to be fixed if the movement of the end section is prevented in the three directions. The movement in the X and Y directions were locked by bolting the arch to two channel sections. To achieve proper lockage, one of the channels was first bolted firmly to the baseplate. The arch was then bolted to the two channel sections. Note that, at this stage the second channel was still not bolted to the baseplate. Only after the arch was bolted tightly to the two sections, was the second channel section secured to the baseplate. To achieve this, slot holes were drilled for the second channel in the baseplate. This procedure was followed to ensure proper fixture of the arch with the channel section.

In order to lock the rotational movement, and also to increase the moment of inertia at the end section, a hat section was designed. Five flat plates were welded together, as shown in the sketch, to form the hat section. The welded section was bolted to the channels and the baseplate.

The section thus built was satisfactory. In fact, after the wooden formwork was removed, the steel arch remained in its intended parabolic form. This was tested by putting the formwork back into its place, and the bolts in the formwork went right into the tapped holes made for them in the baseplate.

## Roller supports

The main idea of testing the arch by placing it horizontally on the table was to reduce the possibility of the arch's movement in the transverse direction. The arch will move in the transverse direction if the loading points do not pass exactly through the central section of the arch. By providing the rollers underneath the arch would reduce this problem. In the experiment, rollers were provided at five places.

Rollers also helped the arch in its free movement, caused due to the application of loads. The rollers were bolted to wooden blocks which in turn were made to sit under the arch. Care was taken to see that the roller-seat did not cause too much friction to the arch.

## Mounting of strain gages

As mentioned earlier, five sections (symmetrical about the center line) were chosen for analysing the stresses. With six gages at each section, totally thirty gages were mounted. The surface where the gage was being mounted was carefully prepared by sanding away the dirt and rust to obtain a smooth, but not a highly polished surface. Solvents such as the degreaser and the neutralizer were then employed to remove all traces of oil or grease and to give the surface a proper chemical affinity for the adhesive. The location on the arch was accurately marked and the gage positioned with the help of a rigid transparent tape. As the bonded type of strain gage is a high quality precision resistor, it must be attached to the specimen with a suitable adhesive.

M-Bond 200 was used as the adhesive in the present work. Maintaining the position and orientation of the gage by the tape, the adhesive was carefully applied. Since the adhesive is sufficiently strong to control the deformation of the strain-sensitive element in the gage, any residual stresses developed in the adhesive will influence the output of the strain gage. The adhesive was, therefore, subjected to gentle pressures over a suitable length of period to ensure a complete cure. After the gages were properly bonded to the structure, three lead wires were attached to the gage through anchor terminals. Since the strain gages are relatively fragile, care must be taken in attaching the lead wires to the soldering tabs. The properties of the strain gages, classified as Student gages by the Measurement Group Inc, are as follows.

Gage type	: EA - 06 - 240LZ - 120
Resistance in ohms	: $120.0 \pm 0.3 \%$
Gage factor at $75^{\circ}\text{F}$	: $2.045 \pm 0.5 \%$
Option	: E

As described by the suppliers, student strain gages are EA-series gages and are constructed with a 0.001 inch tough, flexible polyimide film backing. All student gages include option E, a polyimide encapsulation of the grid face, with exposed solder tabs. Normal use temperature range for static strain measurements is  $-100^{\circ}\text{F}$  to  $+350^{\circ}\text{F}$ .

The five sections chosen for analysing the stresses along with the positioning of the gages are shown in the sketch below.

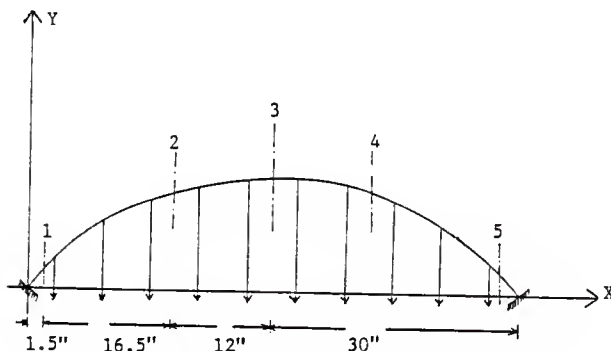


Fig.7 Strain gage sections

Loading applied on the structure was symmetrical. Loads were applied at ten points. Aluminium wires were used to transfer the load on the arch. Calculation of the buckling load was made by making use of the tables given in references [ 1 ] and [ 6 ].

### Calculation of the buckling load

From reference [1],

$$q_{cr} = \frac{g_4 EI}{L^3}$$

where  $g_4$  is obtained from the table below.

$f/L$	0.1	0.2
$g_4$	60.7	101.0

By interpolation, for  $f/L = 0.1333$ ,  $g_4 = 74.133$

$$q_{cr} = \frac{[74.133 \times 30 \times 10^6 \times \{1 \times (1/8)^3\}]}{60^3 \times 12}$$
$$= 1.67582 \text{ lbs/in}$$

Calculation from reference [6] yielded,

$$q_{cr} = 1.69 \text{ lbs/in}$$

Taking  $q_{cr} = 1.67582 \text{ lbs/in}$ ,

$$M_{cr} = \frac{q_{cr} L^2}{8} = \frac{1.67582 \times 60^2}{8}$$
$$= 754.119 \text{ lb-in}$$
$$H_{cr} = \frac{M_{cr}}{f} = \frac{754.119}{8}$$
$$= 94.265 \text{ lbs}$$

Sand and lead weights were used as loads on the structure. Special cylindrical loading bowls were prepared for the

purpose. Automatic data acquisition system, coupled with the apple minicomputer, was used to determine the strain. The free end of the lead wires coming from the strain gages were soldered to a pin connector. This pin is inserted into the sockets provided at the back of the data acquisition system.

The controller is essentially the brain of the data acquisition system and contains a microprocessor with several memory devices. The controller activates scanner and controls the time sequence of the switching from one channel to the next. Also, it stores the output, the channel number and the time when the reading is made in its operating memory. The final form of the data is then transmitted to the mini-computer.

#### Calculation of the stresses from the strains obtained

Let,  $E_t$  = Strain obtained from the top surface of the arch.

$E_b$  = Strain obtained from the bottom surface of the arch.

$A_a$  = Cross sectional area of the arch.

$M$  = Moment at the section under consideration.

$N$  = Thrust at the section under consideration.

Both the moment and thrust contribute to the strain at any section. As the arch is basically a compression member, the contribution from the thrust is negative.

$$E_t = - \frac{N}{A_a E} - \frac{Mc}{EI}$$

$$E_b = - \frac{N}{A_a E} + \frac{Mc}{EI}$$

Adding the two equations,

$$N = - \frac{AE}{2} (E_t + E_b)$$

Subtracting the two equations,

$$M = \frac{EI}{2c} (E_b - E_t)$$

Shear ( $V$ ) can also be calculated if the moments at two sections, a small distance apart, are known.

$$V = \frac{M_1 - M_2}{ds} \quad \text{where, } M_1 \text{ and } M_2 \text{ are the moments at two sections distance } ds \text{ apart.}$$

Thus, the stresses are determined from the strains obtained from the experiment. A computer program, in BASIC language, was generated to calculate the stresses as explained above.

## Numerical results

The following types of loadings have been considered and discussed here.

- 1 A moving load of 10 lbs with no dead load on the structure.
- 2 A moving load of 1 lb with a dead load of 50 lbs (which is about 53% of the buckling load) on the structure.
- 3 A moving load of 5 lbs with a dead load of 50 lbs on the structure.
- 4 A moving load of 10 lbs with a dead load of 50 lbs on the structure.
- 5 Static loads of 5 lbs, 10 lbs and 10 lbs at fourth, fifth and sixth loading points respectively, in addition to a dead load of 50 lbs on the structure.

A computer program was generated to calculate the moment and thrust from the strain data obtained and has been made to run on the Zenith - 100 mini-computer. A listing of the program is given in Appendix 2. The results obtained are tabulated and compared with the theoretical results. This comparison has been made at the center span. Influence lines for all the above loadings at three locations are drawn and shown through figures in Appendix 1.



## Comparison and Conclusion

As shown in Appendix 1 for the central span section, the moment values are in close agreement with the experimental values. For 10 lbs moving load, Table 2 shows that the accuracy is as high as 97%. The accuracy is found to be 73% when the load is acting at 1, indicating the failure of the load to influence the far off sections. The influence lines, at three sections are shown in Appendix 1 and the variation from the calculated values are marked.

However, it should be noted that at some sections the experimental moment values were normalized before being compared. The influence line diagram for the arch when a dead load of 50 lbs was present, failed to agree with the corresponding theoretical results. The reasons for the disagreement are due to a number of factors, the most significant one being the frictional force.

As it has been explained in an earlier chapter, aluminium wires used for applying the loads on the structure, were carried over pulleys. Careful inspection indicated that the loads applied on the structure failed to overcome the friction exerted by the pulleys. The response from the arch due to some of the loads was observed to be negligibly small. In order to overcome this limitation, a series of experiments were conducted, by increasing the magnitude of the moving load each time, with a constant dead load of 50 lbs. The magnitude of the moving loads ranged from 2 lb to 20 lbs at an interval of 2 lbs. In several of the cases, especially when the moving loads were near the ends, the arch was seen to respond only when the magnitude of the moving load was more than 10 lbs.

The results obtained from this series of experiments were then utilised in interpolating the strains for three moving load cases

of 1 lb, 5 lbs and 10 lbs. A computer program was generated for this interpolation and for the calculation of the stresses. It was observed that at some sections, the stresses were still not in agreement with the theoretical values. The experimental values were therefore normalized for a unit load. This treatment immediately yielded satisfactory results. The percentage variation of the values from the corresponding theoretical values are given in Appendix 1, for stresses as obtained due to a moving load of 10 lbs. The table indicates a very close agreement as the load approaches the section of interest. From this it could be clearly seen that, the influence of a load at any section of the arch is inversely proportional to its distance from the loaded point. The obvious reason is the frictional resistance from the pulleys.

Though utmost care was practiced in the mounting of strain gages, the possibility of human errors cannot be neglected. The characteristics of the adhesive used in mounting the gage are such that it can influence apparent gage factor, hysteresis characteristics, resistance to stress relaxation, gage resistance, temperature induced zero drift and insulation resistance<sup>[5]</sup>. Such sensitiveness could blow up very small errors and might influence the final results. In fact, six of the thirty gages mounted, failed to respond even though a check on their mounting and resistance indicated satisfactory results.

From table 1 in the Appendix, it could be seen that the variation in the moments is not linear as the load is increased from 1 lb to 10 lbs. This proves that the change in geometry of the structure has a considerable effect on the results.

However, further work in the area is required before using the method as a useful tool in the practical field.

## Recommendations

Placing the arch in a vertical position and applying the loads directly, without any pulleys, would yield better results. Such a setup will remove the frictional forces, which influenced the final results considerably, in the present work.

It is also recommended that the wires carrying the load, should be made to sit directly on the arch. Connection of the wire to an eyebolt will generate local moments which are considerably large near the ends. Eye bolts were initially used in the present work, and later removed, at all but middle two loading points of the arch, after the above mentioned phenomena was observed. In the middle section, the alignment of the eye bolts was seen to be along the loading line. The influence line diagram, shown in Fig (3) of Appendix 1, indicates an offset in the values obtained for the middle two points. Thus, it is observed that the local moments due to the eyebolts, however small they were, have affected the final results.

Also, the horizontal component of the displacement was not considered in the present work. Hence, in order to predict the behaviour of the structure with a much higher accuracy, it is recommended that the horizontal component be taken into consideration while formulating the equilibrium conditions in all future works.

## ACKNOWLEDGEMENT

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Thanks are also due to all friends and well wishers who offered their valuable and highly acknowledged help, during the construction of the arch model.

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## APPENDIX 1

### Tables and figures

TABLE 1

Loading at point no.	P = 1 lb		P = 5 lb		P = 10 lb	
	Calculated	Experimental	Calculated	Experimental	Calculated	Experimental
1	- 1.80	- 1.38	- 1.92	- 1.51	- 2.1	- 1.52
2	- 3.00	- 2.73	- 3.60	- 3.38	- 5.40	- 4.78
3	- 3.00	- 3.01	- 5.40	- 5.29	- 9.00	- 8.38
4	- 3.12	- 3.64	- 6.00	- 5.69	- 8.52	- 7.87
5	- 2.40	- 2.80	- 1.32	- 1.01	- 7.20	- 6.96

Experimental and calculated influence line coefficients for moment at the  
central section of the arch

TABLE 2

Loading at point no.	P = 1 lb (%)	P = 5 lbs (%)	P = 10 lbs (%)
1	76.76	78.63	72.31
2	90.80	93.82	88.55
3	99.55	98.04	93.13
4	83.33	94.90	92.32
5	83.34	76.54	96.72

Variation of Influence line coefficients for moment  
at the central section of the arch  
(in percentage)



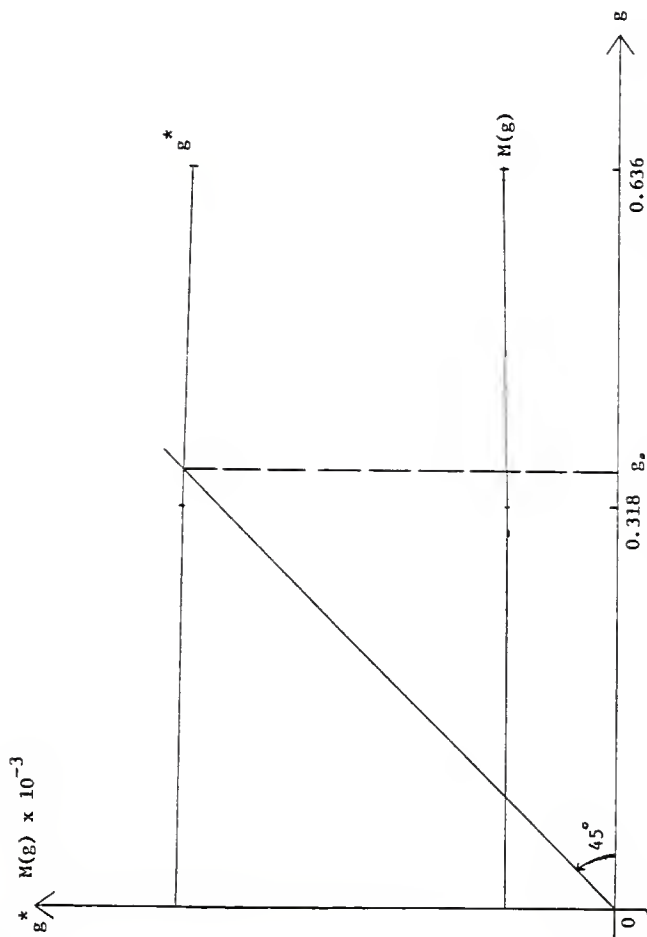
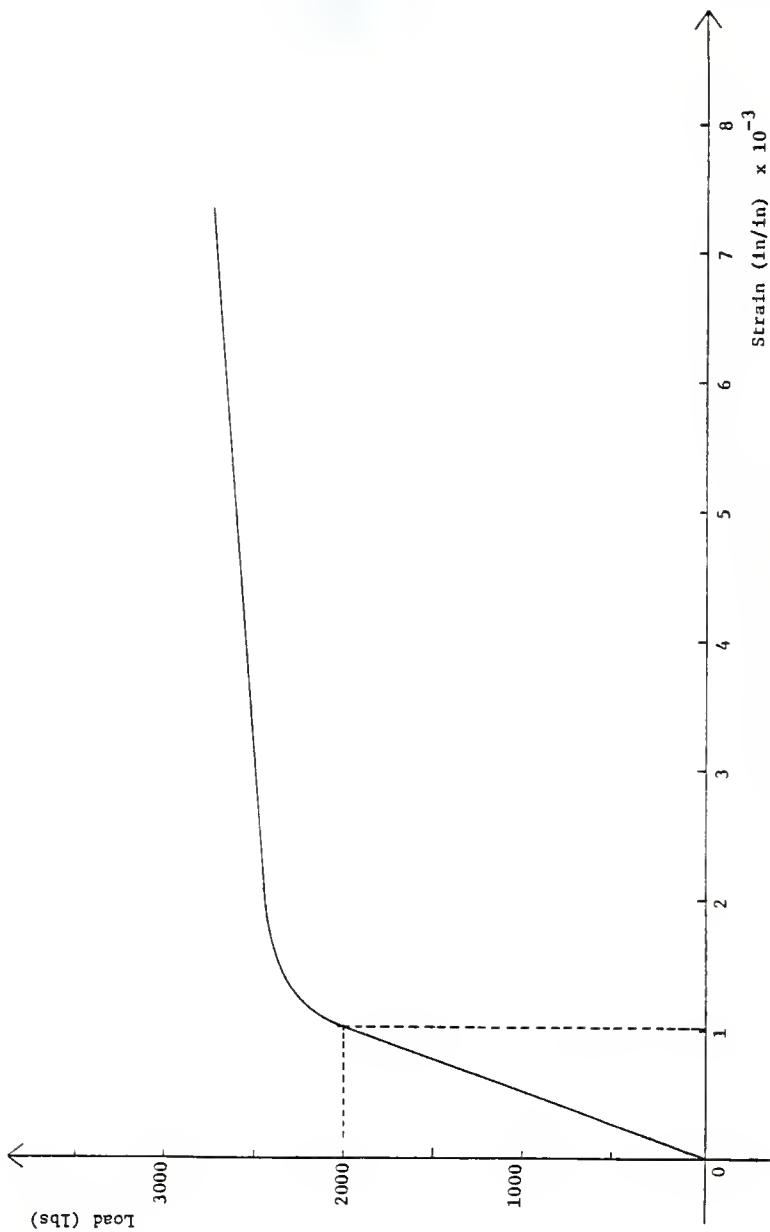


Fig A1 Graphical method to find the actual forces for the central section

Dead load = 50 lbs

Moving load = 10 lbs at loading point 1.



FigA2 Load vs Strain curve

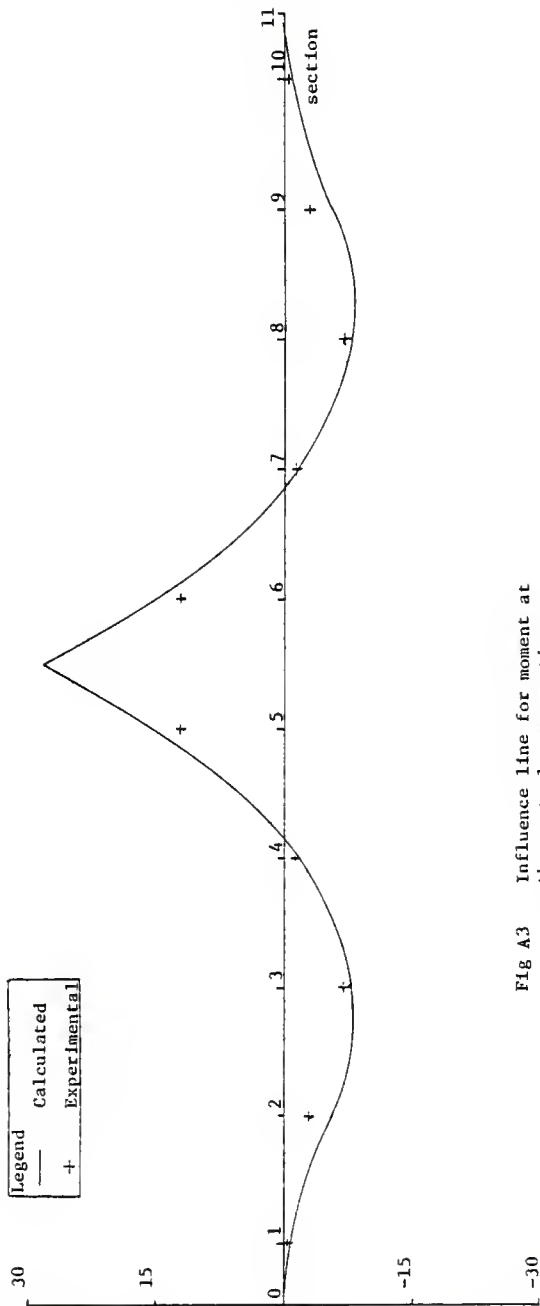


Fig A3 Influence line for moment at the central span section

Dead load = 50 lbs

Moving load = 10 lbs

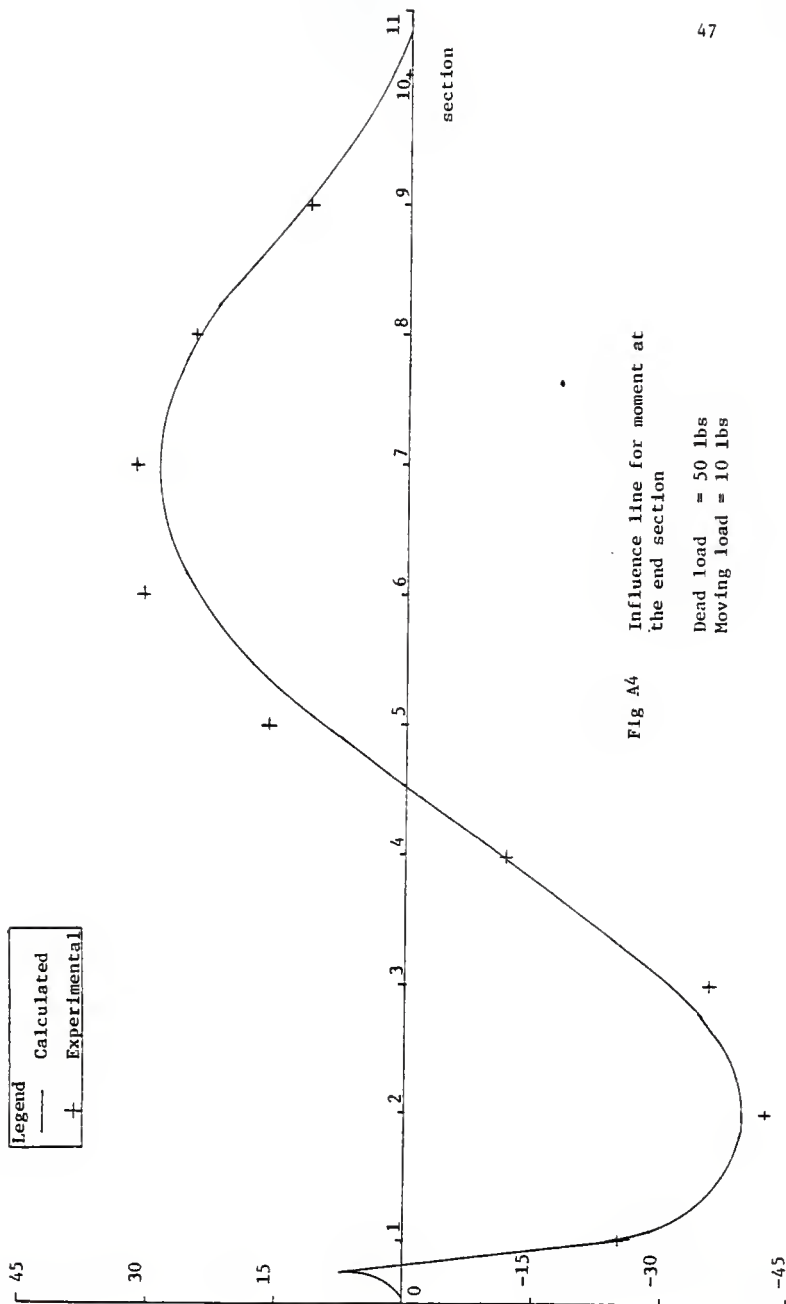


Fig A4 Influence line for moment at the end section

Dead load = 50 lbs  
Moving load = 10 lbs

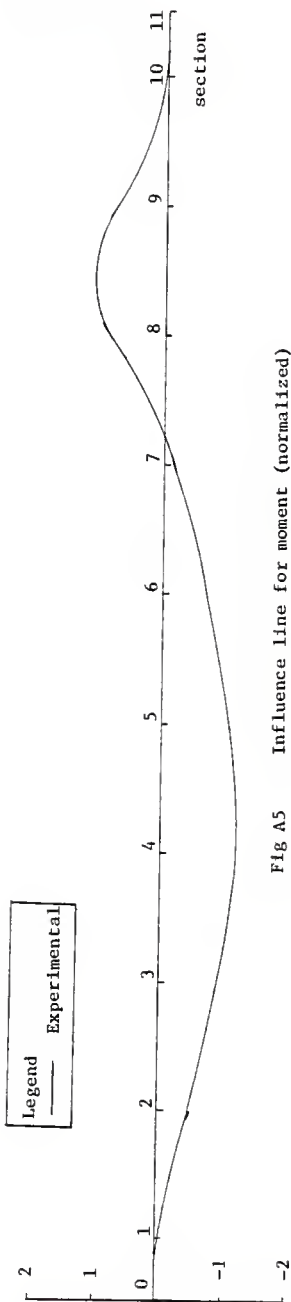


Fig A5 Influence line for moment (normalized)  
at 18" from right support

Dead load = 50 lbs

Moving load = 10 lbs

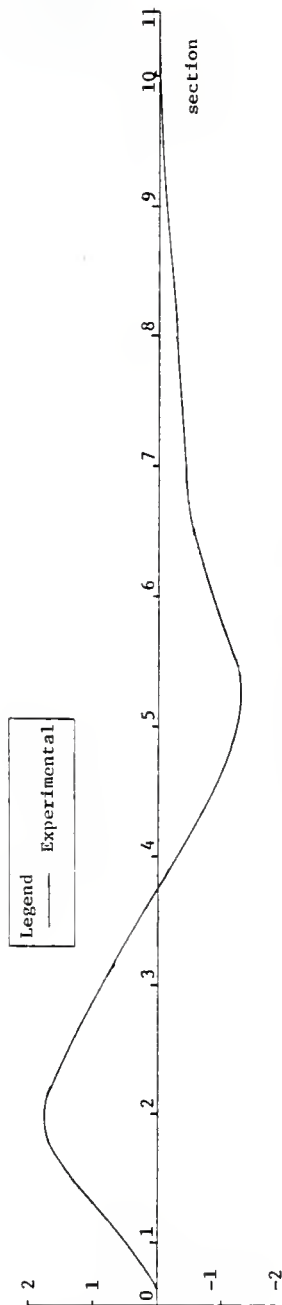
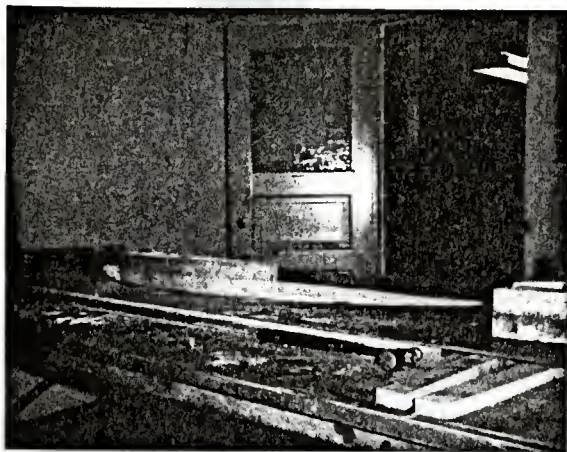


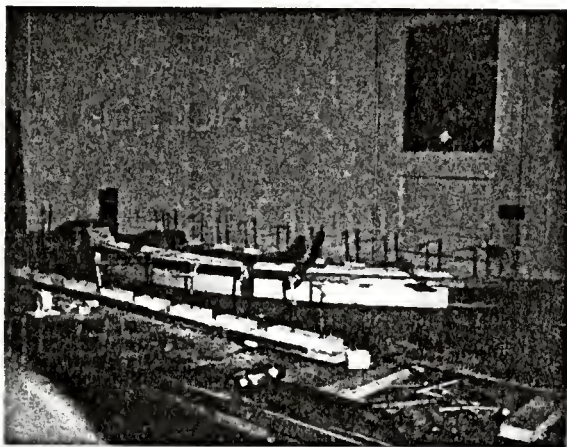
Fig A6 Influence line for moment (normalized)  
at 18" from left support

Dead load = 50 lbs

Moving load = 10 lbs



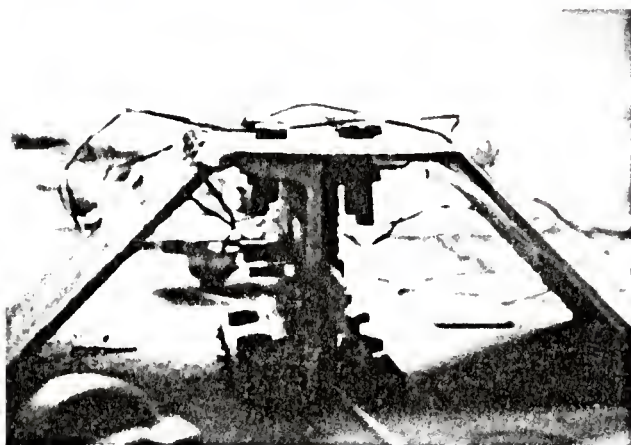
p1 Fixing the formwork



p2 Placing the arch

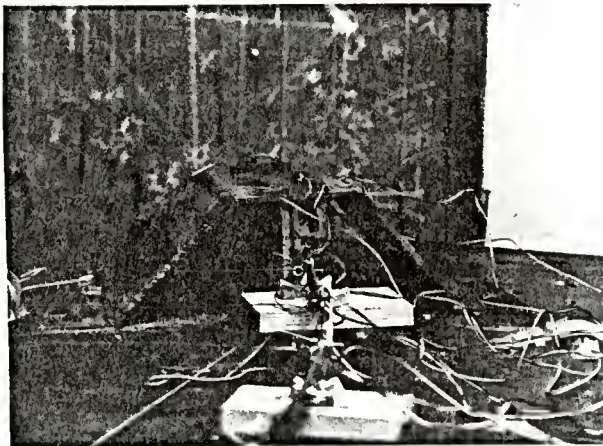


P3 The hat section

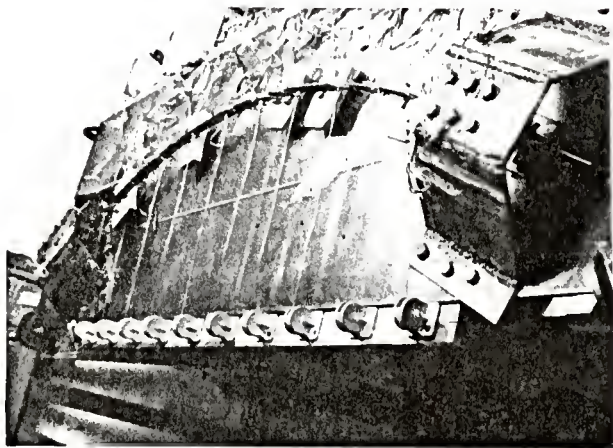


P4 Sectional view of the fixed end

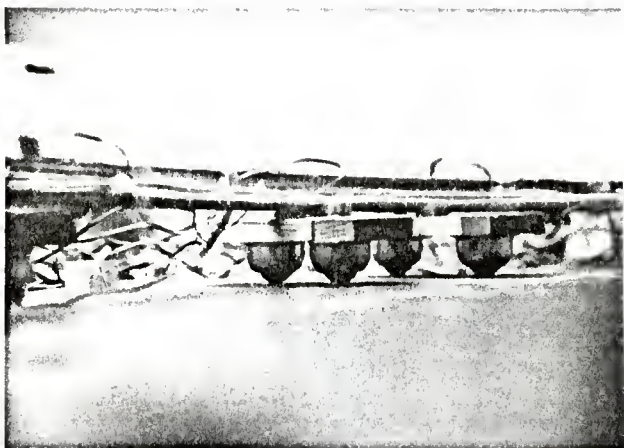




P5 General view of the end section



P6 The arch model



P7 Roller supports

APPENDIX 2  
Computer programs and results

```

10 REM
20 REM This program calculates the influence line coefficients for a
   fixed ended arch with constant moment of inertia.
30 REM
40 REM *****
50 REM Some of the variables used in the program are explained below
60 REM AN =>  $n=f/L$ 
70 REM G =>  $\cos(\theta)$ 
80 REM GP =>  $G' = dG/dx$ 
90 REM YP =>  $y' = dy/dx$ 
100 REM W1(I,J), TH(I,J), SV(I,J) => Moment, Thrust and Shear at
   section I of the arch due to unit load at J.
110 REM *****
120 DIM A(4,5), AA(4,21), AGN(4), ALM(8), AN(4), AP(4), AVN(4)
130 DIM BT(8,6,5), C(4), CN(21), DRIV(21), DX(21), DY(4), E(2)
140 DIM F(21), FA(3,21), G(21), GP(21), HF(4,21), HH(6,5), HX(21)
150 DIM IX(21), PA(3), PSA(8,6,5), PVA(4), Q(4)
160 DIM S(4,10,21), S1P(21), SAN(8,6,5), SMNY(4), SN(21), SPS(4,21)
170 DIM SS(6), ST(6), SV(6,21), SYMX(4)
180 DIM T(21), T1(21), TA(4), TH(6,21), TIG(4,21), TJP(4), TWH(4,21)
190 DIM U(8,6,5), W1(6,21), W2(11,21), W3(11,21), WH(4,4,21)
200 DIM XI(3), Y(4), YP(21), YY(5), Z(5)
210 PI=3.14159265358
220 EI=6000000
230 CLS
240 PRINT "In the present work, the rise to span ratio is 8/60 = 0.1333"
250 INPUT "Rise to span ratio =";AN(3)
260 PRINT : PRINT "Input the assumed values of H/Hcr"
270 PRINT "In the present work, Hcr was calculated as 94.34 [Ref Elastic Stability by Timoshenko]. Hmax expected was 60 lbs. H/Hcr = 60/94.34 = 0.636"
280 PRINT "For plotting we need a minimum of three points"
290 PRINT "Hence 0, (0+0.636)/2 and 0.636 were fed in as the input"
300 PRINT : PRINT : PRINT
310 FOR I=1 TO 3
320 INPUT "H/Hcr=";ALM(I)
330 NEXT I
340 II=3
350 FOR JJ=1 TO 3
360 X=0
370 H=1/20
380 FOR J=1 TO 21
390 G(J)=1/SQR(1+(4*AN(II))*(1-2*X))^2)
400 CN(J)=G(J)
410 YP(J)=4*AN(II)*(1-2*X)
420 SN(J)=YP(J)*CN(J)
430 GP(J)=32*AN(II)^2*(1-2*X)/((1+(4*AN(II)*(1-2*X))^2)^(3/2))
440 X=X+H
450 NEXT J
460 ALM(JJ)=PI*ALM(JJ)
470 NEQ=4
480 FOR J=1 TO 2
490 MN=J+2

```

```

500 FOR I = 1 TO 4
510 Q(I)=0
520 Y(I)=0
530 NEXT I
540 Y(MN)=1
550 FOR M=1 TO 4
560 WH(M,J,1)=Y(M)
570 NEXT M
580 X=0
590 KK=2
600 FOR K=2 TO 21
610 GOSUB 2360
620 FOR M=1 TO 4
630 WH(M,J,K)=Y(M)
640 NEXT M
650 NEXT K
660 NEXT J
670 KK=1
680 FOR J=1 TO 4
690 WH(J,3,1)=0
700 Y(J)=0
710 Q(J)=0
720 NEXT J
730 X=0
740 FOR J= 2 TO 21
750 GOSUB 2360
760 FOR K=1 TO 4
770 WH(K,3,J)=Y(K)
780 NEXT K
790 NEXT J
800 D=WH(2,1,11)*WH(4,2,11)-WH(2,2,11)*WH(4,1,11)
810 D1=-WH(2,3,11)*WH(4,2,11)+WH(2,2,11)*WH(4,3,11)
820 D2=-WH(2,1,11)*WH(4,3,11)+WH(2,3,11)*WH(4,1,11)
830 C1=D1/D
840 C2=D2/D
850 FOR J= 1 TO 4
860 J1=J+1
870 FOR M= 1 TO 11
880 JK=22-M
890 TWH(J,M)=C1*WH(J,1,M)+C2*WH(J,2,M)+WH(J,3,M)
900 TWH(J,JK)=TWH(J,M)*((-1)J1)
910 NEXT M
920 NEXT J
930 FOR J=1 TO 21
940 T1(J)=TWH(2,J)*YP(J)
950 NEXT J
960 N=21
970 GOSUB 2840
980 DTH=AR
990 FOR J=1 TO 21
1000 HF(1,J)=TWH(1,J)/DTH
1010 NEXT J
1020 FOR M=1 TO 21
1030 HF(3,M)=-G(M)*TWH(3,M)
1040 HF(4,M)=-GP(M)*TWH(3,M)-G(M)*TWH(4,M)
1050 NEXT M
1060 FOR J=1 TO 2
1070 MN=J+2
1080 CI=-1
1090 FOR M=1 TO 4

```

```

1100 CI=CI*(-1)
1110 FOR K=1 TO 21
1120 KM=22-K
1130 WH(M,MN,K)=WH(M,J,KM)*CI
1140 NEXT K,M,J
1150 FOR I=2 TO 20
1160 FOR J=1 TO 3
1170 FOR K=1 TO 4
1180 A(J,K)=WH(J,K,I)
1190 FOR L=1 TO 4
1200 A(4,L)=-GP(I)*WH(3,L,I)-G(I)*WH(4,L,I)
1210 A(L,5)=0
1220 NEXT L
1230 NEXT K,J
1240 FOR K=1 TO 4
1250 FOR J=3 TO 4
1260 A(K,J)=-A(K,J)
1270 NEXT J,K
1280 A(4,5)=1
1290 GOSUB 2140
1300 S1P(I)=0
1310 FOR J=1 TO 2
1320 S1P(I)=S1P(I)-A(J,5)*(GP(I)*WH(3,J,I)+G(I)*WH(4,J,I))
1330 NEXT J
1340 FOR J=1 TO 11 STEP 2
1350 I1=(J+1)/2
1360 SV(I1,I)=0
1370 W3(I1,I)=0
1380 IF J >= I THEN 1460
1390 FOR K=1 TO 2
1400 SV(I1,I)=SV(I1,I)-(GP(J)*WH(3,K,J)+G(J)*WH(4,K,J))*A(K,5)
1410 W2(I1,I)=HF(3,J)*HF(1,I)
1420 W3(I1,I)=W3(I1,I)-G(J)*A(K,5)*WH(3,K,J)
1430 W1(I1,I)=W3(I1,I)+W2(I1,I)
1440 NEXT K
1450 GOTO 1520
1460 FOR K=3 TO 4
1470 SV(I1,I)=SV(I1,I)-(GP(J)*WH(3,K,J)+G(J)*WH(4,K,J))*A(K,5)
1480 W2(I1,I)=HF(3,J)*HF(1,I)
1490 W3(I1,I)=W3(I1,I)-G(J)*A(K,5)*WH(3,K,J)
1500 W1(I1,I)=W3(I1,I)+W2(I1,I)
1510 NEXT K
1520 NEXT J
1530 NEXT I
1540 FOR I=1 TO 6
1550 W1(I,1)=0 : SV(I,1)=0 : SV(I,21)=0 : W1(I,21)=0
1560 NEXT I
1570 S1P(1)=1
1580 SV(1,1)=1
1590 FOR I=1 TO 6
1600 NP=2*I-1
1610 FOR J=1 TO 21
1620 TH(I,J)=HF(1,J)*CN(NP)+SV(I,J)*SN(NP)
1630 SV(I,J)=(SV(I,J)+HF(4,NP)*HF(1,J))*CN(NP)
1640 NEXT J
1650 ST(1)=HF(1,NP)*CN(NP)+S1P(1)*SN(NP)
1660 SS(1)=(S1P(1)+HF(4,NP)*HF(1,NP))*CN(NP)
1670 NEXT I
1680 FOR XI=1 TO 6
1690 FOR J=1 TO 21

```

```

1700 TWH(1,J)=W1(XI,J)
1710 TWH(2,J)=HF(1,J)
1720 TWH(3,J)=TH(XI,J)
1730 TWH(4,J)=SV(XI,J)
1740 NEXT J
1750 NP=2*X1-1
1760 AJJ=JJ-1
1770 AJJ=AJJ*0.2*PI
1780 LPRINT
1790 LPRINT "LAMBDA= ";AJJ
1800 LPRINT
1810 LPRINT "Influence lines for section #";NP
1820 LPRINT
1830 LPRINT "Moment", : LPRINT "Thrust", : LPRINT "SHEAR"
1840 FOR J=1 TO 21
1850 LPRINT W1(XI,J), : LPRINT TH(XI,J), : LPRINT SV(XI,J)
1860 NEXT J
1870 SYSTEM "T"
1880 IF XI < > 1 THEN 1920
1890 LPRINT
1900 GOTO 1990
1910 REM Change STH to HTS & SSV to VSS
1920 HTS=ST(X1)
1930 VSS=SS(X1)
1940 LPRINT
1950 REM LPRINT "(Special Jump Point)"
1960 REM LPRINT HTS : REM LPRINT VSS
1970 TJP(3)=HTS
1980 TJP(4)=VSS
1990 GOSUB 2940
2000 IF NP=11 THEN GOSUB 4100
2010 FOR J=1 TO 3
2020 PSA(JJ,XI,J)=PA(J)
2030 SAN(JJ,XI,J)=AGN(J)
2040 NEXT J
2050 FOR K=1 TO 3
2060 BT(JJ,XI,K)=T(K)
2070 NEXT K
2080 NEXT XI
2090 NEXT JJ
2100 PP=600
2110 D=1.3*PI
2120 END

```

```
2130 REM *****
2140 REM   Subroutine GJR(A)
2150 REM *****
2160 N=4
2170 N1=N+1
2180 DET=1.0
2190 FOR J=1 TO N
2200 DIV=A(J,J)
2210 S=1/DIV
2220 DET=DET*DIV
2230 FOR K=J TO N1
2240 A(J,K)=A(J,K)*S
2250 NEXT K
2260 FOR L=1 TO N
2270 IF (L-J)=0 THEN 2320
2280 AIJ=-A(L,J)
2290 FOR K=J TO N1
2300 A(L,K)=A(L,K)+AIJ*A(J,K)
2310 NEXT K
2320 NEXT L
2330 NEXT J
2340 RETURN
```



```

2350 REM *****
2360 REM Subroutine RKG
2370 REM *****
2380 REM The independent variable X is incremented in this Program.Y(I) & DY(I)
2390 REM are the dependent variable & its derivative.All the Q(I) must be initially
2400 REM set to zero in the main program.
2410 REM NEQ = Number of first order equations
2420 REM H = interval size
2430 E(1)=0.2928932188134524
2440 E(2)=1.7071067811865475
2450 H2=0.5*H
2460 GOSUB 2690
2470 FOR I=1 TO NEQ
2480 B=H2*DY(I)-Q(I)
2490 Y(I)=Y(I)+B
2500 Q(I)=Q(I)+3*B-H2*DY(I)
2510 NEXT I
2520 X=X+H2
2530 FOR JK=1 TO 2
2540 GOSUB 2690
2550 FOR I=1 TO NEQ
2560 B=E(JK)*(H*DY(I)-Q(I))
2570 Y(I)=Y(I)+B
2580 Q(I)=Q(I)+3*B-E(JK)*H*DY(I)
2590 NEXT I,JK
2600 X=X+H2
2610 GOSUB 2690
2620 FOR I=1 TO NEQ
2630 B=0.1666666666666666666666666666*(H*DY(I)-2*Q(I))
2640 Y(I)=Y(I)+B
2650 Q(I)=Q(I)+3*B-H2*DY(I)
2660 NEXT I
2670 RETURN

```

```
2680 REM *****
2690 REM   Subroutine deriv
2700 REM *****
2710 L=NEQ-1
2720 FOR I=1 TO L
2730 DY(I)=Y(I+1)
2740 NEXT I
2750 G=1/SQR(1+(4*AN(II)*(1-2*X))2)
2760 GP=32*AN(II)2*(1-2*X)/((1+(4*AN(II)*(1-2*X))2)3/2)
2770 SB=(-ALM(JJ)2)*Y(3)-64*(AN(II)2)*(48*AN(II)2*(1-2*X)2/(1
+16*AN(II)2*(1-2*X)2-1)/((1+16*AN(II)2*(1-2*X)2)3/2))*Y(3)
-2*GP*Y(4)
2780 IF KK=1 THEN 2810
2790 DY(4)=SB/G
2800 GOTO 2820
2810 DY(4)=(-8*AN(II)+SB)/G
2820 RETURN
```

```
2830 REM *****
2840 REM Subroutine INTGL
2850 REM *****
2860 AR=T1(1)-T1(N)
2870 M=N-1
2880 FOR I=2 TO M STEP 2
2890 J=I+1
2900 AR=AR+4*T1(I)+2*T1(J)
2910 NEXT I
2920 AR=AR*H/3
2930 RETURN
```

```

2940 REM *****
2950 REM Subroutine TINT60
2960 REM *****
2970 REM CHANGE ANV TO AVN ;PAV TO PVA ; A TO AA ; ANG TO AGN ; S
YMN TO SMYN ; Y TO YY
2980 NN=N+1
2990 FOR I=1 TO 3
3000 YY(I)=0
3010 Z(I)=0
3020 NEXT I
3030 FOR J=2 TO 20 STEP 2
3040 J1=J-1
3050 J2=J+1
3060 IF J=2 THEN 3100
3070 B=TWH(1,J1)*TWH(1,J)
3080 IF B > 0 THEN 3100
3090 GOTO 3210
3100 B=TWH(1,J)*TWH(1,J2)
3110 IF B > 0 THEN 3130
3120 GOTO 3290
3130 FOR I=1 TO 3
3140 IF N=1 THEN 3190
3150 IF I < = 2 THEN 3190
3160 IF J=NN THEN 3180
3170 GOTO 3190
3180 TWH(I,J1)=TJP(I)
3190 YY(I)=YY(I)+(TWH(I,J1)+4*TWH(I,J)+TWH(I,J2))/60
3200 NEXT I,J
3210 M=J1
3220 X=ABS(TWH(1,M))/(ABS(TWH(1,M))+ABS(TWH(1,M+1)))
3230 FOR I=1 TO 3
3240 YY(I)=YY(I)+TWH(I,M)*X/40
3250 Z(I)=Z(I)+(TWH(I,M)+4*TWH(I,M+1)+TWH(I,M+2))/60-TWH(I,M)*X/4
0
3260 NEXT I
3270 M=M+3
3280 GOTO 3360
3290 M=J
3300 X=ABS(TWH(1,M))/(ABS(TWH(1,M))+ABS(TWH(1,M+1)))
3310 FOR I=1 TO 3
3320 Z(I)=Z(I)+(1-X)*TWH(I,M+1)/40
3330 YY(I)=YY(I)+(TWH(I,M-1)+4*TWH(I,M)+TWH(I,M+1))/60-Z(I)
3340 NEXT I
3350 M=M+2
3360 FOR J=M TO 20 STEP 2
3370 J1=J-1
3380 J2=J+1
3390 IF J = 20 THEN 3460
3400 B=TWH(1,J1)*TWH(1,J)
3410 IF B > 0 THEN 3430
3420 GOTO 3560
3430 B=TWH(1,J)*TWH(1,J2)
3440 IF B > 0 THEN 3460
3450 GOTO 3460
3460 FOR I=1 TO 3
3470 IF N=1 THEN 3520
3480 IF I < = 2 THEN 3520
3490 IF J = NN THEN 3510
3500 GOTO 3520
3510 TWH(I,J1)=TJP(I)

```

```

3520 Z(I)=Z(I)+(TWH(I,J1)+4*TWH(I,J)+TWH(I,J2))/60
3530 NEXT I
3540 NEXT J
3550 GOTO 3770
3560 M=J1
3570 X=ABS(TWH(1,M))/(ABS(TWH(1,M))+ABS(TWH(1,M+1)))
3580 FOR I=1 TO 3
3590 Z(I)=Z(I)+TWH(I,M)*X/40
3600 YY(I)=YY(I)+(TWH(I,M)+4*TWH(I,M+1)+TWH(I,M+2))/60-TWH(I,M)*X
/40
3610 NEXT I
3620 M=M+3
3630 GOTO 3710
3640 M=J
3650 X=ABS(TWH(1,M))/(ABS(TWH(1,M))+ABS(TWH(1,M+1)))
3660 FOR I=1 TO 3
3670 YY(1)=YY(1)+(1-X)*TWH(I,M+1)/40
3680 Z(I)=Z(I)+(TWH(I,M-1)+4*TWH(I,M)+TWH(I,M+1))/60-(1-X)*TWH(I,
M+1)/40
3690 NEXT I
3700 M=M+2
3710 FOR J=M TO 20 STEP 2
3720 J1=J-1
3730 J2=J+1
3740 FOR I=1 TO 3
3750 YY(I)=YY(I)+(TWH(I,J1)+4*TWH(I,J)+TWH(I,J2))/60
3760 NEXT I,J
3770 IF YY(1) > 0 THEN 3840
3780 FOR I=1 TO 3
3790 AGN(I)=YY(I)
3800 T(I)=YY(I)+Z(I)
3810 PA(I)=Z(I)
3820 NEXT I
3830 GOTO 3890
3840 FOR I=1 TO 3
3850 PA(I)=YY(I)
3860 AGN(I)=Z(I)
3870 T(I)=YY(I)+Z(I)
3880 NEXT I
3890 GOTO 4040
3900 LPRINT "INTEGRATION OF INFLUENCE LINES"
3910 LPRINT " ", : LPRINT "MOMENT", : LPRINT "HOR. REACTION",
: LPRINT "THRUST"
3920 LPRINT "T.A.",
3930 FOR I=1 TO 3
3940 LPRINT T(I),
3950 NEXT I : LPRINT
3960 LPRINT "+ M ",
3970 FOR I=1 TO 3
3980 LPRINT PA(I),
3990 NEXT I : LPRINT
4000 LPRINT "- M ",
4010 FOR I=1 TO 3
4020 LPRINT AGN(I),
4030 NEXT I : LPRINT
4040 LPRINT : LPRINT : LPRINT : LPRINT
4050 RETURN
4060 END

```

```

4070 REM *****
4080 REM Stress Subroutine
4090 REM *****
4100 REM LO(1) => Moving load of 1 lb. LO(2) => Moving load of 5
1b. LO(3) => Moving load of 10 lb.
4110 LO(1)=1 : LO(2)=5 : LO(3)=10
4120 MS=0 : HS=0
4130 FOR TT=1 TO 3
4140 STOP
4150 FOR BB=2 TO 20 STEP 2
4160 MS=MS+W1(XI,BB)
4170 HS=HS+TH(XI,BB)
4180 NEXT BB
4190 LPRINT "LAMBDA= ";AJJ
4200 LPRINT "Loading Type      ", : LPRINT "H", : LPRINT "M", : LP
RINT "M-n"
4210 LPRINT
4220 FOR CC=2 TO 20 STEP 2
4230 LPRINT
4240 LPRINT "W=5# And P=";LO(TT), : LPRINT "at";CC/2,
4250 H=5*HS+LO(TT)*TH(XI,CC)
4260 M=(5*MS+LO(TT)*W1(XI,CC))*60
4270 LPRINT H,M,
4280 HN=(H-5*HS)/LO(TT)
4290 MN=(M/60 - 5*MS)/LO(TT)
4300 LPRINT MN
4310 NEXT CC
4320 LPRINT : LPRINT : LPRINT
4330 SYSTEM "T"
4340 NEXT TT
4350 RETURN

```

## Influence lines for section # 1

Moment	Thrust	SHEAR
0	.470497	.882402
-.0391564	.524804	.844894
-.05979	.662932	.746995
-.066213	.851708	.60841
-.0621867	1.053	.446069
-.0509659	1.27332	.274332
-.0353365	1.46352	.105186
-.0176485	1.61846	-.051593
1.5156E-04	1.72678	-.188292
.0164971	1.78069	-.299144
.0301808	1.77583	-.380238
.0403394	1.7112	-.429461
.0464462	1.58912	-.446473
.0483065	1.41525	-.432711
.0460618	1.19873	-.391426
.0401982	.952287	-.327756
.0315611	.692483	-.248819
.0213748	.43994	-.163846
.0112675	.21967	-.0843285
3.30014E-03	.0614073	-.0241931
0	0	0

## Influence lines for section # 3

Moment	Thrust	SHEAR
0	0	0
6.94316E-03	.057351	-.0326653
.0261098	.203433	-.118242
5.21727E-03	.795851	.679846
-7.75269E-03	1.0204	.536402
-.014574	1.2448	.383513
-.0167941	1.44892	.231465
-.0157511	1.61685	.0886846
-.0125902	1.7366	-.038126
-8.27546E-03	1.7999	-.143896
-3.60137E-03	1.80208	-.225106
7.98412E-04	1.74195	-.279738
4.4455E-03	1.6218	-.307254
7.01286E-03	1.44739	-.308592
8.32459E-03	1.22811	-.286203
8.35735E-03	.977082	-.244102
7.24549E-03	.71142	-.187949
5.28754E-03	.452471	-.125153
2.95588E-03	.226145	-.0649987
9.08022E-04	.0632706	-.0187873
0	0	0



## Influence lines for section # 5

Moment	Thrust	SHEAR
0	0	0
3.74148E-03	.0601519	-.0271644
.0144999	.21359	-.0987191
.0316093	.42415	-.201222
.0544456	.661116	-.323061
.0324234	1.20352	.498131
.0149922	1.42096	.365817
1.63469E-03	1.6015	.23935
-8.13843E-03	1.73256	.124281
-.0147909	1.80547	.0248881
-.0187653	1.81523	-.0557634
-.0204955	1.76047	-.115774
-.0203616	1.64341	-.154394
-.0187923	1.46989	-.17202
-.0161688	1.24946	-.170216
-.0128781	.995614	-.151751
-9.30553E-03	.725868	-.120663
-5.83787E-03	.462184	-.0823338
-2.86553E-03	.231228	-.043567
-7.84873E-04	.0647493	-.012794
0	0	0

LAMBDA= 0

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Influence lines for section # 7

Moment	Thrust	SHEAR
0	0	0
1.23903E-03	.0625528	-.0210549
5.38018E-03	.22234	-.0770139
.0129634	.44204	-.158094
.0244088	.689938	-.255791
.0400261	.939501	-.362785
.0600224	1.16901	-.472844
.034509	1.5698	.397251
.013507	1.71165	.29577
-3.04931E-03	1.79407	.204111
-.0153109	1.81179	.124827
-.0235124	1.76326	.0596744
-.0279751	1.65062	9.61698E-03
-.029109	1.47971	-.0251585
-.0274183	1.2602	-.0452577
-.0235081	1.00576	-.0521011
-.0180919	.734264	-.0479619
-.0120014	.469077	-.0360157
-6.19676E-03	.234414	-.0204025
-1.77854E-03	.0657	-6.29892E-03
0	0	0

## Influence lines for section # 9

Moment 0	Thrust 0	SHEAR 0
-5.64198E-04	.064399	-.0144542
-1.24933E-03	.229128	-.0535406
-7.20626E-04	.456052	-.111399
2.13668E-03	.712745	-.182861
8.23439E-03	.972058	-.263396
.0182965	1.21174	-.349061
.0328719	1.4141	-.436455
.0523461	1.56571	-.522678
.0269494	1.76323	.389066
6.76175E-03	1.78907	.312048
-8.28224E-03	1.74757	.242214
-.0183949	1.64072	.180745
-.0239371	1.47434	.128432
-.0254239	1.2581	.0856773
-.0235327	1.00574	.0524838
-.0191136	.735278	.0284445
-.013203	.469288	.012721
-7.0378E-03	.235266	4.01773E-03
-2.07299E-03	.0659989	5.4854E-04
0	0	0

LAMBDA= 0

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Influence lines for section # 11

Moment	Thrust	SHEAR
0	0	0
-1.66821E-03	.0655687	-7.54374E-03
-5.38867E-03	.233513	-.0289424
-9.44277E-03	.465294	-.0624119
-.0123708	.728117	-.106252
-.0129519	.994508	-.158835
-.0101857	1.24192	-.218602
-3.27688E-03	1.45241	-.284045
8.37877E-03	1.6123	-.353705
.025205	1.71203	-.426158
.0474526	1.7459	-.5
.025205	1.71203	.426158
8.3788E-03	1.6123	.353705
-3.2769E-03	1.45241	.284045
-.0101857	1.24192	.218602
-.0129518	.994508	.158836
-.0123708	.728117	.106252
-9.44276E-03	.465294	.062412
-5.38866E-03	.233513	.0289424
-1.66821E-03	.0655687	7.54389E-03
0	0	0

LAMBDA= 0 Loading Type	H	M	M-n
W=5# And P= 1 at 1	46.9531	-1.38093	-1.166825
W=5# And P= 1 at 2	47.3527	-1.84741	-1.944294
W=5# And P= 1 at 3	47.8818	-2.05795	-1.2952
W=5# And P= 1 at 4	48.3396	-1.47744	-1.327677
W=5# And P= 1 at 5	48.5991	.231482	2.52052
W=5# And P= 1 at 6	48.5991	.231483	2.52052
W=5# And P= 1 at 7	48.3396	-1.47744	-1.327682
W=5# And P= 1 at 8	47.8818	-2.05795	-1.29519
W=5# And P= 1 at 9	47.3527	-1.84741	-1.944293
W=5# And P= 1 at 10	46.9531	-1.38093	-1.166826

LAMBDA= 0 Loading Type	H	M	M-n
W=5# And P= 1 at 1	46.9531	-1.38093	-1.166025
W=5# And P= 1 at 2	47.3527	-1.84741	-.944394
W=5# And P= 1 at 3	47.8818	-2.05795	-1.2952
W=5# And P= 1 at 4	48.3396	-1.47744	-.327677
W=5# And P= 1 at 5	48.5991	.231482	2.52052
W=5# And P= 1 at 6	48.5991	.231483	2.52052
W=5# And P= 1 at 7	48.3396	-1.47744	-.327682
W=5# And P= 1 at 8	47.8818	-2.05795	-1.29519
W=5# And P= 1 at 9	47.3527	-1.84741	-.944293
W=5# And P= 1 at 10	46.9531	-1.38093	-1.166826

LAMBDA= 0  
Loading Type

	H	M	M-m
W=5# And P= 5 at 1	94.1028	-3.06214	-1.166825
W=5# And P= 5 at 2	96.101	-5.39454	-1.944294
W=5# And P= 5 at 3	98.7464	-6.44725	-1.2952
W=5# And P= 5 at 4	101.035	-3.54469	-1.327677
W=5# And P= 5 at 5	102.333	4.9999	2.52052
W=5# And P= 5 at 6	102.333	4.99991	2.52052
W=5# And P= 5 at 7	101.035	-3.54471	-1.327682
W=5# And P= 5 at 8	98.7464	-6.44724	-1.29519
W=5# And P= 5 at 9	96.101	-5.39454	-1.944293
W=5# And P= 5 at 10	94.1028	-3.06214	-1.166826

LAMBDA= 0				
Loading type	H	M	M-n	
W=5# And P= 10 at 1	141.318	-4.84344	-1.66825	
W=5# And P= 10 at 2	145.314	-9.50926	-.944294	
W=5# And P= 10 at 3	150.605	-11.6137	-1.2952	
W=5# And P= 10 at 4	155.193	-5.80856	-.327677	
W=5# And P= 10 at 5	157.779	11.2806	2.52052	
W=5# And P= 10 at 6	157.779	11.2806	2.52052	
W=5# And P= 10 at 7	155.193	-5.80858	-.327682	
W=5# And P= 10 at 8	150.605	-11.6137	-1.29519	
W=5# And P= 10 at 9	145.314	-9.50925	-.944293	
W=5# And P= 10 at 10	141.318	-4.84345	-1.66826	



Influence lines for section # 1

Moment	Thrust	SHEAR
0	.470497	.882402
-.0392444	.524524	.845171
-.0600514	.662217	.747767
-.0666355	.85078	.609586
-.0627064	1.0622	.447402
-.0515005	1.27297	.275553
-.0358054	1.4638	.106066
-.0179874	1.61942	-.0513013
-1.71661E-05	1.7283	-.188434
.0165121	1.78253	-.299772
.030368	1.77769	-.381227
.0406665	1.71275	-.430639
.0468657	1.59008	-.447654
.0467635	1.41546	-.433724
.0465018	1.19815	-.392151
.0405753	.951075	-.328143
.0318443	.690929	-.248901
.0215531	.438447	-.163731
.0113519	.21863	-.0841658
3.32133E-03	.0610223	-.024112
0	0	0

LAMBDA= .629319

77

Influence lines for section # 3

Moment	Thrust	SHEAR
0	0	0
6.94835E-03	.057396	-.0320222
.026108	.204062	-.115752
5.16221E-03	.797482	.684138
-7.87624E-03	1.02308	.541344
-.0147505	1.24859	.388179
-.016993	1.45379	.235177
-.0159383	1.62261	.0910195
-.012736	1.74295	-.0373442
-8.35906E-03	1.80644	-.144631
-3.61306E-03	1.80836	-.227148
8.57249E-04	1.74752	-.262754
4.56332E-03	1.62629	-.310836
7.17047E-03	1.45056	-.312317
8.49849E-03	1.2299	-.289679
8.52357E-03	.97764	-.247016
7.38333E-03	.711074	-.190107
5.3835E-03	.451695	-.126504
3.00666E-03	.225438	-.0656404
9.22608E-04	.0629717	-.018951
0	0	0

LAMBDA= .628319

78

Influence lines for section # 5

Moment	Thrust	SHEAR
0	0	0
3.78323E-03	.0599679	-.0270771
.0146449	.213341	-.0982947
.031874	.424409	-.200019
.0547868	.662636	-.320375
.0327487	1.20666	.502061
.0152356	1.4256	.369855
1.76575E-03	1.60738	.242691
-8.12393E-03	1.7393	.12644
-.0148797	1.81259	.0256547
-.0189328	1.82219	-.0563658
-.0207025	1.76677	-.117545
-.0205979	1.64862	-.157009
-.0190212	1.47372	-.175086
-.0163691	1.25183	-.173327
-.0130361	.996603	-.154546
-9.41573E-03	.725822	-.122869
-5.90269E-03	.461587	-.083807
-2.89435E-03	.230603	-.0443389
-7.917E-04	.0644704	-.0130033
0	0	0

LAMBDA= .628319

79

Influence lines for section # 7

Moment	Thrust	SHEAR
0	0	0
1.27291E-03	.062233	-.021255
5.50521E-03	.221571	-.0776821
.0132158	.441169	-.159245
.0247954	.689506	-.257138
.0405161	.940059	-.363718
.0605374	1.17101	-.472427
.0349347	1.57329	.399032
.0137676	1.71627	.297998
-2.98271E-03	1.79934	.206158
-.0154302	1.81719	.126324
-.0237843	1.76826	.0604591
-.0283506	1.65478	9.69763E-03
-.0295326	1.48271	-.0256532
-.0278357	1.26193	-.0461251
-.0238734	1.00631	-.0531106
-.0183732	.73392	-.0488976
-.0121846	.467302	-.0367163
-6.28787E-03	.233704	-.0207936
-1.8032E-03	.0653978	-6.41631E-03
0	0	0

Influence lines for section # 9

Moment	Thrust	SHEAR
0	0	0
-5.55884E-04	.0640213	-.0147283
-1.21348E-03	.228136	-.0545214
-6.34806E-04	.454693	-.113308
2.29385E-03	.711456	-.185673
8.47709E-03	.97128	-.266821
.0186223	1.21181	-.352532
.033252	1.41518	-.439133
.0527135	1.56782	-.523459
.0272074	1.76611	.39029
6.85523E-03	1.79228	.314383
-8.36133E-03	1.75062	.244988
-.0186201	1.64321	.183485
-.0242604	1.47596	.130837
-.0257675	1.25874	.0875874
-.0238804	1.00548	.0538549
-.0193995	.734383	.0293172
-.0133992	.468183	.0131918
-7.13982E-03	.234399	4.21096E-03
-2.10172E-03	.065655	5.91385E-04
0	0	0

## Influence lines for section # 11

Moment	Thrust	SHEAR
0	0	0
-1.68451E-03	.0651908	-7.74203E-03
-5.44258E-03	.23252	-.0296811
-9.53616E-03	.463922	-.0639283
-.0124872	.726784	-.108648
-.0130604	.993621	-.162057
-.0102493	1.24176	-.22242
-3.26172E-03	1.45307	-.288041
8.49195E-03	1.61371	-.357263
.0254082	1.71395	-.428453
.0476975	1.748	-.5
.0254083	1.71395	.428453
8.4919E-03	1.61371	.357262
-3.26182E-03	1.45307	.288041
-.0102493	1.24176	.22242
-.0130604	.993621	.162057
-.0124871	.726784	.108648
-9.53618E-03	.463922	.0639282
-5.44258E-03	.23252	.0296811
-1.68453E-03	.0651908	7.74196E-03
0	0	0

LAMBDA= -628319  
Loading Type

	H	M	M-n
W=5# And P= 1 at 1	46.9521	-1.39182	-1.148456
W=5# And P= 1 at 2	47.3508	-1.05293	-1.951643
W=5# And P= 1 at 3	47.8803	-2.06437	-1.30605
W=5# And P= 1 at 4	48.3397	-1.47645	-1.326172
W=5# And P= 1 at 5	48.6005	.243769	2.54086
W=5# And P= 1 at 6	48.6005	.243772	2.54026
W=5# And P= 1 at 7	48.3397	-1.47645	-1.32617
W=5# And P= 1 at 8	47.8803	-2.06437	-1.30605
W=5# And P= 1 at 9	47.3508	-1.05293	-1.951635
W=5# And P= 1 at 10	46.9521	-1.39182	-1.168457

LAMBDA= .628319  
Loading Type

	H	M	M-n
W=5# And P= 5 at 1	94.0999	-3.06686	-.168456
W=5# And P= 5 at 2	96.093	-5.42242	-.953643
W=5# And P= 5 at 3	98.7409	-6.47964	-1.30605
W=5# And P= 5 at 4	101.038	-3.54	-.326172
W=5# And P= 5 at 5	102.342	5.06108	2.54086
W=5# And P= 5 at 6	102.342	5.06109	2.54086
W=5# And P= 5 at 7	101.038	-3.54	-.32617
W=5# And P= 5 at 8	98.7409	-6.47964	-1.30605
W=5# And P= 5 at 9	96.093	-5.42239	-.953635
W=5# And P= 5 at 10	94.0998	-3.06686	-.168457



LAMBDA= .628319  
Loading Type

W=5# And P= 10 at 1	H	M	M-n
	141.313	-4.85297	-.158456
W=5# And P= 10 at 2	145.299	-9.56409	-.953643
W=5# And P= 10 at 3	150.595	-11.6785	-1.30605
W=5# And P= 10 at 4	155.188	-5.79926	-.326172
W=5# And P= 10 at 5	157.796	11.4029	2.54086
W=5# And P= 10 at 6	157.796	11.4029	2.54086
W=5# And P= 10 at 7	155.188	-5.79926	-.32617
W=5# And P= 10 at 8	150.595	-11.6785	-1.30605
W=5# And P= 10 at 9	145.299	-9.56405	-.953635
W=5# And P= 10 at 10	141.313	-4.85298	-.168457

Influence lines for section # 1

Moment	Thrust	SHEAR
0	.470497	.882402
-.0395172	.523664	.846017
-.060862	.66003	.750153
-.0679522	.647935	.613237
-.0643354	1.05975	.45157
-.0531829	1.27189	.279388
-.0372877	1.46469	.108848
-.0190662	1.6224	-.0499325
-5.62757E-04	1.73301	-.188831
.0165462	1.78924	-.301692
.0309477	1.78343	-.384288
.0416908	1.71752	-.434308
.0481851	1.59383	-.451342
.0502045	1.41606	-.436902
.047892	1.19634	-.394439
.041768	.947291	-.329383
.0327408	.686187	-.249191
.0221182	.433631	-.163402
.0116199	.215429	-.0836814
3.3888E-03	.0598416	-.0238684
0	0	0

Influence lines for section # 3

Moment	Thrust	SHEAR
0	0	0
6.96214E-03	.0575783	-.0300192
.026096	.206137	-.108029
4.98413E-03	.802785	.697473
-8.2687E-03	1.03182	.556799
-.0153084	1.26094	.402844
-.0176208	1.46963	.24692
-.0165296	1.64136	.0984902
-.0131967	1.76366	-.0347407
-8.62281E-03	1.82779	-.146812
-3.64882E-03	1.82887	-.233476
1.04469E-03	1.76577	-.29219
4.93765E-03	1.64108	-.3221
7.67089E-03	1.46114	-.324062
9.0504E-03	1.23605	-.300658
9.05075E-03	.979809	-.256232
7.82025E-03	.710311	-.196937
5.68733E-03	.449485	-.130781
3.16725E-03	.223351	-.0676733
9.68672E-04	.0620779	-.0194704
0	0	0

Influence lines for section # 5

Moment	Thrust	SHEAR
0	0	0
3.91315E-03	.0594543	-.0267763
.0150963	.212759	-.0968766
.0326978	.425569	-.196114
.0558512	.667882	-.31186
.033769	1.21712	.514433
.0160048	1.4409	.38257
2.18631E-03	1.6267	.253248
-8.06804E-03	1.76142	.133295
-.0151486	1.83595	.0281245
-.0194521	1.8451	-.0582332
-.0213805	1.78756	-.12313
-.0213407	1.6659	-.165287
-.0197434	1.48655	-.184812
-.0170032	1.25989	-.183214
-.0135375	1.00026	-.163435
-9.766E-03	.726099	-.129886
-6.10915E-03	.459999	-.0884914
-2.98636E-03	.228802	-.0467285
-8.1357E-04	.0636479	-.0136678
0	0	0

## Influence lines for section # 7

Moment	Thrust	SHEAR
0	0	0
1.38047E-03	.0612805	-.0218692
5.90192E-03	.219308	-.0797284
.0140151	.438695	-.162758
.0260178	.688511	-.261229
.0420615	.942257	-.366514
.0621601	1.1778	-.47108
.0362795	1.58479	.404556
.0145954	1.73136	.304905
-2.76374E-03	1.81653	.212518
-.0157929	1.83479	.130975
-.0246380	1.78461	.0628915
-.0295381	1.66844	9.92646E-03
-.0308737	1.4927	-.027232
-.0291599	1.26784	-.0488774
-.0250339	1.00842	-.0563092
-.0192674	.733165	-.0518612
-.0127673	.465104	-.0389343
-6.5777E-03	.231614	-.022031
-1.88164E-03	.0644972	-6.78732E-03
0	0	0

## Influence lines for section # 9

Moment	Thrust	SHEAR
0	0	0
-5.28219E-04	.0628705	-.0155949
-1.0953E-03	.225111	-.0576211
-3.55294E-04	.450551	-.119334
2.80141E-03	.707554	-.194537
9.25326E-03	.968987	-.277591
.0196562	1.21216	-.363427
.0344498	1.41872	-.447542
.0538654	1.57457	-.525993
.0280153	1.77531	.393986
7.14596E-03	1.80248	.321599
-8.6133E-03	1.76035	.253653
-.0193326	1.65115	.192115
-.0252829	1.48121	.138465
-.0269387	1.2609	.09369
-.0249813	1.0048	.0582664
-.0203048	.731727	.0321454
-.0140206	.464848	.0147292
-7.46286E-03	.231773	4.8478E-03
-2.19265E-03	.0646118	7.34169E-04
0	0	0

## Influence lines for section # 11

Moment	Thrust	SHEAR
0	0	0
-1.73529E-03	.0640343	-8.37794E-03
-5.61024E-03	.229467	-.032051
-9.82654E-03	.459693	-.068784
-.0128479	.722666	-.116304
-.0133965	.990865	-.172319
-.0104454	1.24124	-.234534
-3.21328E-03	1.4551	-.300663
8.84377E-03	1.61805	-.368441
.0260379	1.71989	-.435624
.0484544	1.75451	-.5
.0260379	1.71989	.435624
8.84385E-03	1.61805	.368441
-3.2133E-03	1.4551	.300663
-.0104455	1.24124	.234534
-.0133965	.990865	.172319
-.012848	.722666	.116304
-9.82649E-03	.459693	.0687842
-5.61023E-03	.229467	.032051
-1.73527E-03	.0640343	8.37805E-03
0	0	0

LAMEJJA= 1.25664  
Loading Type

	H	M	M-n
W=5# And P= 1 at 1	46.9492	-1.38416	-.173529
W=5# And P= 1 at 2	47.3448	-1.86965	-.982666
W=5# And P= 1 at 3	47.8759	-2.08384	-1.33966
W=5# And P= 1 at 4	48.34	-1.47283	-.321306
W=5# And P= 1 at 5	48.6047	.282246	2.60382
W=5# And P= 1 at 6	48.6047	.282247	2.60382
W=5# And P= 1 at 7	48.34	-1.47284	-.321319
W=5# And P= 1 at 8	47.8759	-2.08384	-1.33965
W=5# And P= 1 at 9	47.3448	-1.86964	-.982664
W=5# And P= 1 at 10	46.9492	-1.38417	-.173531



LAMBDA= 1.25664  
Loading Type

	H	M	M-n
W=5# And P= 5 at 1	94.0909	-3.09068	-.173529
W=5# And P= 5 at 2	96.0684	-5.50809	-.982666
W=5# And P= 5 at 3	98.7237	-6.57907	-1.33966
W=5# And P= 5 at 4	101.044	-3.52401	-.321305
W=5# And P= 5 at 5	102.368	5.25137	2.60382
W=5# And P= 5 at 6	102.368	5.25137	2.60382
W=5# And P= 5 at 7	101.044	-3.52405	-.321319
W=5# And P= 5 at 8	98.7237	-6.57905	-1.33965
W=5# And P= 5 at 9	96.0684	-5.50809	-.982664
W=5# And P= 5 at 10	94.0905	-3.09069	-.173531

LAMBDA= 1.25664  
Loading Type

	H	M	M-n
W=5# And P= 10 at 1	141.296	-4.88131	-.173529
W=5# And P= 10 at 2	145.252	-9.73614	-.982666
W=5# And P= 10 at 3	150.562	-11.8781	-1.33966
W=5# And P= 10 at 4	155.203	-5.75798	-.321306
W=5# And P= 10 at 5	157.951	11.7828	2.60782
W=5# And P= 10 at 6	157.951	11.7828	2.60382
W=5# And P= 10 at 7	155.203	-5.76805	-.321319
W=5# And P= 10 at 8	150.562	-11.878	-1.33965
W=5# And P= 10 at 9	145.252	-9.73612	-.982664
W=5# And P= 10 at 10	141.296	-4.88133	-.173531

## Experimental results

```

10 REM
20 REM This program reads the strain values obtained from the experiment conducted on the fixed ended arch,
   and calculates the stresses at the required sections.
30 REM The program also interpolates the strain values for any loading and determines the corresponding
   stresses.
40 REM
50 CLS
60 C1=30/16
70 C2=30/768
80 INPUT "Input the increment of the load ";DP
90 DIM A(6,3), B(3,3), G(3,3), EB(6), ET(6), PT(3), PB(3), CT(3), CB(3), PI(4)
100 FOR I=1 TO 6
110 A(I,1)=1
120 A(I,2)=(I-1)*DP
130 A(I,3)=A(I,2)^2
140 NEXT I
150 FOR I=1 TO 3
160 FOR J=1 TO 3
170 B(I,J)=0
180 FOR K=1 TO 6
190 B(I,J)=B(I,J)+A(K,I)*A(K,J)
200 NEXT K
210 NEXT J
220 NEXT I
230 G(1,1)=B(2,2)*B(3,3)-B(2,3)*B(3,2)
240 G(2,1)=-(B(2,1)*B(3,3)-B(2,3)*B(3,1))
250 G(3,1)=B(2,1)*B(3,2)-B(2,2)*B(3,1)
260 G(1,2)=G(2,1)
270 G(2,2)=B(1,1)*B(3,3)-B(1,3)*B(3,1)
280 G(3,2)=-(B(1,1)*B(3,2)-B(1,2)*B(3,1))
290 G(1,3)=G(3,1)
300 G(2,3)=G(3,2)
310 G(3,3)=B(1,1)*B(2,2)-B(1,2)*B(2,1)
320 D=B(1,1)*G(1,1)+B(1,2)*G(2,1)+B(1,3)*G(3,1)
330 FOR I=1 TO 3
340 FOR J=1 TO 3
350 G(I,J)=G(I,J)/D
360 NEXT J,I
370 FOR J=1 TO 3
380 FOR I=1 TO 3
390 GB(I,J)=0
400 FOR K=1 TO 3
410 GB(I,J)=GB(I,J)+B(I,K)*G(K,J)
420 NEXT K,J,I
430 REM NT = No. of tests.
440 REM NE = No. of experiments.
450 REM ET = Strains recorded by the gages on top of the arch.
460 REM EB = Strains recorded by the gages on bottom of the arch.
470 NT=10
480 REM NG = No. of pairs of gages
490 NG = 8
500 FOR BB=1 TO NG
510 LPRINT "*****"
520 IF BB=1 THEN LPRINT "* Strain gage nos. 3 and 4" : GOTO 600
530 IF BB=2 THEN LPRINT "* Strain gage nos. 7 and 8" : GOTO 600
540 IF BB=3 THEN LPRINT "* Strain gage nos. 13 and 14" : GOTO 600
550 IF BB=4 THEN LPRINT "* Strain gage nos. 17 and 18" : GOTO 600
560 IF BB=5 THEN LPRINT "* Strain gage nos. 19 and 20" : GOTO 600

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570 IF BB=6 THEN LPRINT "* Strain gage nos. 21 and 22" : GOTO 600
580 IF BB=7 THEN LPRINT "* Strain gage nos. 23 and 24" : GOTO 600
590 IF BB=8 THEN LPRINT "* Strain gage nos. 25 and 26"
600 LPRINT "*****"
610 LPRINT
620 FOR NE = 1 TO NT
630 FOR I=1 TO 6
640 READ EB(I)
650 IF NE ( 6 THEN 740
660 IF BB=1 THEN EB(I)=EB(I)-3.9 : GOTO 820
670 IF BB=2 THEN EB(I)=EB(I)-.9 : GOTO 820
680 IF BB=3 THEN EB(I)=EB(I)-.9 : GOTO 820
690 IF BB=4 THEN EB(I)=EB(I)-2.9 : GOTO 820
700 IF BB=5 THEN EB(I)=EB(I)-.9 : GOTO 820
710 IF BB=6 THEN EB(I)=EB(I)-3.9 : GOTO 820
720 IF BB=7 THEN EB(I)=EB(I)-1.9 : GOTO 820
730 IF BB=8 THEN EB(I)=EB(I)-3.9 : GOTO 820
740 IF BB=1 THEN EB(I)=EB(I)-4.8 : GOTO 820
750 IF BB=2 THEN EB(I)=EB(I)-3.9 : GOTO 820
760 IF BB=3 THEN EB(I)=EB(I)-1.9 : GOTO 820
770 IF BB=4 THEN EB(I)=EB(I) : GOTO 820
780 IF BB=5 THEN EB(I)=EB(I)-1.9 : GOTO 820
790 IF BB=6 THEN EB(I)=EB(I)-.9 : GOTO 820
800 IF BB=7 THEN EB(I)=EB(I)-1.9 : GOTO 820
810 IF BB=8 THEN EB(I)=EB(I)-5.8 : GOTO 820
820 NEXT I
830 FOR I=1 TO 6
840 READ ET(I)
850 IF NE ( 6 THEN 940
860 IF BB=1 THEN ET(I)=ET(I)-2.9 : GOTO 1020
870 IF BB=2 THEN ET(I)=ET(I)-.9 : GOTO 1020
880 IF BB=3 THEN ET(I)=ET(I)-1.9 : GOTO 1020
890 IF BB=4 THEN ET(I)=ET(I)-3.9 : GOTO 1020
900 IF BB=5 THEN ET(I)=ET(I)-3.9 : GOTO 1020
910 IF BB=6 THEN ET(I)=ET(I)-.9 : GOTO 1020
920 IF BB=7 THEN ET(I)=ET(I)-1.9 : GOTO 1020
930 IF BB=8 THEN ET(I)=ET(I) : GOTO 1020
940 IF BB=1 THEN ET(I)=ET(I)-3.9 : GOTO 1020
950 IF BB=2 THEN ET(I)=ET(I)+9.7 : GOTO 1020
960 IF BB=3 THEN ET(I)=ET(I)-1.9 : GOTO 1020
970 IF BB=4 THEN ET(I)=ET(I)-4.8 : GOTO 1020
980 IF BB=5 THEN ET(I)=ET(I)-.9 : GOTO 1020
990 IF BB=6 THEN ET(I)=ET(I)-1.9 : GOTO 1020
1000 IF BB=7 THEN ET(I)=ET(I)-1.9 : GOTO 1020
1010 IF BB=8 THEN ET(I)=ET(I)-.9 : GOTO 1020
1020 NEXT I
1030 FOR I=1 TO 3
1040 PT(I)=0 : PB(I)=0
1050 FOR K=1 TO 6
1060 PT(I)=PT(I)+A(K,I)*ET(K)
1070 PB(I)=PB(I)+A(K,I)*EB(K)
1080 NEXT K,I
1090 FOR I=1 TO 3
1100 CT(I)=0
1110 CB(I)=0
1120 FOR K=1 TO 3
1130 CT(I)=CT(I)+B(I,K)*PT(K)
1140 CB(I)=CB(I)+B(I,K)*PB(K)
1150 NEXT K,I
1160 PRINT

```

```

1170 LPRINT
1180 LPRINT "Loads at loading point #";NE
1190 LPRINT
1200 LPRINT "Coefficients C1, C2 and C3 for equations of curve fitting"
1210 LPRINT "-----"
1220 LPRINT " ", : LPRINT "Top gages", : LPRINT "Bot. gages"
1230 LPRINT
1240 FOR I=1 TO 3
1250 LPRINT "C";I,
1260 LPRINT CT(I),CB(I)
1270 NEXT I
1280 P1(0)=0
1290 P1(1)=1
1300 P1(2)=5
1310 P1(3)=10
1320 FOR J=0 TO 3
1330 RT(J)=(CT(3)*P1(J)+CT(2))*P1(J)+CT(1)
1340 RB(J)=(CB(3)*P1(J)+CB(2))*P1(J)+CB(1)
1350 N=C1*(RB(J)+RT(J))
1360 M=C2*(RB(J)-RT(J))
1370 IF N<1 THEN N=-N
1380 LPRINT
1390 LPRINT "W=S# and P=";P1(J);" Strain in top gage=";RT(J)
1400 LPRINT "          Strain in bottom gage=";RB(J)
1410 LPRINT "          Moment M=";M : LPRINT "          Thrust N=";N
1420 NEXT J
1430 FOR J=1 TO 3
1440 RT(J)=RT(J)-RT(0)
1450 RB(J)=RB(J)-RB(0) : N=C1*(RB(J)+RT(J))/P1(J) : M=C2*(RB(J)-RT(J))/P1(J)
1460 IF N<1 THEN N=-N
1470 LPRINT "W=0 and P=";P1(J) : LPRINT "          Normalized Moment =" ;M : LPRINT "          Normalized Thrust
      =" ;N
1480 NEXT J
1490 LPRINT CHR$(12)
1500 LPRINT : LPRINT : PRINT
1510 NEXT NE
1520 NEXT BB
1530 PRINT
1540 END

```

```

1550 REM *****
1560 REM          DATA STATEMENTS
1570 REM *****
1580 DATA 94.7,84.75,2,65.4,47.8,43.9 : REM Data for gage #3 at loading point 1- WSP0; WSP2, WSP4, WSP6, WSP8,
WSP10. All data given below are in the same order.
1590 DATA -92.8,-83,-69.3,-63.5,-43.9,-41 : REM Data for gage #4 at 1.
1600 DATA 91.8,35.1,-25.4,-15.6,-71.3,-101.6 : REM Data for #3 at 2.
1610 DATA -91.8,-34.2,28.3,13.6,78.3,100.6 : REM Data for #4 at 2.
1620 DATA 45.9,40,11.7,4.8,-16.6,-52.7 : REM Data for #3 at 3.
1630 DATA -43.9,-43.9,-14.6,-9.7,9.7,43.9 : REM Data for #4 at 3.
1640 DATA 23.4,27.3,33.2,35.1,39,42.9 : REM Data for #3 at 4.
1650 DATA -28.3,-30.2,-40,-43.9,-50.8,-57.6 : REM Data for #4 at 4.
1660 DATA 22.4,27.3,57.6,58.6,88.9,92.8 : REM Data for #3 at 5.
1670 DATA -22.4,-35.1,-72.3,-72.3,-102.6,-109.4 : REM Data for #4 at 5.
1680 DATA 53.7,70.3,97.7,130.9,164.1,198.3 : REM Data for #3 at 6.
1690 DATA -69.3,-85,-109.4,-142.6,-175.8,-212 : REM Data for #4 at 6.
1700 DATA 82.88.9,109.4,144.6,168,175.8 : REM Data for #3 at 7.
1710 DATA -85.9,-93.8,-113.3,-152.4,-175.8,-186.6 : REM Data for #4 at 7.
1720 DATA 74.2,75.2,91.8,107.4,145.6,183.7 : REM Data for #3 at 8.
1730 DATA -76.2,-78.1,-94.7,-107.4,-148.5,-187.6 : REM Data for #4 at 8.
1740 DATA 85,85.9,88.9,106.5,116.2,119.2 : REM Data for #3 at 9.
1750 DATA -80.1,-82,-84,-105.5,-113.3,-115.3 : REM Data for #4 at 9.
1760 DATA 65.4,73.2,66.4,70.3,71.3,66.4 : REM Data for #3 at 10.
1770 DATA -60.5,-68.4,-68.5,-64.4,-64.4,-61.5 : REM Data for #4 at 10.

```

```

1780 REM *****
1790 REM      Data for channels 7 and 8
1800 REM *****
1810 DATA -88.9,-98.8,-77.1,-85,-79.1,-76.1 : REM Data for #7 at 1.
1820 DATA -837.4,-654,-868.7,-652.1,-921.5,-932.2 : REM Data for #8 at 1.
1830 DATA -87.9,-35.1,28.3,17.5,70.3,101.6 : REM Data for #7 at 2.
1840 DATA -788.6,-1099.3,-1279.1,-1451.1,-1145.2,-1104.2 : REM Data for #8 at 2.
1850 DATA -37.1,-28.3,-4.0,3.9,22.4,57.6 : REM Data for #7 at 3.
1860 DATA -1340.7,-1386.6,-1422.8,-1457.9,-1529.3,-1418.8 : REM Data for #8 at 3.
1870 DATA -34.2,-43.9,-67.4,-83,-105.5,-126 : REM Data for #7 at 4.
1880 DATA -1479.4,-1468.7,-1514.6,-1540,-1538.1,-1471.6 : REM Data for #8 at 4.
1890 DATA -38.1,-50.8,-97.7,-103.5,-148.5,-163.1 : REM Data for #7 at 5.
1900 DATA -1668,-1671,-1635.8,-1635.8,-1589.9,-1425.7 : REM Data for #8 at 5.
1910 DATA -53.7,-76.2,-84,-116.2,-148.5,-184.6 : REM Data for #7 at 6.
1920 DATA -11.7,5.8,12.7,-4.8,-15.6,108.4 : REM Data for #8 at 6.
1930 DATA -66.4,-72.3,-83,-102.6,-111.4,-112.3 : REM Data for #7 at 7.
1940 DATA -117.2,-116.2,-107.4,-97.7,-104.5,-117.2 : REM Data for #8 at 7.
1950 DATA -60.5,-50.8,-59.6,-59.6,-78.1,-96.7 : REM Data for #7 at 8.
1960 DATA -169,-153.4,-141.6,-149.5,-150.4,-139.7 : REM Data for #8 at 8.
1970 DATA -58.8,-53.7,-49.8,-60.5,-59.6,-55.7 : REM Data for #7 at 9.
1980 DATA -182.7,-190.5,-197.3,-185.6,-157.3,-160.2 : REM Data for #8 at 9.
1990 DATA -37.1,-42.9,-37.1,-38.1,-38.1,-33.2 : REM Data for #7 at 10.
2000 DATA -202.2,-194.4,-204.2,-209.1,-204.2,-214.9 : REM Data for #8 at 10.

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2010 REM *****
2020 REM   Data for channels 13 and 14
2030 REM *****
2040 DATA -16.6,-17.5,-19.5,-16.6,-16.5,-20.5 : REM Data for #13 at 1.
2050 DATA 23.4,25.4,30.2,26.3,28.3,28.3 : REM Data for #14 at 1.
2060 DATA -14.6,-24.4,-51.7,-44.9,-59.6,-67.4 : REM Data for #13 at 2.
2070 DATA 22.4,33.2,58.6,50.8,63.5,69.3 : REM Data for #14 at 2.
2080 DATA -30.2,-50.8,-68.4,-78.1,-90.8,-117.2 : REM Data for #13 at 3.
2090 DATA 39,57.6,72.3,79.1,86.9,111.4 : REM Data for #14 at 3.
2100 DATA -40,-58.6,-68.4,-78.1,-85.9,-95.7 : REM Data for #13 at 4.
2110 DATA 42,58.6,67.4,74.2,82,86.9 : REM Data for #14 at 4.
2120 DATA -36.1,-36.1,34.2,42.9,96.7,131.9 : REM Data for #13 at 5.
2130 DATA 42,32.2,-35.1,-47.8,-93.8,-128.9 : REM Data for #14 at 5.
2140 DATA -36.1,-9.7,9.7,49.8,93.8,123.1 : REM Data for #13 at 6.
2150 DATA 23.4,-4.8,-22.4,-55.7,-99.6,-127 : REM Data for #14 at 6.
2160 DATA -22.4,-31.2,-39,-36.1,-57.6,-77.1 : REM Data for #13 at 7.
2170 DATA 26.3,33.2,39,32.2,55.7,72.3 : REM Data for #14 at 7.
2180 DATA -3.9,-32.2,-42,-66.4,-87.9,-136.8 : REM Data for #13 at 8.
2190 DATA 4.8,36.1,46.9,72.3,92.8,137.7 : REM Data for #14 at 8.
2200 DATA -27.3,-28.3,-36.1,-39,-65.4,-77.1 : REM Data for #13 at 9.
2210 DATA 34.2,35.1,47.8,46.9,75.2,63 : REM Data for #14 at 9.
2220 DATA -21.4,-14.6,-24.4,-31.2,-27.3,-31.2 : REM Data for #13 at 10.
2230 DATA 35.1,28.3,39,44.9,40,44.9 : REM Data for #14 at 10

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```

2240 REM *****
2250 REM   Data for channels 17 and 18
2260 REM *****
2270 DATA -19.5,-21.4,-23.4,-22.4,-22.4,-25.4 : REM Data for #17 at 1.
2280 DATA 19.5,17.5,23.4,20.5,19.5,19.5 : REM Data for #18 at 1.
2290 DATA -19.5,-30.2,-51.7,-45.9,-61.5,-68.4 : REM Data for #17 at 2.
2300 DATA 16.6,24.4,47.8,41.52,7.61.5 : REM Data for #18 at 2.
2310 DATA -33.2,-52.7,-70.3,-82,-94.7,-121.1 : REM Data for #17 at 3.
2320 DATA 30.2,47.8,62.5,71.3,80.1,105.5 : REM Data for #18 at 3.
2330 DATA -47.8,-64.4,-76.2,-87.9,-101.6,-116.2 : REM Data for #17 at 4.
2340 DATA 33.2,51.7,63.5,71.3,82,91.8 : REM Data for #18 at 4.
2350 DATA -46.9,-49.8,2.9,6.8,46.9,76.2 : REM Data for #17 at 5.
2360 DATA 40.34,2,-20.5,-29.3,-67.4,-94.7 : REM Data for #18 at 5.
2370 DATA -26.3,3.9,42.9,86.9,142.6,176.8 : REM Data for #17 at 6.
2380 DATA 15.6,-15.6,-47.8,-89.9,-142.6,-177.8 : REM Data for #18 at 6.
2390 DATA -11.7,-20.5,-27.3,-10.7,-30.2,-51.7 : REM Data for #17 at 7.
2400 DATA 19.5,26.3,30.2,11.7,31.2,55.7 : REM Data for #18 at 7.
2410 DATA 2.9,-27.3,-39,-64.4,-80.1,-129.9 : REM Data for #17 at 8.
2420 DATA 3.9,34.2,44.9,71.3,87.9,131.9 : REM Data for #18 at 8.
2430 DATA -22.4,-20.5,-33.2,-33.2,-64.4,-74.2 : REM Data for #17 at 9.
2440 DATA 29.3,31.2,43.9,42.72,3,81.1 : REM Data for #18 at 9.
2450 DATA -21.4,-13.6,-24.4,-30.2,-26.3,-31.2 : REM Data for #17 at 10.
2460 DATA 31.2,24.4,37.1,42.9,39,43.9 : REM Data for #18 at 10.

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```

2470 REM *****
2480 REM Data for channels 19 and 20
2490 REM *****
2500 DATA 33,33.2,37.1,35.1,31.2,33.2 : REM Data for #19 at 1.
2510 DATA -40,-37.1,-37.1,-34.2,-34.2,-35.1 : REM Data for #20 at 1.
2520 DATA 35.1,31.2,39,28.3,32.2,30.2 : REM Data for #19 at 2.
2530 DATA -34.2,-35.1,-42,-31.2,-37.1,-36.1 : REM Data for #20 at 2.
2540 DATA 37.1,30.2,34.2,24.4,19.5,15.6 : REM Data for #19 at 3.
2550 DATA -38.1,-35.1,-39,-34.2,-29.3,-27.3 : REM Data for #20 at 3.
2560 DATA 14.6,11.7,7.8,2.9,-2.9,-6.8 : REM Data for #19 at 4.
2570 DATA -24.4,-19.5,-17.5,-13.6,-9.7,-8.7 : REM Data for #20 at 4.
2580 DATA 4.8,2.9,-22.4,-27.3,-47.8,-76.2 : REM Data for #19 at 5.
2590 DATA -7.8,-16.6,2.9,9.7,33.2,60.5 : REM Data for #20 at 5.
2600 DATA 48.8,18.5,17.5,-5.8,-36.1,-56.6 : REM Data for #19 at 6.
2610 DATA -63.5,-38.2,-29.3,-2.9,30.2,50.8 : REM Data for #20 at 6.
2620 DATA 53.7,49.8,46.9,46.9,54.7,81.1 : REM Data for #19 at 7.
2630 DATA -53.7,-47.8,-52.7,-51.7,-57.6,-85 : REM Data for #20 at 7.
2640 DATA 67.4,96.7,131.9,194.4,252.1,316.6 : REM data for #19 at 8.
2650 DATA -67.4,-94.7,-128,-188.6,-248.2,-316.6 : REM Data for #20 at 8.
2660 DATA 96.7,110.4,140.7,179.8,230.6,267.7 : REM Data for #19 at 9.
2670 DATA -85,-100.6,-132.8,-171.9,-224.7,-263.8 : REM Data for #20 at 9.
2680 DATA 80.1,80.1,86.9,96.7,87.9,99.6 : REM Data for #19 at 10.
2690 DATA -68.4,-69.3,-72.3,-85,-77.1,-85.9 : REM Data for #20 at 10.

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2700 REM *****
2710 REM   Data for channels 21 and 22
2720 REM *****
2730 DATA 31.2,29.3,33.2,28.3,26.3,27.3 : REM Data for #21 at 1.
2740 DATA -33.2,-32.2,-31.2,-29.3,-29.3,-30.2 : REM Data for #22 at 1.
2750 DATA 30.2,29.3,32.2,21.4,26.3,25.4 : REM Data for #21 at 2.
2760 DATA -30.2,-30.2,-35.1,-24.4,-30.2,-31.2 : REM Data for #22 at 2.
2770 DATA 33.2,25.4,30.2,22.4,15.6,11.7 : REM Data for #21 at 3.
2780 DATA -32.2,-27.3,-35.1,-29.3,-24.4,-22.4 : REM Data for #22 at 3.
2790 DATA 14.6,9.7,7.8,9,-3.9,-7.8 : REM Data for #21 at 4.
2800 DATA -18.5,-16.6,-13.6,-9.7,-6.8,-7.8 : REM Data for #22 at 4.
2810 DATA 3.9,9,-21.4,-27.3,-47.8,-75.2 : REM Data for #21 at 5.
2820 DATA -5.8,-10.7,7.8,11.7,36.1,61.5 : REM Data for #22 at 5.
2830 DATA 42.9,11.7,12.7,-12.6,-45.9,-65.4 : REM Data for #21 at 6.
2840 DATA -59.6,-26.3,-26.3,1.9,35.1,53.7 : REM Data for #22 at 6.
2850 DATA 43.9,39.39,34.2,36.1,60.5 : REM Data for #21 at 7.
2860 DATA -49.8,-42.9,-42.9,-40,-42,-66.4 : REM Data for #22 at 7.
2870 DATA 62.5,87.9,116.2,171,221.8,276.5 : REM Data for #21 at 8.
2880 DATA -62.5,-87.9,-116.2,-171,-222.8,-280.4 : REM Data for #22 at 8.
2890 DATA 85.9,101.6,130.7,182.7,234.5,282.4 : REM Data for #21 at 9.
2900 DATA -88.1,-98.6,-133.8,-175.8,-227.6,-277.5 : REM Data for #22 at 9.
2910 DATA 72.3,73.2,77.1,92.8,84,94.7 : REM Data for #21 at 10.
2920 DATA -63.5,-67.4,-69.3,-84,-74.2,-86.9 : REM Data for #22 at 10.

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2930 REM *****
2940 REM Data for channels 23 and 24
2950 REM *****
2960 DATA 33.2,15.6,29.3,14.6,12.7,13.6 : REM Data for #23 at 1.
2970 DATA -29.3,-27.3,-25.4,-23.4,-21.4,-25.4 : REM Data for #24 at 1.
2980 DATA 14.6,14.6,17.5,8.7,12.7,13.6 : REM Data for #23 at 2.
2990 DATA -24.4,-23.4,-29.3,-20.5,-24.4,-25.4 : REM Data for #24 at 2.
3000 DATA 17.5,8.7,18.5,5.8,8.7,-3.9 : REM Data for #23 at 3.
3010 DATA -25.4,-22.4,-30.2,-24.4,-21.4,-17.5
3020 DATA -5.8,-6.8,-9.7,-13.6,-19.5,-21.4
3030 DATA -14.6,-8.7,-9.7,-5.8,-2.9,-5.8
3040 DATA 3.9,-13.6,-31.2,-36.1,-53.7,-83
3050 DATA -1.9,-6.8,8.7,11.7,33.2,59.6
3060 DATA 38.1,6.8,8.7,-18.5,-48.8,-70.3
3070 DATA -57.6,-25.4,-24.4,3.9,37.1,53.7
3080 DATA 39,31.2,30.2,19.5,20.5,42.9
3090 DATA -45.9,-40,-38.1,-31.2,-29.3,-52.7
3100 DATA 59.6,87.9,111.4,159.2,204.2,250.1
3110 DATA -60.5,-82,-103.5,-151.4,-196.4,-243.3
3120 DATA 87.9,106.5,147.5,192.5,247.2,300.9
3130 DATA -75.2,-95.7,-134.8,-179.8,-232.5,-288.2
3140 DATA 75.2,80.1,82,97.7,90.8,102.6
3150 DATA -59.6,-60.5,-64.4,-77.1,-78.3,-82

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```

3160 REM *****
3170 REM   Data for channels 25 and 26
3180 REM *****
3190 DATA -53.7,-50.0,-48.0,-47.0,-43.9,-46.9
3200 DATA 88.9,85.88.9,85.9,84,82
3210 DATA -49.0,-44.9,-43.9,-40,-37.1,-33.2
3220 DATA 87.9,84,81.1,76.2,74.2,68.4
3230 DATA -45.9,-40,-36.1,-29.3,-17.5,-3.9
3240 DATA 85.9,75.2,74.2,63.5,50.0,35.1
3250 DATA -24.4,-22.4,-14.6,-6.0,-.9,6.0
3260 DATA 59.6,55.7,47.0,41,31.2,20.5
3270 DATA -4.0,-15.6,-.9,1.9,29.3,50.0
3280 DATA 44.9,46.9,27.3,24.4,2.9,-18.5
3290 DATA -89.9,-67.4,-83,-67.4,-51.7,-47.0
3300 DATA 142.6,120.1,138.7,127,114.3,110.4
3310 DATA -81.1,-82,-96.7,-116.2,-140.7,-171.9
3320 DATA 146.5,140.5,163.1,181.7,204.2,233.5
3330 DATA -82,-104.5,-126,-172.9,-231.5,-300.9
3340 DATA 153.4,177.0,201.3,244.3,300,365.4
3350 DATA -97.7,-117.2,-153.4,-197.3,-252.1,-304.0
3360 DATA 180.7,196.4,229.6,272.6,319.5,370.3
3370 DATA -76.2,-80.1,-77.1,-86.9,-74.2,-82
3380 DATA 160.2,162.2,159.2,168,155.3,163.1

```

\*\*\*\*\*  
 \* Strain gage nos. 3 and 4  
 \*\*\*\*\*

Loads at loading point # 1

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-97.42496	90.22856
C 2	5.945145	-5.266419
C 3	-4.866028E-02	-5.355835E-03

W=5# and P= 0 Strain in top gage=-97.42496  
 Strain in bottom gage= 90.22856  
 Moment M= 7.330216  
 Thrust N=-13.49324

W=5# and P= 1 Strain in top gage=-91.52848  
 Strain in bottom gage= 84.95679  
 Moment M= 6.893935  
 Thrust N=-12.32191

W=5# and P= 5 Strain in top gage=-68.91575  
 Strain in bottom gage= 63.76258  
 Moment M= 5.182747  
 Thrust N=-9.662189

W=5# and P= 10 Strain in top gage=-42.83354  
 Strain in bottom gage= 37.02879  
 Moment M= 3.119857  
 Thrust N=-10.89515

W=0 and P= 1  
 Normalized Moment =-.4362601  
 Normalized Thrust =-1.171331

W=0 and P= 5  
 Normalized Moment =-.4294938  
 Normalized Thrust = .7662106

W=0 and P= 10  
 Normalized Moment =-.4210359  
 Normalized Thrust = .2598095

Loads at loading point # 2

Coefficients C1, C2 and C3 for equations of curve fitting

---

	Top gages	Bot. gages
C 1	-88.9964	81.01428
C 2	25.1409	-25.17716
C 3	-.712946	.692854

---

W=5# and P= 0 Strain in top gage=-88.9964  
 Strain in bottom gage= 81.01428  
 Moment M= 6.641042  
 Thrust N=-14.96647

W=5# and P= 1 Strain in top gage=-64.56845  
 Strain in bottom gage= 56.52992  
 Moment M= 4.730407  
 Thrust N=-15.07211

W=5# and P= 5 Strain in top gage= 18.68445  
 Strain in bottom gage=-27.55014  
 Moment M=-1.813851  
 Thrust N=-16.24817

W=5# and P= 10 Strain in top gage= 91.11801  
 Strain in bottom gage=-101.4719  
 Moment M=-7.523042  
 Thrust N=-19.41347

W=0 and P= 1  
 Normalized Moment =-1.910635  
 Normalized Thrust =-.1056433

W=0 and P= 5  
 Normalized Moment =-1.690979  
 Normalized Thrust =-.2563391

W=0 and P= 10  
 Normalized Moment =-1.416408  
 Normalized Thrust =-.4447003



## Loads at loading point # 3

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-49.02143	42.02857
C 2	2.772499	-4.35286
C 3	.5866075	-.5285721
W=5# and P= 0	Strain in top gages=-49.02143 Strain in bottom gage= 42.02857 Moment M= 3.556641 Thrust N=-13.11163	
W=5# and P= 1	Strain in top gages=-45.66233 Strain in bottom gage= 37.14713 Moment M= 3.234744 Thrust N=-15.96598	
W=5# and P= 5	Strain in top gages=-20.49375 Strain in bottom gage= 7.049965 Moment M= 1.075926 Thrust N=-25.2071	
W=5# and P= 10	Strain in top gage= 37.3643 Strain in bottom gage=-54.35724 Moment M=-3.582873 Thrust N=-31.86175	
W=0 and P= 1	Normalized Moment =-.3218961 Normalized Thrust =-2.854357	
W=0 and P= 5	Normalized Moment =-.4961428 Normalized Thrust =-2.419094	
W=0 and P= 10	Normalized Moment =-.7139514 Normalized Thrust =-1.875013	

## Loads at loading point # 4

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	-31.31872	18.60001
C 2	-2.455551	2.27858
C 3	-5.758558E-02	-.0357132

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W=5# and P= 0 Strain in top gages=-31.31872  
 Strain in bottom gage= 18.60001  
 Moment M= 1.949633  
 Thrust N=-23.83258

W=5# and P= 1 Strain in top gages=-33.82385  
 Strain in bottom gage= 20.84287  
 Moment M= 2.135419  
 Thrust N=-24.33934

W=5# and P= 5 Strain in top gages=-45.02819  
 Strain in bottom gage= 29.10008  
 Moment M= 2.895635  
 Thrust N=-29.86521

W=5# and P= 10 Strain in top gage=-61.62589  
 Strain in bottom gage= 37.81448  
 Moment M= 3.884358  
 Thrust N=-44.64488

W=0 and P= 1  
 Normalized Moment = .1857814  
 Normalized Thrust =-.5067587

W=0 and P= 5  
 Normalized Moment = .1891935  
 Normalized Thrust =-1.206525

W=0 and P= 10  
 Normalized Moment = .1934721  
 Normalized Thrust =-2.08123

## Loads at loading point # 5

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-23.98212	14.42139
C 2	-11.32767	7.906898
C 3	.2191925	-2.231789E-02

W=50 and P= 0 Strain in top gages=-23.98212  
 Strain in bottom gage= 14.42139  
 Moment M= 1.500137  
 Thrust N=-17.92637

W=50 and P= 1 Strain in top gages=-25.09059  
 Strain in bottom gage= 22.30517  
 Moment M= 2.242022  
 Thrust N=-23.97267

W=50 and P= 5 Strain in top gages=-75.14064  
 Strain in bottom gage= 53.39393  
 Moment M= 5.020882  
 Thrust N=-40.77509

W=50 and P= 10 Strain in top gage=-115.3395  
 Strain in bottom gage= 91.25058  
 Moment M= 8.069926  
 Thrust N=-45.16682

W=0 and P= 1  
 Normalized Moment = .741885  
 Normalized Thrust =-6.045304

W=0 and P= 5  
 Normalized Moment = .704149  
 Normalized Thrust =-4.569743

W=0 and P= 10  
 Normalized Moment = .656979  
 Normalized Thrust =-2.724044

Loads at loading point # 6

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-70.65356	47.77136
C 2	-8.411255	9.858581
C 3	-.6147308	.4964257

W=5# and P= 0 Strain in top gage=-70.65356  
 Strain in bottom gage= 47.77136  
 Moment M= 4.625974  
 Thrust N=-42.90413

W=5# and P= 1 Strain in top gage=-79.67955  
 Strain in bottom gage= 58.12637  
 Moment M= 5.383044  
 Thrust N=-40.41221

W=5# and P= 5 Strain in top gage=-128.0781  
 Strain in bottom gage= 109.4749  
 Moment M= 9.279415  
 Thrust N=-34.88099

W=5# and P= 10 Strain in top gage=-216.2392  
 Strain in bottom gage= 195.9997  
 Moment M= 16.10309  
 Thrust N=-37.94898

W=0 and P= 1  
 Normalized Moment = .7570701  
 Normalized Thrust =-2.491915

W=0 and P= 5  
 Normalized Moment = .9306882  
 Normalized Thrust =-1.604628

W=0 and P= 10  
 Normalized Moment = 1.147711  
 Normalized Thrust = .4955149

Loads at loading point # 7

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-82.9964	72.21076
C 2	-9.921936	9.874004
C 3	-.1343842	7.188416E-02
W=5# and P= 0	Strain in top gage=-82.9964 Strain in bottom gage= 72.21076 Moment M= 6.06278 Thrust N=-20.22306	
W=5# and P= 1	Strain in top gage=-93.05272 Strain in bottom gage= 82.15673 Moment M= 6.844119 Thrust N=-20.42999	
W=5# and P= 5	Strain in top gage=-135.9657 Strain in bottom gage= 123.3783 Moment M= 10.13062 Thrust N=-23.60138	
W=5# and P= 10	Strain in top gage=-195.6542 Strain in bottom gage= 178.14 Moment M= 14.60134 Thrust N=-32.83905	
W=0 and P= 1	Normalized Moment = .7813395 Normalized Thrust =-.2069092	
W=0 and P= 5	Normalized Moment = .8135689 Normalized Thrust =-.6756592	
W=0 and P= 10	Normalized Moment = .8538556 Normalized Thrust =-1.251597	

Loads at loading point # 8

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-79.443	69.9607
C 2	1.522888	-1.076965
C 3	-1.267868	1.213841

W=5# and P= 0 Strain in top gage=-79.443  
Strain in bottom gage= 69.9607  
Moment M= 5.636082  
Thrust N=-17.77931

W=5# and P= 1 Strain in top gage=-79.18798  
Strain in bottom gage= 78.09756  
Moment M= 5.631466  
Thrust N=-17.04452

W=5# and P= 5 Strain in top gage=-103.5253  
Strain in bottom gage= 94.92188  
Moment M= 7.751841  
Thrust N=-16.12133

W=5# and P= 10 Strain in top gage=-191.0009  
Strain in bottom gage= 180.5751  
Moment M= 14.51469  
Thrust N=-19.54843

W=0 and P= 1  
Normalized Moment =-4.615188E-03  
Normalized Thrust = .7347965

W=0 and P= 5  
Normalized Moment = .3831519  
Normalized Thrust = .3295956

W=0 and P= 10  
Normalized Moment = .8678606  
Normalized Thrust =-.1769114

## Loads at loading point # 9

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-88.19645	78.63925
C 2	-3.184859	2.327698
C 3	-.1858844	.1665154
W=5# and P= 0	Strain in top gage=-88.19645	
	Strain in bottom gage= 78.63925	
	Moment M= 6.28452	
	Thrust N=-2.919731	
W=5# and P= 1	Strain in top gage=-83.48711	
	Strain in bottom gage= 81.13347	
	Moment M= 6.427367	
	Thrust N=-4.263867	
W=5# and P= 5	Strain in top gage=-98.36584	
	Strain in bottom gage= 94.44862	
	Moment M= 7.531583	
	Thrust N=-7.359782	
W=5# and P= 10	Strain in top gage=-121.8255	
	Strain in bottom gage= 118.5678	
	Moment M= 9.398361	
	Thrust N=-6.188198	
W=0 and P= 1	Normalized Moment = .2228469	
	Normalized Thrust =-1.343336	
W=0 and P= 5	Normalized Moment = .2653967	
	Normalized Thrust =-.888801	
W=0 and P= 10	Normalized Moment = .3185842	
	Normalized Thrust =-.3188467	

Loads at loading point # 10

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-65.07145	62.78214
C 2	-.955719	1.487686
C 3	9.999846E-02	-.1441937

W=5# and P= 0    Strain in top gage=-65.07145  
                               Strain in bottom gage= 62.78214  
                   Moment M= 4.994281  
                   Thrust N=-4.29245

W=5# and P= 1    Strain in top gage=-65.92716  
                               Strain in bottom gage= 64.12563  
                   Moment M= 5.000188  
                   Thrust N=-3.377881

W=5# and P= 5    Strain in top gage=-67.35008  
                               Strain in bottom gage= 66.61573  
                   Moment M= 5.233039  
                   Thrust N=-1.37691

W=5# and P= 10    Strain in top gage=-64.62578  
                               Strain in bottom gage= 63.23963  
                   Moment M= 4.99486  
                   Thrust N=-2.604661

W=0 and P= 1  
                   Normalized Moment = 8.590659E-02  
                   Normalized Thrust = .9145689

W=0 and P= 5  
                   Normalized Moment = 4.775173E-02  
                   Normalized Thrust = .583108

W=0 and P= 10  
                   Normalized Moment = 5.796552E-05  
                   Normalized Thrust = .1687789



\*\*\*\*\*  
 \* Strain gage nos. 7 and 8  
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Loads at loading point # 1

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-826.3672	-93.86869
C 2	-8.698918	1.965518
C 3	-.1308269	-7.455635E-02

W=5# and P= 0    Strain in top gage=-826.3672  
                     Strain in bottom gage=-93.86869  
                     Moment M= 28.61353  
                     Thrust N=-1725.427

W=5# and P= 1    Strain in top gage=-835.189  
                     Strain in bottom gage=-92.82972  
                     Moment M= 29.82966  
                     Thrust N=-1738.535

W=5# and P= 5    Strain in top gage=-873.8925  
                     Strain in bottom gage=-86.19781  
                     Moment M= 38.73811  
                     Thrust N=-1798.668

W=5# and P= 10   Strain in top gage=-926.3592  
                     Strain in bottom gage=-82.26115  
                     Moment M= 32.97258  
                     Thrust N=-1891.163

W=0 and P= 1    Normalized Moment = .4161227  
                     Normalized Thrust =-13.18778

W=0 and P= 5    Normalized Moment = .4249143  
                     Normalized Thrust =-14.64812

W=0 and P= 10   Normalized Moment = .4359847  
                     Normalized Thrust =-16.5736

## Loads at loading point # 2

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-779.7315	-86.53216
C 2	-192.2041	24.59055
C 3	16.52365	-.6691952
W=5# and P= 0	Strain in top gage=-779.7315 Strain in bottom gage=-86.53216 Moment M= 27.8781 Thrust N=-1624.244	
W=5# and P= 1	Strain in top gage=-955.4119 Strain in bottom gage=-62.61082 Moment M= 34.87504 Thrust N=-1908.753	
W=5# and P= 5	Strain in top gage=-1327.661 Strain in bottom gage= 19.69068 Moment M= 52.63092 Thrust N=-2452.444	
W=5# and P= 10	Strain in top gage=-1049.407 Strain in bottom gage= 92.45377 Moment M= 44.60395 Thrust N=-1794.280	
W=0 and P= 1	Normalized Moment = 7.796945 Normalized Thrust =-284.5483	
W=0 and P= 5	Normalized Moment = 5.118563 Normalized Thrust =-165.6399	
W=0 and P= 10	Normalized Moment = 1.752585 Normalized Thrust =-17.00437	

## Loads at loading point # 3

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-1317.172	-40.25714
C 2	-48.82831	4.06144
C 3	2.862427	.5
W=5# and P= 0 Strain in top gage=-1317.172		
Strain in bottom gage=-40.25714		
Moment M= 43.87949		
Thrust N=-2545.179		
W=5# and P= 1 Strain in top gage=-1355.13		
Strain in bottom gage=-35.6957		
Moment M= 51.5404		
Thrust N=-2607.798		
W=5# and P= 5 Strain in top gage=-1449.713		
Strain in bottom gage=-7.449944		
Moment M= 56.33839		
Thrust N=-2732.18		
W=5# and P= 10 Strain in top gage=-1439.132		
Strain in bottom gage= 50.35726		
Moment M= 58.18319		
Thrust N=-2683.953		
W=0 and P= 1		
Normalized Moment = 1.660911		
Normalized Thrust =-62.61834		
W=0 and P= 5		
Normalized Moment = 1.291782		
Normalized Thrust =-37.40014		
W=0 and P= 10		
Normalized Moment = .8383786		
Normalized Thrust =-5.877385		

Loads at loading point # 4

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-1450.478	-36.44284
C 2	-23.771	-7.187927
C 3	2.89906	-.223217
W=5# and P= 0	Strain in top gage=-1450.478 Strain in bottom gage=-36.44284 Moment M= 55.23575 Thrust N=-2787.977	
W=5# and P= 1	Strain in top gage=-1472.15 Strain in bottom gage=-43.85399 Moment M= 55.79281 Thrust N=-2842.507	
W=5# and P= 5	Strain in top gage=-1516.857 Strain in bottom gage=-77.96291 Moment M= 56.28678 Thrust N=-2990.286	
W=5# and P= 10	Strain in top gage=-1478.282 Strain in bottom gage=-130.6438 Moment M= 52.64212 Thrust N=-3016.736	
W=0 and P= 1	Normalized Moment = .5578598 Normalized Thrust =-54.53867	
W=0 and P= 5	Normalized Moment = .1942859 Normalized Thrust =-48.46193	
W=0 and P= 10	Normalized Moment =-.2593634 Normalized Thrust =-22.87593	

## Loads at loading point # 5

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-1646.27	-38.30353
C 2	-18.4502	-13.11371
C 3	3.923279	-8.487701E-03
W=5# and P= 0	Strain in top gage=-1646.27 Strain in bottom gage=-38.30353 Moment M= 62.8112 Thrust N=-3158.575	
W=5# and P= 1	Strain in top gage=-1660.797 Strain in bottom gage=-51.42573 Moment M= 62.86606 Thrust N=-3210.418	
W=5# and P= 5	Strain in top gage=-1640.439 Strain in bottom gage=-104.0643 Moment M= 60.01306 Thrust N=-3270.961	
W=5# and P= 10	Strain in top gage=-1438.444 Strain in bottom gage=-170.2894 Moment M= 49.53729 Thrust N=-3016.375	
W=0 and P= 1	Normalized Moment = 5.486951E-02 Normalized Thrust =-51.84197	
W=0 and P= 5	Normalized Moment =-.5594671 Normalized Thrust =-22.48113	
W=0 and P= 10	Normalized Moment =-1.32739 Normalized Thrust =-14.22001	

Loads at loading point # 6

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	5.325012	-56.77161
C 2	-13.2002	-5.497803
C 3	2.061162	-.7410051

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W=5# and P= 0 Strain in top gage= 5.325012  
 Strain in bottom gage=-56.77161  
 Moment M=-2.425649  
 Thrust N=-56.46236

W=5# and P= 1 Strain in top gage=-5.814021  
 Strain in bottom gage=-63.0105  
 Moment M=-2.234237  
 Thrust N=-129.046

W=5# and P= 5 Strain in top gage=-9.146914  
 Strain in bottom gage=-102.7878  
 Moment M=-3.657845  
 Thrust N=-209.8775

W=5# and P= 10 Strain in top gage= 79.43926  
 Strain in bottom gage=-185.8581  
 Moment M=-10.36318  
 Thrust N=-199.5354

W=0 and P= 1  
 Normalized Moment = .1914119  
 Normalized Thrust =-32.5836

W=0 and P= 5  
 Normalized Moment =-.2464392  
 Normalized Thrust =-22.66303

W=0 and P= 10  
 Normalized Moment =-.793753  
 Normalized Thrust =-10.3073

## Loads at loading point # 7

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-121.925	-64.12146
C 2	6.483734	-6.689636
C 3	-.5843811	.1455387
W=5# and P= 0	Strain in top gages=-121.925 Strain in bottom gages=-64.12146 Moment M= 2.25795 Thrust N=-348.8371	
W=5# and P= 1	Strain in top gages=-116.8256 Strain in bottom gages=-70.66556 Moment M= 1.771878 Thrust N=-350.046	
W=5# and P= 5	Strain in top gages=-104.1158 Strain in bottom gages=-93.93138 Moment M= .3978389 Thrust N=-371.3385	
W=5# and P= 10	Strain in top gages=-115.5258 Strain in bottom gages=-116.4648 Moment M=-3.667951E-02 Thrust N=-434.9822	
W=0 and P= 1	Normalized Moment =-.4868726 Normalized Thrust =-1.208911	
W=0 and P= 5	Normalized Moment =-.3728239 Normalized Thrust =-4.580289	
W=0 and P= 10	Normalized Moment =-.229463 Normalized Thrust =-8.614511	

Loads at loading point # 8

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-166.5249	-68.48363
C 2	5.478893	4.293427
C 3	-.3361626	-.8849164
W=5% and P= 0	Strain in top gage=-166.5249 Strain in bottom gage=-68.48363 Moment M= 4.145363 Thrust N=-425.491	
W=5% and P= 1	Strain in top gage=-161.391 Strain in bottom gage=-56.91512 Moment M= 4.881888 Thrust N=-409.3239	
W=5% and P= 5	Strain in top gage=-147.5785 Strain in bottom gage=-59.8594 Moment M= 3.457778 Thrust N=-387.4461	
W=5% and P= 10	Strain in top gage=-145.4482 Strain in bottom gage=-97.951 Moment M= 1.854658 Thrust N=-456.3773	
W=0 and P= 1	Normalized Moment =-6.427408E-02 Normalized Thrust =-16.16787	
W=0 and P= 5	Normalized Moment =-.137517 Normalized Thrust =-7.688982	
W=0 and P= 10	Normalized Moment =-.2298785 Normalized Thrust =-3.888632	



## Loads at loading point # 9

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-186.0035	-50.82855
C 2	-4.164551	-1.737854
C 3	.7361603	9.821319E-02
W=5# and P= 0	Strain in top gage=-186.0035 Strain in bottom gage=-50.82855 Moment M= 5.280271 Thrust N=-444.0601	
W=5# and P= 1	Strain in top gage=-189.4319 Strain in bottom gage=-52.4682 Moment M= 5.350144 Thrust N=-453.5626	
W=5# and P= 5	Strain in top gage=-188.4222 Strain in bottom gage=-57.06249 Moment M= 5.13124 Thrust N=-460.2839	
W=5# and P= 10	Strain in top gage=-154.033 Strain in bottom gage=-58.38578 Moment M= 3.736218 Thrust N=-398.2851	
W=0 and P= 1	Normalized Moment = 6.987304E-02 Normalized Thrust =-9.502559	
W=0 and P= 5	Normalized Moment =-.0298062 Normalized Thrust =-3.244758	
W=0 and P= 10	Normalized Moment =-.1544052 Normalized Thrust =-4.577494	

Loads at loading point # 10

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-200.7534	-39.19646
C 2	.1072998	-.8826732
C 3	-.150444	.1352644
W=5# and P= 0	Strain in top gage=-200.7534 Strain in bottom gage=-39.19646 Moment M= 6.310817 Thrust N=-449.9059	
W=5# and P= 1	Strain in top gage=-200.7965 Strain in bottom gage=-39.94387 Moment M= 6.283307 Thrust N=-451.3882	
W=5# and P= 5	Strain in top gage=-203.978 Strain in bottom gage=-40.22822 Moment M= 6.396475 Thrust N=-457.8866	
W=5# and P= 10	Strain in top gage=-214.7248 Strain in bottom gage=-34.49677 Moment M= 7.040157 Thrust N=-467.2904	
W=0 and P= 1	Normalized Moment =-2.751008E-02 Normalized Thrust =-1.482303	
W=0 and P= 5	Normalized Moment = .0171316 Normalized Thrust =-1.59614	
W=0 and P= 10	Normalized Moment = 7.293396E-02 Normalized Thrust =-1.738447	

\*\*\*\*\*  
 \* Strain gage nos. 13 and 14  
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Loads at loading point # 1

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	21.72856	-19.00359
C 2	1.365006	-5.230713E-02
C 3	-9.464264E-02	-2.276802E-02

W=5# and P= 0 Strain in top gage= 21.72856  
 Strain in bottom gage=-19.00359  
 Moment M=-1.5911  
 Thrust N=-5.109329

W=5# and P= 1 Strain in top gage= 22.99893  
 Strain in bottom gage=-19.07866  
 Moment M=-1.643656  
 Thrust N=-7.350494

W=5# and P= 5 Strain in top gage= 26.18752  
 Strain in bottom gage=-19.83432  
 Moment M=-1.797728  
 Thrust N=-11.91225

W=5# and P= 10 Strain in top gage= 25.91435  
 Strain in bottom gage=-21.80346  
 Moment M=-1.863977  
 Thrust N=-7.707925

W=0 and P= 1  
 Normalized Moment =-5.255617E-02  
 Normalized Thrust =-2.241165

W=0 and P= 5  
 Normalized Moment =-4.132576E-02  
 Normalized Thrust =-1.360585

W=0 and P= 10  
 Normalized Moment =-2.728775E-02  
 Normalized Thrust = .2598596

Loads at loading point # 2

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	28.53571	-16.15717
C 2	7.921882	-7.879273
C 3	-.3383923	.2696419

W=5# and P= 0 Strain in top gage= 28.53571  
Strain in bottom gage=-16.15717  
Moment M=-1.433315  
Thrust N=-8.289763

W=5# and P= 1 Strain in top gages 28.1184  
Strain in bottom gage=-23.7668  
Moment M=-2.026765  
Thrust N=-8.159248

W=5# and P= 5 Strain in top gages 51.68131  
Strain in bottom gage=-48.81248  
Moment M=-3.925539  
Thrust N=-5.379845

W=5# and P= 10 Strain in top gage= 65.9873  
Strain in bottom gage=-67.9857  
Moment M=-5.238196  
Thrust N=-3.897814

W=0 and P= 1  
Normalized Moment =-.59345  
Normalized Thrust =-5.051494E-02

W=0 and P= 5  
Normalized Moment =-.4984447  
Normalized Thrust =-.5661435

W=0 and P= 18  
Normalized Moment =-.379688  
Normalized Thrust =-1.210678

## Loads at loading point # 3

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	39.97504	-34.70722
C 2	6.439453	-7.647492
C 3	8.487701E-03	-4.197312E-02
W=5# and P= 0	Strain in top gage= 39.97504 Strain in bottom gage=-34.70722 Moment M=-2.917276 Thrust N=-9.877167	
W=5# and P= 1	Strain in top gage= 46.42298 Strain in bottom gage=-42.39668 Moment M=-3.469518 Thrust N=-7.54931	
W=5# and P= 5	Strain in top gage= 72.3845 Strain in bottom gage=-73.99401 Moment M=-5.71791 Thrust N=-3.017836	
W=5# and P= 10	Strain in top gage= 105.2183 Strain in bottom gage=-115.3794 Moment M=-8.617101 Thrust N=-19.05207	
W=0 and P= 1	Normalized Moment =-.5522424 Normalized Thrust =-2.327857	
W=0 and P= 5	Normalized Moment =-.5601269 Normalized Thrust =-2.579001	
W=0 and P= 10	Normalized Moment =-.5699825 Normalized Thrust =-2.892923	

Loads at loading point # 4

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	41.36069	-43.48569
C 2	7.097351	-7.608612
C 3	-.2790165	.2321434
W=5# and P= 0	Strain in top gage= 41.36069 Strain in bottom gage=-43.48569 Moment M=-3.314312 Thrust N=-3.984375	
W=5# and P= 1	Strain in top gage= 48.17903 Strain in bottom gage=-52.86216 Moment M=-3.868796 Thrust N=-5.030073	
W=5# and P= 5	Strain in top gage= 69.87203 Strain in bottom gage=-75.72516 Moment M=-5.687391 Thrust N=-10.97461	
W=5# and P= 10	Strain in top gage= 84.43255 Strain in bottom gage=-96.35747 Moment M=-7.06211 Thrust N=-22.35922	
W=0 and P= 1	Normalized Moment =-.5544846 Normalized Thrust =-1.046496	
W=0 and P= 5	Normalized Moment =-.4746158 Normalized Thrust =-1.398048	
W=0 and P= 10	Normalized Moment =-.3747739 Normalized Thrust =-1.637465	

## Loads at loading point # 5

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	46.01779	-45.51432
C 2	-15.94482	12.90503
C 3	-.1643796	.4910690

W=5# and P= 0 Strain in top gage= 46.01779  
 Strain in bottom gage=-45.51432  
 Moment M=-3.575473  
 Thrust N= .9440231

W=5# and P= 1 Strain in top gage= 29.68859  
 Strain in bottom gage=-32.11821  
 Moment M=-2.422141  
 Thrust N=-4.180548

W=5# and P= 5 Strain in top gage=-38.31582  
 Strain in bottom gage= 31.28756  
 Moment M= 2.718883  
 Thrust N=-13.17794

W=5# and P= 10 Strain in top gage=-131.8684  
 Strain in bottom gage= 132.643  
 Moment M= 10.33248  
 Thrust N=-1.452284

W=0 and P= 1  
 Normalized Moment = 1.153332  
 Normalized Thrust =-5.124572

W=0 and P= 5  
 Normalized Moment = 1.258871  
 Normalized Thrust =-2.824393

W=0 and P= 10  
 Normalized Moment = 1.390795  
 Normalized Thrust = 5.082608E-02





Loads at loading point # 7

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	27.55356	-26.26068
C 2	-1.173019	-.1623363
C 3	.532589	-.4834824
W=5# and P= 0	Strain in top gage= 27.55356 Strain in bottom gage=-26.26068 Moment M=-2.102119 Thrust N=-2.424145	
W=5# and P= 1	Strain in top gage= 26.91313 Strain in bottom gage=-26.9065 Moment M=-2.102329 Thrust N= 1.242399E-02	
W=5# and P= 5	Strain in top gage= 35.00319 Strain in bottom gage=-39.15943 Moment M=-2.896977 Thrust N=-7.792962	
W=5# and P= 10	Strain in top gage= 69.00226 Strain in bottom gage=-76.2323 Moment M=-5.67635 Thrust N=-13.40633	
W=0 and P= 1	Normalized Moment =-2.105534E-04 Normalized Thrust =-2.411721	
W=0 and P= 5	Normalized Moment =-.1589717 Normalized Thrust =-2.043421	
W=0 and P= 10	Normalized Moment =-.3574231 Normalized Thrust =-1.583047	

Loads at loading point # 8

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	8.12854	-10.20715
C 2	7.517884	-5.541046
C 3	.4767914	-.6687546
W=5# and P= 0	Strain in top gage= 8.12854 Strain in bottom gage=-10.20715 Moment M=-.716238 Thrust N=-3.8974	
W=5# and P= 1	Strain in top gage= 16.12322 Strain in bottom gage=-16.41695 Moment M=-1.2711 Thrust N=-.5507613	
W=5# and P= 5	Strain in top gage= 57.63774 Strain in bottom gage=-54.63125 Moment M=-4.385308 Thrust N=-5.637174	
W=5# and P= 10	Strain in top gage= 130.9865 Strain in bottom gage=-132.4931 Moment M=-10.29217 Thrust N=-2.824883	
W=0 and P= 1	Normalized Moment =-.5548623 Normalized Thrust =-3.346639	
W=0 and P= 5	Normalized Moment =-.7338539 Normalized Thrust =-1.906915	
W=0 and P= 10	Normalized Moment =-.9575933 Normalized Thrust = .1072598	

## Loads at loading point # 9

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	31.61072	-28.10358
C 2	.8655091	.5212403
C 3	.4325924	-.5709856

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W=5# and P= 0 Strain in top gage= 31.61072  
 Strain in bottom gage=-28.10358  
 Moment M=-2.33259  
 Thrust N=-6.57589

W=5# and P= 1 Strain in top gage= 32.90882  
 Strain in bottom gage=-28.15332  
 Moment M=-2.38524  
 Thrust N=-8.91556

W=5# and P= 5 Strain in top gage= 46.75308  
 Strain in bottom gage=-39.77202  
 Moment M=-3.379887  
 Thrust N=-13.08948

W=5# and P= 10 Strain in top gage= 83.52505  
 Strain in bottom gage=-79.98976  
 Moment M=-6.387297  
 Thrust N=-6.628576

W=0 and P= 1  
 Normalized Moment =-5.255035E-02  
 Normalized Thrust =-2.340671

W=0 and P= 5  
 Normalized Moment =-.2094594  
 Normalized Thrust =-1.302718

W=0 and P= 10  
 Normalized Moment =-.4054708  
 Normalized Thrust = 5.278588E-03



\*\*\*\*\*  
 \* Strain gage nos. 17 and 18  
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Loads at loading point # 1

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	13.91428	-20.01786
C 2	.8300018	-.5616074
C 3	-7.857132E-02	.0111599

W=5# and P= 0 Strain in top gage= 13.91428  
 Strain in bottom gage=-20.01786  
 Moment M=-1.325474  
 Thrust N=-11.44421

W=5# and P= 1 Strain in top gage= 14.66571  
 Strain in bottom gage=-20.56831  
 Moment M=-1.376329  
 Thrust N=-11.06736

W=5# and P= 5 Strain in top gage= 16.10001  
 Strain in bottom gage=-22.5469  
 Moment M=-1.509645  
 Thrust N=-12.00792

W=5# and P= 10 Strain in top gage= 14.35717  
 Strain in bottom gage=-24.51795  
 Moment M=-1.518539  
 Thrust N=-19.05145

W=0 and P= 1  
 Normalized Moment =-5.085461E-02  
 Normalized Thrust = .3768432

W=0 and P= 5  
 Normalized Moment =-3.683411E-02  
 Normalized Thrust =-.1287425

W=0 and P= 10  
 Normalized Moment =-1.938848E-02  
 Normalized Thrust =-.7607246

## Loads at loading point # 2

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	11.76427	-19.98714
C 2	6.188935	-6.653214
C 3	-.1866874	.1901779
W=5% and P= 0 Strain in top gage= 11.76427		
Strain in bottom gage=-19.98714		
Moment M=-1.237164		
Thrust N=-15.26788		
W=5% and P= 1 Strain in top gage= 17.76659		
Strain in bottom gage=-26.37817		
Moment M=-1.724892		
Thrust N=-16.13171		
W=5% and P= 5 Strain in top gage= 38.04376		
Strain in bottom gage=-48.41876		
Moment M=-3.377442		
Thrust N=-19.45313		
W=5% and P= 10 Strain in top gage= 54.99288		
Strain in bottom gage=-67.42148		
Moment M=-4.781811		
Thrust N=-23.38363		
W=0 and P= 1		
Normalized Moment =-.4869282		
Normalized Thrust =-.8638287		
W=0 and P= 5		
Normalized Moment =-.4280555		
Normalized Thrust =-.8370495		
W=0 and P= 10		
Normalized Moment =-.3544647		
Normalized Thrust =-.8035755		

## Loads at loading point # 3

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	27.90711	-35.32504
C 2	6.201111	-7.508506
C 3	6.874048E-02	-6.652451E-02
W=50 and P= 0	Strain in top gage= 27.90711 Strain in bottom gage=-35.32504 Moment M=-2.470006 Thrust N=-13.90663	
W=50 and P= 1	Strain in top gage= 34.17697 Strain in bottom gage=-42.97208 Moment M=-3.013634 Thrust N=-16.49083	
W=50 and P= 5	Strain in top gage= 60.63137 Strain in bottom gage=-74.89069 Moment M=-5.293831 Thrust N=-26.73622	
W=50 and P= 10	Strain in top gage= 96.79306 Strain in bottom gage=-117.7826 Moment M=-8.38186 Thrust N=-39.35529	
W=0 and P= 1	Normalized Moment =-.5435285 Normalized Thrust =-2.582195	
W=0 and P= 5	Normalized Moment =-.564765 Normalized Thrust =-2.565517	
W=0 and P= 10	Normalized Moment =-.5911854 Normalized Thrust =-2.544665	

## Loads at loading point # 4

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	29.95355	-48.97144
C 2	7.734101	-6.754303
C 3	-.2138386	1.071549E-02
W=5# and P= 0	Strain in top gage= 29.95355 Strain in bottom gage=-48.97144 Moment M=-3.083007 Thrust N=-35.65853	
W=5# and P= 1	Strain in top gage= 37.47382 Strain in bottom gage=-55.71503 Moment M=-3.640189 Thrust N=-34.20226	
W=5# and P= 5	Strain in top gage= 63.27809 Strain in bottom gage=-82.47507 Moment M=-5.693483 Thrust N=-35.99433	
W=5# and P= 10	Strain in top gage= 85.9107 Strain in bottom gage=-115.4429 Moment M=-7.865376 Thrust N=-55.37291	
W=0 and P= 1	Normalized Moment =-.5571817 Normalized Thrust =-1.456268	
W=0 and P= 5	Normalized Moment =-.5220951 Normalized Thrust =-6.715965E-02	
W=0 and P= 10	Normalized Moment =-.4782368 Normalized Thrust =-1.971438	



## Loads at loading point # 5

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	40.31079	-52.36429
C 2	-12.26663	8.055359
C 3	-.1834831	.4937516

W=5# and P= 0 Strain in top gage= 40.31079  
 Strain in bottom gage=-52.36429  
 Moment M=-3.62012  
 Thrust N=-22.60031

W=5# and P= 1 Strain in top gage= 27.86068  
 Strain in bottom gage=-43.81518  
 Moment M=-2.799838  
 Thrust N=-29.91469

W=5# and P= 5 Strain in top gage=-25.68945  
 Strain in bottom gage= .2562943  
 Moment M= 1.018381  
 Thrust N=-47.53717

W=5# and P= 10 Strain in top gage=-100.7038  
 Strain in bottom gage= 77.56446  
 Moment M= 6.963606  
 Thrust N=-43.38636

W=0 and P= 1  
 Normalized Moment = .8202823  
 Normalized Thrust =-7.314384

W=0 and P= 5  
 Normalized Moment = .9261001  
 Normalized Thrust =-4.987373

W=0 and P= 10  
 Normalized Moment = 1.058373  
 Normalized Thrust =-2.078605

## Loads at loading point # 6

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	12.9715	-32
C 2	-15.38585	17.20588
C 3	-.4553566	.3875888
W=5# and P= 0	Strain in top gage= 12.9715 Strain in bottom gage=-32 Moment M=-1.756699 Thrust N=-35.67845	
W=5# and P= 1	Strain in top gage=-2.788914 Strain in bottom gage=-14.40742 Moment M=-.453848 Thrust N=-32.24313	
W=5# and P= 5	Strain in top gage=-74.93768 Strain in bottom gage= 63.71291 Moment M= 5.416839 Thrust N=-21.84646	
W=5# and P= 10	Strain in top gage=-185.6147 Strain in bottom gage= 178.8889 Moment M= 14.23498 Thrust N=-12.77596	
W=0 and P= 1	Normalized Moment = 1.382851 Normalized Thrust =-3.435316	
W=0 and P= 5	Normalized Moment = 1.434548 Normalized Thrust =-2.926397	
W=0 and P= 10	Normalized Moment = 1.599168 Normalized Thrust =-2.298249	

Loads at loading point # 7

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	21.52501	-19.87502
C 2	-4.205185	2.066971
C 3	.6736622	-.5102702

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W=5# and P= 0 Strain in top gage= 21.52501  
 Strain in bottom gage=-19.87502  
 Moment M=-1.617189  
 Thrust N=-3.093739

W=5# and P= 1 Strain in top gage= 17.99349  
 Strain in bottom gage=-18.31831  
 Moment M=-1.41843  
 Thrust N=-.609051

W=5# and P= 5 Strain in top gage= 17.34064  
 Strain in bottom gage=-22.29691  
 Moment M=-1.548342  
 Thrust N=-9.293014

W=5# and P= 10 Strain in top gage= 46.83938  
 Strain in bottom gage=-50.23232  
 Moment M=-3.791864  
 Thrust N=-6.361764

W=0 and P= 1  
 Normalized Moment = .1987588  
 Normalized Thrust =-3.70279

W=0 and P= 5  
 Normalized Moment = 1.376931E-02  
 Normalized Thrust =-2.477351

W=0 and P= 10  
 Normalized Moment =-.2174675  
 Normalized Thrust =-.9455501

## Loads at loading point # 8

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	4.824921	-5.42865
C 2	7.7899	-7.822125
C 3	.4111595	-.5089341
W=5# and P= 0	Strain in top gage= 4.824921 Strain in bottom gage=-5.42865 Moment M=-.4885381 Thrust N=-1.131992	
W=5# and P= 1	Strain in top gage= 12.94598 Strain in bottom gage=-12.95971 Moment M=-1.811941 Thrust N=-2.574286E-02	
W=5# and P= 5	Strain in top gage= 53.65341 Strain in bottom gage=-53.26263 Moment M=-4.176487 Thrust N= .7327151	
W=5# and P= 10	Strain in top gage= 123.8399 Strain in bottom gage=-126.5433 Moment M=-9.749343 Thrust N=-6.568938	
W=0 and P= 1	Normalized Moment =-.6114189 Normalized Thrust =-1.18625	
W=0 and P= 5	Normalized Moment =-.7551755 Normalized Thrust = .3729415	
W=0 and P= 10	Normalized Moment =-.9348813 Normalized Thrust =-.5436945	

Loads at loading point # 9

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	25.13928	-24.19641
C 2	.7512818	.3337402
C 3	.4683837	-.5915184

W=5# and P= 0 Strain in top gage= 25.13928  
Strain in bottom gage=-24.19641  
Moment M=-1.927176  
Thrust N=-1.767883

W=5# and P= 1 Strain in top gage= 26.35887  
Strain in bottom gage=-24.45419  
Moment M=-1.984885  
Thrust N=-3.571272

W=5# and P= 5 Strain in top gage= 48.60328  
Strain in bottom gage=-37.31567  
Moment M=-3.043709  
Thrust N=-6.164274

W=5# and P= 10 Strain in top gage= 79.48247  
Strain in bottom gage=-88.01085  
Moment M=-6.238208  
Thrust N=-.990715

W=0 and P= 1  
Normalized Moment =-5.770952E-02  
Normalized Thrust =-1.003389

W=0 and P= 5  
Normalized Moment =-.2233067  
Normalized Thrust = .8792782

W=0 and P= 10  
Normalized Moment =-.4303032  
Normalized Thrust =-.2758598

Loads at loading point # 10

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	23.96785	-21.0687
C 2	1.968399	-1.117333
C 3	-3.526688E-02	-2.098274E-02
W=5# and P= 0	Strain in top gage= 23.96785 Strain in bottom gage=-21.0687 Moment M=-1.758928 Thrust N=-5.458987	
W=5# and P= 1	Strain in top gage= 25.90098 Strain in bottom gage=-22.19902 Moment M=-1.878906 Thrust N=-6.941189	
W=5# and P= 5	Strain in top gage= 32.92817 Strain in bottom gage=-27.17193 Moment M=-2.34766 Thrust N=-10.79296	
W=5# and P= 10	Strain in top gage= 40.12515 Strain in bottom gage=-34.3323 Moment M=-2.908494 Thrust N=-10.8616	
W=0 and P= 1	Normalized Moment =-.1199784 Normalized Thrust =-1.490282	
W=0 and P= 5	Normalized Moment =-.1177465 Normalized Thrust =-1.06841	
W=0 and P= 10	Normalized Moment =-.1149566 Normalized Thrust =-.5410695	

\*\*\*\*\*  
 \* Strain gage nos. 19 and 20  
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Loads at loading point # 1

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-40.89287	36.00714
C 2	1.363922	-.8767776
C 3	-.0048217	3.482151E-02

W=5# and P= 0 Strain in top gage=-40.89287  
 Strain in bottom gage= 36.00714  
 Moment M= 3.003907  
 Thrust N=-9.168738

W=5# and P= 1 Strain in top gage=-39.61377  
 Strain in bottom gage= 35.16519  
 Moment M= 2.921053  
 Thrust N=-8.341096

W=5# and P= 5 Strain in top gage=-36.1938  
 Strain in bottom gage= 32.49379  
 Moment M= 2.683109  
 Thrust N=-6.937523

W=5# and P= 10 Strain in top gage=-35.73582  
 Strain in bottom gage= 30.72152  
 Moment M= 2.59599  
 Thrust N=-9.401816

W=0 and P= 1  
 Normalized Moment =-8.285374E-02  
 Normalized Thrust = .8196402

W=0 and P= 5  
 Normalized Moment =-6.415951E-02  
 Normalized Thrust = .444643

W=0 and P= 10  
 Normalized Moment =-4.079171E-02  
 Normalized Thrust =-.0241077

## Loads at loading point # 2

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-35.71073	32.70356
C 2	-.6698151	-.1876755
C 3	6.026554E-02	-2.723122E-02

W=5# and P= 0 Strain in top gage=-35.71073  
 Strain in bottom gage= 32.70356  
 Moment M= 2.672434  
 Thrust N=-5.63839

W=5# and P= 1 Strain in top gage=-36.32028  
 Strain in bottom gage= 32.48868  
 Moment M= 2.68785  
 Thrust N=-7.184243

W=5# and P= 5 Strain in top gage=-37.55316  
 Strain in bottom gage= 31.08443  
 Moment M= 2.681156  
 Thrust N=-12.12888

W=5# and P= 10 Strain in top gage=-36.38232  
 Strain in bottom gage= 28.10371  
 Moment M= 2.518985  
 Thrust N=-15.5224

W=0 and P= 1  
 Normalized Moment = 1.541585E-02  
 Normalized Thrust =-1.543854

W=0 and P= 5  
 Normalized Moment = 1.744375E-03  
 Normalized Thrust =-1.290098

W=0 and P= 10  
 Normalized Moment =-1.534484E-02  
 Normalized Thrust =-.9884012



Loads at loading point # 3

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-38.37857	34.37859
C 2	-.2596436	-1.214645
C 3	.13482	-9.196377E-02
W=5# and P= 0	Strain in top gage=-38.37857 Strain in bottom gage= 34.37859 Moment M= 2.842876 Thrust N=-7.499972	
W=5# and P= 1	Strain in top gage=-38.5834 Strain in bottom gage= 33.87198 Moment M= 2.795913 Thrust N=-10.18391	
W=5# and P= 5	Strain in top gage=-36.38629 Strain in bottom gage= 26.88626 Moment M= 2.434884 Thrust N=-19.31255	
W=5# and P= 10	Strain in top gage=-27.49381 Strain in bottom gage= 13.83576 Moment M= 1.583155 Thrust N=-27.18735	
W=0 and P= 1	Normalized Moment =-.0461635 Normalized Thrust =-2.68394	
W=0 and P= 5	Normalized Moment =-8.159846E-02 Normalized Thrust =-2.362516	
W=0 and P= 10	Normalized Moment =-.1258922 Normalized Thrust =-1.968738	

Loads at loading point # 4

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-25.16872	13.82143
C 2	2.128391	-1.661785
C 3	-5.312538E-02	-5.624998E-02
W=5# and P= 0	Strain in top gage=-25.16872 Strain in bottom gage= 13.82143 Moment M= 1.49149 Thrust N=-22.76117	
W=5# and P= 1	Strain in top gage=-23.08545 Strain in bottom gage= 11.38339 Moment M= 1.343314 Thrust N=-22.09136	
W=5# and P= 5	Strain in top gage=-15.8469 Strain in bottom gage= 3.386255 Moment M= .7481699 Thrust N=-23.5137	
W=5# and P= 10	Strain in top gage=-9.189342 Strain in bottom gage=-9.22142 Moment M=-1.253839E-03 Thrust N=-34.52018	
W=0 and P= 1	Normalized Moment =-.1481758 Normalized Thrust = .6698884	
W=0 and P= 5	Normalized Moment =-.148664 Normalized Thrust =-.1585073	
W=0 and P= 10	Normalized Moment =-.1492743 Normalized Thrust =-1.175982	

Loads at loading point # 5

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-11.10358	3.832123
C 2	-1.662308	-2.970566
C 3	.8772326	-.5058041
W=50 and P= 0	Strain in top gage=-11.10358 Strain in bottom gage= 3.832123 Moment M= .5834258 Thrust N=-13.63398	
W=50 and P= 1	Strain in top gage=-11.88865 Strain in bottom gage= .355753 Moment M= .4782971 Thrust N=-21.62419	
W=50 and P= 5	Strain in top gage= 2.515699 Strain in bottom gage=-23.66581 Moment M=-1.022715 Thrust N=-39.65645	
W=50 and P= 10	Strain in top gage= 59.9966 Strain in bottom gage=-76.45395 Moment M=-5.330099 Thrust N=-38.85752	
W=0 and P= 1	Normalized Moment =-.1051287 Normalized Thrust =-7.99021	
W=0 and P= 5	Normalized Moment =-.3212282 Normalized Thrust =-5.204496	
W=0 and P= 10	Normalized Moment =-.5913525 Normalized Thrust =-1.722355	

## Loads at loading point # 6

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	-63.14644	43.76428
C 2	8.214829	-7.156784
C 3	.2915182	-.3844653

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W=5# and P= 0 Strain in top gage=-63.14644  
 Strain in bottom gage= 43.76428  
 Moment M= 4.1762  
 Thrust N=-36.34155

W=5# and P= 1 Strain in top gage=-54.64889  
 Strain in bottom gage= 36.38383  
 Moment M= 3.552466  
 Thrust N=-34.38199

W=5# and P= 5 Strain in top gage=-14.78434  
 Strain in bottom gage= .3687287  
 Moment M= .5919168  
 Thrust N=-27.82927

W=5# and P= 10 Strain in top gage= 48.15367  
 Strain in bottom gage=-58.25809  
 Moment M=-4.156397  
 Thrust N=-18.93879

W=0 and P= 1  
 Normalized Moment =-.6237343  
 Normalized Thrust =-1.95958

W=0 and P= 5  
 Normalized Moment =-.7168567  
 Normalized Thrust =-1.862454

W=0 and P= 10  
 Normalized Moment =-.8332597  
 Normalized Thrust =-1.741876

Loads at loading point # 7

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-58.92582	55.34641
C 2	4.978154	-6.586943
C 3	-.7611618	.8674187
W=5# and P= 0	Strain in top gage=-58.92582	
	Strain in bottom gage= 55.34641	
	Moment M= 4.463728	
	Thrust N=-6.7899	
W=5# and P= 1	Strain in top gage=-54.71683	
	Strain in bottom gage= 49.78687	
	Moment M= 4.87982	
	Thrust N=-9.392166	
W=5# and P= 5	Strain in top gage=-53.1833	
	Strain in bottom gage= 44.49696	
	Moment M= 3.81251	
	Thrust N=-16.13689	
W=5# and P= 10	Strain in top gage=-85.33966	
	Strain in bottom gage= 77.81805	
	Moment M= 6.342898	
	Thrust N=-15.68383	
W=0 and P= 1	Normalized Moment =-.3847081	
	Normalized Thrust =-2.682266	
W=0 and P= 5	Normalized Moment =-.1382435	
	Normalized Thrust =-1.885397	
W=0 and P= 10	Normalized Moment =.187837	
	Normalized Thrust =-.8893132	

Loads at loading point # 8

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-70.00911	64.68555
C 2	-11.37378	13.47791
C 3	-1.387055	1.1875
W=5# and P= 0	Strain in top gage=-70.00911 Strain in bottom gage= 64.68555 Moment M= 5.264635 Thrust N=-10.13168	
W=5# and P= 1	Strain in top gage=-82.84995 Strain in bottom gage= 79.35095 Moment M= 6.335973 Thrust N=-6.560612	
W=5# and P= 5	Strain in top gage=-161.6344 Strain in bottom gage= 161.7626 Moment M= 12.63269 Thrust N= .2483832	
W=5# and P= 10	Strain in top gage=-322.5324 Strain in bottom gage= 318.2146 Moment M= 25.02918 Thrust N=-8.09578	
W=0 and P= 1	Normalized Moment = 1.071338 Normalized Thrust =-3.571072	
W=0 and P= 5	Normalized Moment = 1.473612 Normalized Thrust =-2.074413	
W=0 and P= 10	Normalized Moment = 1.976454 Normalized Thrust = .2835904	

Loads at loading point # 9

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-85.68933	92.38713
C 2	-9.724426	9.840485
C 3	-.8924256	.8883896
W=5# and P= 0	Strain in top gage=-85.68933 Strain in bottom gage= 92.38713 Moment M= 6.952987 Thrust N=-12.40837	
W=5# and P= 1	Strain in top gage=-96.38618 Strain in bottom gage= 182.2359 Moment M= 7.755552 Thrust N=-11.11826	
W=5# and P= 5	Strain in top gage=-156.6221 Strain in bottom gage= 159.7189 Moment M= 12.35787 Thrust N=-5.886584	
W=5# and P= 10	Strain in top gage=-272.1762 Strain in bottom gage= 271.5582 Moment M= 21.23931 Thrust N=-1.173763	
W=0 and P= 1	Normalized Moment = .8825643 Normalized Thrust =-1.298187	
W=0 and P= 5	Normalized Moment = 1.888817 Normalized Thrust =-1.328374	
W=0 and P= 10	Normalized Moment = 1.428632 Normalized Thrust =-1.358213	

Loads at loading point # 10

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-71.16068	78.08216
C 2	-1.948731	2.04126
C 3	1.630292E-02	-1.741028E-02
W=5# and P= 0	Strain in top gage=-71.16068 Strain in bottom gage= 78.08216 Moment M= 5.829798 Thrust N=-12.97777	
W=5# and P= 1	Strain in top gage=-73.0911 Strain in bottom gage= 80.186 Moment M= 5.984263 Thrust N=-13.15294	
W=5# and P= 5	Strain in top gage=-80.44676 Strain in bottom gage= 87.85319 Moment M= 6.574217 Thrust N=-13.88708	
W=5# and P= 10	Strain in top gage=-88.81769 Strain in bottom gage= 96.75372 Moment M= 7.248883 Thrust N=-14.88007	
W=0 and P= 1	Normalized Moment = .154464 Normalized Thrust = .1751661	
W=0 and P= 5	Normalized Moment = .1488838 Normalized Thrust = .1818609	
W=0 and P= 10	Normalized Moment = .1419085 Normalized Thrust = .1902234	



\*\*\*\*\*  
 \* Strain gage nos. 21 and 22  
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Loads at loading point # 1

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-35.43215	29.99643
C 2	.9683914	.1041107
C 3	-.0682684	-4.955292E-02

W=5# and P= 0 Strain in top gage=-35.43215  
 Strain in bottom gage= 29.99643  
 Moment M= 2.553804  
 Thrust N=-10.19197

W=5# and P= 1 Strain in top gage=-34.52482  
 Strain in bottom gage= 30.05099  
 Moment M= 2.522462  
 Thrust N=-8.386938

W=5# and P= 5 Strain in top gage=-32.0969  
 Strain in bottom gage= 29.27816  
 Moment M= 2.397463  
 Thrust N=-5.285132

W=5# and P= 10 Strain in top gage=-31.77507  
 Strain in bottom gage= 26.08225  
 Moment M= 2.260051  
 Thrust N=-10.67405

W=0 and P= 1  
 Normalized Moment =-3.334239E-02  
 Normalized Thrust =-1.085027

W=0 and P= 5  
 Normalized Moment =-.0316681  
 Normalized Thrust = .9813666

W=0 and P= 10  
 Normalized Moment =-2.557523E-02  
 Normalized Thrust =-4.820824E-02

Loads at loading point # 2

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-33.03574	30.17143
C 2	.4653473	-.9828415
C 3	-3.839398E-02	3.571415E-02
W=5# and P= 0	Strain in top gage=-33.03574 Strain in bottom gage= 30.17143	
	Moment M= 2.46903	
	Thrust N=-5.378569	
W=5# and P= 1	Strain in top gage=-32.60878 Strain in bottom gage= 29.22431	
	Moment M= 2.415355	
	Thrust N=-6.345899	
W=5# and P= 5	Strain in top gage=-31.66885 Strain in bottom gage= 26.15008	
	Moment M= 2.258552	
	Thrust N=-18.3477	
W=5# and P= 10	Strain in top gage=-32.22166 Strain in bottom gage= 23.91443	
	Moment M= 2.192816	
	Thrust N=-15.57685	
W=0 and P= 1	Normalized Moment =-5.367583E-02 Normalized Thrust =-.9753299	
W=0 and P= 5	Normalized Moment =-4.209563E-02 Normalized Thrust =-.9954257	
W=0 and P= 10	Normalized Moment =-2.762139E-02 Normalized Thrust =-1.028548	

## Loads at loading point # 3

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-32.72582	38.91786
C 2	-.7134818	-.8662432
C 3	.1628531	-.1288886
W=5# and P= 0	Strain in top gage=-32.72582 Strain in bottom gage= 38.91786 Moment M= 2.48685 Thrust N=-3.388424	
W=5# and P= 1	Strain in top gage=-33.27637 Strain in bottom gage= 29.93153 Moment M= 2.469859 Thrust N=-6.271581	
W=5# and P= 5	Strain in top gage=-32.2487 Strain in bottom gage= 23.58442 Moment M= 2.188669 Thrust N=-16.23853	
W=5# and P= 10	Strain in top gage=-23.65373 Strain in bottom gage= 18.24655 Moment M= 1.32423 Thrust N=-25.13846	
W=0 and P= 1	Normalized Moment =-1.699157E-02 Normalized Thrust =-2.883157	
W=0 and P= 5	Normalized Moment =-6.187624E-02 Normalized Thrust =-2.568421	
W=0 and P= 10	Normalized Moment =-.1161821 Normalized Thrust =-2.175803	



## Loads at loading point # 5

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-9.853589	3.55716
C 2	-.9483795	-2.696427
C 3	.7816973	-.5125008
W=5# and P= 0	Strain in top gage=-9.853589 Strain in bottom gage= 3.55716 Moment M= .4926874 Thrust N=-10.38581	
W=5# and P= 1	Strain in top gage=-9.228271 Strain in bottom gage= .3482323 Moment M= .3737697 Thrust N=-16.63587	
W=5# and P= 5	Strain in top gage= 5.746946 Strain in bottom gage=-22.73749 Moment M=-1.112673 Thrust N=-31.85728	
W=5# and P= 10	Strain in top gage= 59.63234 Strain in bottom gage=-74.65718 Moment M=-5.245685 Thrust N=-28.17158	
W=0 and P= 1	Normalized Moment =-.1188377 Normalized Thrust =-6.329268	
W=0 and P= 5	Normalized Moment =-.3218561 Normalized Thrust =-4.318294	
W=0 and P= 10	Normalized Moment =-.5738292 Normalized Thrust =-1.786577	

Loads at loading point # 6

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-56.5893	34.9536
C 2	8.479828	-7.245178
C 3	.2647324	-.3334847
W=5# and P= 0	Strain in top gage=-56.5893 Strain in bottom gage= 34.9536 Moment M= 3.575894 Thrust N=-40.56693	
W=5# and P= 1	Strain in top gage=-47.84474 Strain in bottom gage= 27.37494 Moment M= 2.938268 Thrust N=-38.38088	
W=5# and P= 5	Strain in top gage=-7.571846 Strain in bottom gage=-9.689489 Moment M=-7.959232E-02 Thrust N=-32.21486	
W=5# and P= 10	Strain in top gage= 54.68222 Strain in bottom gage=-78.84665 Moment M=-4.903472 Thrust N=-30.38831	
W=0 and P= 1	Normalized Moment =-.637626 Normalized Thrust =-2.186058	
W=0 and P= 5	Normalized Moment =-.7310973 Normalized Thrust =-1.678416	
W=0 and P= 10	Normalized Moment =-.8479365 Normalized Thrust =-1.025863	

Loads at loading point # 7

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-52.71073	42.42496
C 2	6.541611	-5.886597
C 3	-.7790203	.6879473
W=5# and P= 0	Strain in top gage=-52.71073 Strain in bottom gage= 42.42496 Moment M= 3.716238 Thrust N=-19.28581	
W=5# and P= 1	Strain in top gage=-46.94814 Strain in bottom gage= 37.22631 Moment M= 3.289064 Thrust N=-18.22843	
W=5# and P= 5	Strain in top gage=-39.47818 Strain in bottom gage= 30.19066 Moment M= 2.721439 Thrust N=-17.41411	
W=5# and P= 10	Strain in top gage=-65.19665 Strain in bottom gage= 52.35372 Moment M= 4.591811 Thrust N=-24.0885	
W=0 and P= 1	Normalized Moment =-.4281734 Normalized Thrust =-1.057384	
W=0 and P= 5	Normalized Moment =-.1989597 Normalized Thrust = .3743405	
W=0 and P= 10	Normalized Moment = 8.755736E-02 Normalized Thrust =-.4794681	

Loads at loading point # 8

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-62.23572	57.125
C 2	-10.74469	11.24921
C 3	-1.138397	1.055809
W=5# and P= 0	Strain in top gage=-62.23572 Strain in bottom gage= 57.125 Moment M= 4.662528 Thrust N=-9.562596	
W=5# and P= 1	Strain in top gage=-74.11881 Strain in bottom gage= 69.43001 Moment M= 5.607376 Thrust N=-6.79148	
W=5# and P= 5	Strain in top gage=-144.4191 Strain in bottom gage= 139.7663 Moment M= 11.10099 Thrust N=-8.72406	
W=5# and P= 10	Strain in top gage=-283.5224 Strain in bottom gage= 275.196 Moment M= 21.82501 Thrust N=-15.6082	
W=0 and P= 1	Normalized Moment = .9448478 Normalized Thrust = .7911158	
W=0 and P= 5	Normalized Moment = 1.287693 Normalized Thrust = .1717072	
W=0 and P= 10	Normalized Moment = 1.716248 Normalized Thrust = -.6025601	



Loads at loading point # 9

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	-78.62146	78.34998
C 2	-10.25537	10.54761
C 3	-.9973221	.9812546

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W=5# and P= 0 Strain in top gage=-78.62146  
 Strain in bottom gage= 78.34998  
 Moment M= 6.131697  
 Thrust N=-.5098332

W=5# and P= 1 Strain in top gage=-89.87416  
 Strain in bottom gage= 89.87884  
 Moment M= 7.021601  
 Thrust N= 8.783341E-03

W=5# and P= 5 Strain in top gage=-154.8314  
 Strain in bottom gage= 155.6194  
 Moment M= 12.12698  
 Thrust N=-1.477547

W=5# and P= 10 Strain in top gage=-280.9874  
 Strain in bottom gage= 281.9515  
 Moment M= 21.98668  
 Thrust N=-1.957741

W=0 and P= 1  
 Normalized Moment = .8899045  
 Normalized Thrust = .5178166

W=0 and P= 5  
 Normalized Moment = 1.199057  
 Normalized Thrust = .397316

W=0 and P= 10  
 Normalized Moment = 1.585498  
 Normalized Thrust = .2466774

Loads at loading point # 10

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-64.08566	66.90716
C 2	-2.297882	2.367523
C 3	1.250267E-02	-8.031845E-03
W=5# and P= 0	Strain in top gage=-64.08566 Strain in bottom gage= 66.90716 Moment M= 5.116987 Thrust N=-5.290318	
W=5# and P= 1	Strain in top gage=-66.37104 Strain in bottom gage= 69.26666 Moment M= 5.298348 Thrust N=-5.429278	
W=5# and P= 5	Strain in top gage=-75.26251 Strain in bottom gage= 78.54398 Moment M= 6.009066 Thrust N=-6.152773	
W=5# and P= 10	Strain in top gage=-85.81422 Strain in bottom gage= 89.77921 Moment M= 6.859119 Thrust N=-7.434368	
W=0 and P= 1	Normalized Moment = .1814401 Normalized Thrust = .1389599	
W=0 and P= 5	Normalized Moment = .1782317 Normalized Thrust = .1724911	
W=0 and P= 10	Normalized Moment = .1742211 Normalized Thrust = .2144051	

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 \* Strain gage nos. 23 and 24  
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Loads at loading point # 1

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-31.8286	28.39643
C 2	1.881447	-3.078037
C 3	-.132144	.1343756

W=5# and P= 0 Strain in top gage=-31.8286  
 Strain in bottom gage= 28.39643  
 Moment M= 2.35254  
 Thrust N=-6.435313

W=5# and P= 1 Strain in top gage=-30.0793  
 Strain in bottom gage= 25.45277  
 Moment M= 2.169222  
 Thrust N=-6.674736

W=5# and P= 5 Strain in top gage=-25.72497  
 Strain in bottom gage= 16.36564  
 Moment M= 1.644164  
 Thrust N=-17.54874

W=5# and P= 10 Strain in top gage=-26.22853  
 Strain in bottom gage= 11.05362  
 Moment M= 1.456334  
 Thrust N=-28.45296

W=0 and P= 1 Normalized Moment =-.1833189  
 Normalized Thrust =-2.239423

W=0 and P= 5 Normalized Moment =-.1416752  
 Normalized Thrust =-2.222686

W=0 and P= 10 Normalized Moment =-8.962065E-02  
 Normalized Thrust =-2.201765

Loads at loading point # 2

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-26.64268	13.63929
C 2	.1007233	-.6750919
C 3	-8.930206E-03	.0397327
W=5# and P= 0	Strain in top gage=-26.64268 Strain in bottom gage= 13.63929	
	Moment M= 1.573522	
	Thrust N=-24.38174	
W=5# and P= 1	Strain in top gage=-26.55189	
	Strain in bottom gage= 13.00313	
	Moment M= 1.545087	
	Thrust N=-25.40243	
W=5# and P= 5	Strain in top gage=-26.36252	
	Strain in bottom gage= 11.25315	
	Moment M= 1.469362	
	Thrust N=-28.33008	
W=5# and P= 10	Strain in top gage=-26.52867	
	Strain in bottom gage= 10.85364	
	Moment M= 1.460247	
	Thrust N=-29.39068	
W=0 and P= 1	Normalized Moment =-2.843563E-02	
	Normalized Thrust =-1.020686	
W=0 and P= 5	Normalized Moment =-2.063205E-02	
	Normalized Thrust =-.7896678	
W=0 and P= 10	Normalized Moment =-1.132758E-02	
	Normalized Thrust =-.5008945	

Loads at loading point # 3

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-26.06072	14.025
C 2	-1.439461	-.390893
C 3	.212946	-.1691965
W=5# and P= 0	Strain in top gage=-26.06072 Strain in bottom gage= 14.025 Moment M= 1.565849 Thrust N=-22.56690	
W=5# and P= 1	Strain in top gage=-27.28724 Strain in bottom gage= 13.46491 Moment M= 1.591881 Thrust N=-25.91686	
W=5# and P= 5	Strain in top gage=-27.93438 Strain in bottom gage= 7.840623 Moment M= 1.397461 Thrust N=-37.67579	
W=5# and P= 10	Strain in top gage=-19.16074 Strain in bottom gage=-6.003576 Moment M= .4827016 Thrust N=-48.68309	
W=0 and P= 1	Normalized Moment = 2.603226E-02 Normalized Thrust =-3.349882	
W=0 and P= 5	Normalized Moment =-3.367751E-02 Normalized Thrust =-3.021762	
W=0 and P= 10	Normalized Moment =-.1083147 Normalized Thrust =-2.611611	

## Loads at loading point # 4

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-16.17142	-7.11871
C 2	2.20871	-.977684
C 3	-.1267858	-7.366885E-02
W=5# and P= 0	Strain in top gage=-16.17142 Strain in bottom gage=-7.11871 Moment M= .353934 Thrust N=-43.654	
W=5# and P= 1	Strain in top gage=-14.0975 Strain in bottom gage=-8.162055 Moment M= .2318532 Thrust N=-41.73666	
W=5# and P= 5	Strain in top gage=-8.337513 Strain in bottom gage=-13.84065 Moment M=-.2149564 Thrust N=-41.58406	
W=5# and P= 10	Strain in top gage=-6.842894 Strain in bottom gage=-24.25364 Moment M=-.6801871 Thrust N=-58.30599	
W=0 and P= 1	Normalized Moment =-.1228889 Normalized Thrust =-1.917338	
W=0 and P= 5	Normalized Moment =-.1137801 Normalized Thrust = .4139876	
W=0 and P= 10	Normalized Moment =-.1034041 Normalized Thrust =-1.4652	

Loads at loading point # 5

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-4.489289	-1.050049
C 2	-1.90802	-5.361786
C 3	.0050033	-.2633953
W=5# and P= 0	Strain in top gage=-4.489289 Strain in bottom gage=-1.050049 Moment M= .1343453 Thrust N=-10.38525	
W=5# and P= 1	Strain in top gage=-5.591585 Strain in bottom gage=-6.67523 Moment M=-4.233301E-02 Thrust N=-23.00013	
W=5# and P= 5	Strain in top gage= 6.115694 Strain in bottom gage=-34.44386 Moment M=-1.584358 Thrust N=-53.11532	
W=5# and P= 10	Strain in top gage= 57.01084 Strain in bottom gage=-81.00744 Moment M=-5.39134 Thrust N=-44.99362	
W=0 and P= 1	Normalized Moment =-.1766783 Normalized Thrust =-12.61387	
W=0 and P= 5	Normalized Moment =-.3437406 Normalized Thrust =-8.545812	
W=0 and P= 10	Normalized Moment =-.5525685 Normalized Thrust =-3.468736	

## Loads at loading point # 6

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	-56.15715	31.92142
C 2	8.765014	-6.951767
C 3	.2267857	-.3562527

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W=5# and P= 0 Strain in top gage=-56.15715  
 Strain in bottom gage= 31.92142  
 Moment M= 3.448569  
 Thrust N=-45.442

W=5# and P= 1 Strain in top gage=-47.16535  
 Strain in bottom gage= 24.6134  
 Moment M= 2.883857  
 Thrust N=-42.28491

W=5# and P= 5 Strain in top gage=-6.662438  
 Strain in bottom gage=-11.74374  
 Moment M=-.1984882  
 Thrust N=-34.51158

W=5# and P= 10 Strain in top gage= 54.17156  
 Strain in bottom gage=-73.22152  
 Moment M=-4.976292  
 Thrust N=-35.71867

W=0 and P= 1  
 Normalized Moment =-.6367117  
 Normalized Thrust =-3.157085

W=0 and P= 5  
 Normalized Moment =-.7278115  
 Normalized Thrust =-2.186885

W=0 and P= 10  
 Normalized Moment =-.8416861  
 Normalized Thrust = .9723329



Loads at loading point # 7

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	-50.51074	39.77857
C 2	6.611603	-7.431059
C 3	-.6540203	.7090225

---

W=5# and P= 0 Strain in top gages=-50.51074  
 Strain in bottom gages= 39.77857  
 Moment M= 3.526926  
 Thrust N=-20.12283

W=5# and P= 1 Strain in top gages=-44.55316  
 Strain in bottom gages= 33.05732  
 Moment M= 3.031659  
 Thrust N=-21.5547

W=5# and P= 5 Strain in top gages=-33.00324  
 Strain in bottom gages= 20.36879  
 Moment M= 2.116035  
 Thrust N=-25.18959

W=5# and P= 10 Strain in top gages=-49.79675  
 Strain in bottom gages= 36.45015  
 Moment M= 3.369019  
 Thrust N=-25.02487

W=0 and P= 1  
 Normalized Moment =-.4952666  
 Normalized Thrust =-1.431871

W=0 and P= 5  
 Normalized Moment =-.2821663  
 Normalized Thrust =-1.013351

W=0 and P= 10  
 Normalized Moment =-1.579069E-02  
 Normalized Thrust =-.4902041

Loads at loading point # 8

Coefficients C1, C2 and C3 for equations of curve fitting

---

	Top gages	Bot. gages
C 1	-61.3501	57.48578
C 2	-8.778198	11.50641
C 3	-.9866181	.7767945

---

W=5# and P= 0    Strain in top gage=-61.3501  
                      Strain in bottom gage= 57.48578  
                      Moment M= 4.642827  
                      Thrust N=-7.245598

W=5# and P= 1    Strain in top gage=-71.11491  
                      Strain in bottom gage= 69.76898  
                      Moment M= 5.583278  
                      Thrust N=-2.523623

W=5# and P= 5    Strain in top gage=-129.9065  
                      Strain in bottom gage= 134.4377  
                      Moment M= 10.32595  
                      Thrust N=-8.495894

W=5# and P= 10   Strain in top gage=-247.7939  
                      Strain in bottom gage= 250.2293  
                      Moment M= 19.45483  
                      Thrust N=-4.566422

W=0 and P= 1  
                      Normalized Moment = .8612508  
                      Normalized Thrust =-4.721976

W=0 and P= 5  
                      Normalized Moment = 1.136784  
                      Normalized Thrust =-3.148298

W=0 and P= 10  
                      Normalized Moment = 1.481281  
                      Normalized Thrust =-1.181282

Loads at loading point # 9

Coefficients C1, C2 and C3 for equations of curve fitting

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	Top gages	Bot. gages
C 1	-74.71423	82.78931
C 2	-11.43427	11.60596
C 3	-1.02858	1.02813

---

W=5# and P= 0 Strain in top gage=-74.71423  
 Strain in bottom gage= 82.78931  
 Moment M= 6.152482  
 Thrust N=-15.14076

W=5# and P= 1 Strain in top gage=-87.17708  
 Strain in bottom gage= 95.42339  
 Moment M= 7.132831  
 Thrust N=-15.46184

W=5# and P= 5 Strain in top gage=-157.6001  
 Strain in bottom gage= 166.5223  
 Moment M= 12.66183  
 Thrust N=-16.72929

W=5# and P= 10 Strain in top gage=-291.9149  
 Strain in bottom gage= 301.6618  
 Moment M= 23.18659  
 Thrust N=-18.27559

W=0 and P= 1  
 Normalized Moment = .9803489  
 Normalized Thrust = .3210783

W=0 and P= 5  
 Normalized Moment = 1.38171  
 Normalized Thrust = .3177052

W=0 and P= 10  
 Normalized Moment = 1.783411  
 Normalized Thrust = .3134823

Loads at loading point # 18

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	-60.54285	72.92582
C 2	-1.701447	2.671265
C 3	-5.000115E-02	-3.120422E-03
W=5# and P= 0	Strain in top gage=-60.54285 Strain in bottom gage= 72.92582 Moment M= 5.213589 Thrust N=-23.21657	
W=5# and P= 1	Strain in top gage=-62.2943 Strain in bottom gage= 75.59316 Moment M= 5.386229 Thrust N=-24.93538	
W=5# and P= 5	Strain in top gage=-70.30011 Strain in bottom gage= 86.28333 Moment M= 6.113416 Thrust N=-29.81854	
W=5# and P= 10	Strain in top gage=-82.55743 Strain in bottom gage= 99.32562 Moment M= 7.104807 Thrust N=-31.44037	
W=0 and P= 1	Normalized Moment = .1725404 Normalized Thrust =-1.718083	
W=0 and P= 5	Normalized Moment = .1799654 Normalized Thrust =-1.320394	
W=0 and P= 10	Normalized Moment = .1891218 Normalized Thrust = .8223796	

\*\*\*\*\*  
 \* Strain gage nos. 25 and 26  
 \*\*\*\*\*

Loads at loading point # 1

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	86.96879	-59.73218
C 2	3.382002E-02	1.773422
C 3	-6.115723E-02	-.0977726

W=5# and P= 0 Strain in top gage= 86.96879  
 Strain in bottom gage=-59.73218  
 Moment M=-5.730194  
 Thrust N=-51.05364

W=5# and P= 1 Strain in top gage= 86.93265  
 Strain in bottom gage=-58.05653  
 Moment M=-5.663639  
 Thrust N=-54.14273

W=5# and P= 5 Strain in top gage= 85.59696  
 Strain in bottom gage=-53.30938  
 Moment M=-5.426029  
 Thrust N=-60.53921

W=5# and P= 10 Strain in top gage= 81.17526  
 Strain in bottom gage=-51.77522  
 Moment M=-5.193378  
 Thrust N=-55.12509

W=0 and P= 1  
 Normalized Moment = 6.655425E-02  
 Normalized Thrust =-3.00909

W=0 and P= 5  
 Normalized Moment = 6.003304E-02  
 Normalized Thrust =-1.897113

W=0 and P= 10  
 Normalized Moment = 5.360158E-02  
 Normalized Thrust = .407145

Loads at loading point # 2

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	86.79645	-55.00716
C 2	-1.619446	1.459641
C 3	-2.633667E-02	1.160431E-02
W=5# and P= 0	Strain in top gage= 86.79645 Strain in bottom gage=-55.00716 Moment M=-5.539203 Thrust N=-59.60492	
W=5# and P= 1	Strain in top gage= 85.15066 Strain in bottom gage=-53.53591 Moment M=-5.417445 Thrust N=-59.27767	
W=5# and P= 5	Strain in top gage= 78.0400 Strain in bottom gage=-47.41885 Moment M=-4.900768 Thrust N=-57.41617	
W=5# and P= 10	Strain in top gage= 67.96833 Strain in bottom gage=-39.25032 Moment M=-4.188228 Thrust N=-53.84625	
W=0 and P= 1	Normalized Moment = .1217589 Normalized Thrust =-.3272581	
W=0 and P= 5	Normalized Moment = .1276872 Normalized Thrust =-.4377500	
W=0 and P= 10	Normalized Moment = .1350975 Normalized Thrust =-.5758667	

Loads at loading point # 3

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	83.87858	-58.71787
C 2	-1.621765	.9319687
C 3	-.3285338	.3129454
W=5# and P= 0 Strain in top gage= 83.87858		
Strain in bottom gage=-58.71787		
Moment M=-5.226424		
Thrust N=-68.67635		
W=5# and P= 1 Strain in top gage= 81.13628		
Strain in bottom gage=-49.47295		
Moment M=-5.181924		
Thrust N=-53.36875		
W=5# and P= 5 Strain in top gage= 66.95641		
Strain in bottom gage=-38.23439		
Moment M=-4.189816		
Thrust N=-53.8538		
W=5# and P= 10 Strain in top gage= 34.88756		
Strain in bottom gage=-18.18364		
Moment M=-1.754344		
Thrust N=-46.31984		
W=0 and P= 1		
Normalized Moment = .1245885		
Normalized Thrust =-1.387595		
W=0 and P= 5		
Normalized Moment = .2234816		
Normalized Thrust =-1.364509		
W=0 and P= 10		
Normalized Moment = .347288		
Normalized Thrust =-1.435651		

Loads at loading point # 4

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	56.95716	-31.43929
C 2	-2.002855	2.485893
C 3	-.1857147	8.526754E-02
W=5# and P= 0	Strain in top gage= 56.95716 Strain in bottom gage=-31.43929 Moment M=-3.531111 Thrust N=-51.596	
W=5# and P= 1	Strain in top gage= 56.68859 Strain in bottom gage=-28.86813 Moment M=-3.342059 Thrust N=-52.16336	
W=5# and P= 5	Strain in top gage= 43.90001 Strain in bottom gage=-16.87813 Moment M=-2.374146 Thrust N=-50.66602	
W=5# and P= 10	Strain in top gage= 19.55713 Strain in bottom gage= 1.9464 Moment M=-.6879191 Thrust N=-40.31912	
W=0 and P= 1	Normalized Moment = .189052 Normalized Thrust = .5673588	
W=0 and P= 5	Normalized Moment = .231393 Normalized Thrust =-.1859958	
W=0 and P= 10	Normalized Moment = .2843192 Normalized Thrust =-1.127688	



Loads at loading point # 5

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	45.27857	-12.72501
C 2	-.8932147	-3.246246
C 3	-.55625	.9156256
W=5# and P= 0	Strain in top gage= 45.27857 Strain in bottom gage=-12.72501 Moment M=-2.265765 Thrust N=-61.63794	
W=5# and P= 1	Strain in top gage= 43.82911 Strain in bottom gage=-15.05563 Moment M=-2.380185 Thrust N=-53.95028	
W=5# and P= 5	Strain in top gage= 26.90625 Strain in bottom gage=-6.065599 Moment M=-1.287963 Thrust N=-39.07623	
W=5# and P= 10	Strain in top gage=-19.27857 Strain in bottom gage= 45.37509 Moment M= 2.564596 Thrust N=-50.00598	
W=0 and P= 1	Normalized Moment =-3.442023E-02 Normalized Thrust =-7.087657	
W=0 and P= 5	Normalized Moment = .1955604 Normalized Thrust =-4.392343	
W=0 and P= 10	Normalized Moment = .4830361 Normalized Thrust =-1.023196	

Loads at loading point # 6

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	137.1787	-89.36426
C 2	-1.278259	2.465378
C 3	-.1437416	.1437473
W=5# and P= 0	Strain in top gage= 137.1787 Strain in bottom gage=-89.36426 Moment M=-8.849332 Thrust N=-89.65199	
W=5# and P= 1	Strain in top gage= 135.7567 Strain in bottom gage=-86.75514 Moment M=-8.691866 Thrust N=-91.87784	
W=5# and P= 5	Strain in top gage= 127.1938 Strain in bottom gage=-73.44369 Moment M=-7.837403 Thrust N=-100.7815	
W=5# and P= 10	Strain in top gage= 110.0219 Strain in bottom gage=-50.33575 Moment M=-6.263971 Thrust N=-111.9115	
W=0 and P= 1	Normalized Moment = .1574656 Normalized Thrust =-2.225862	
W=0 and P= 5	Normalized Moment = .202386 Normalized Thrust =-2.225902	
W=0 and P= 10	Normalized Moment = .2585362 Normalized Thrust =-2.225955	

Loads at loading point # 7

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	145.2535	-83.61774
C 2	1.362671	-.7667236
C 3	.7504501	-.8513336
W=5# and P= 0	Strain in top gage= 145.2535 Strain in bottom gage=-83.61774 Moment M=-8.940282 Thrust N=-115.567	
W=5# and P= 1	Strain in top gage= 147.3666 Strain in bottom gage=-85.23579 Moment M=-9.086031 Thrust N=-116.4953	
W=5# and P= 5	Strain in top gage= 170.8281 Strain in bottom gage=-108.7347 Moment M=-10.92042 Thrust N=-116.4251	
W=5# and P= 10	Strain in top gage= 233.9252 Strain in bottom gage=-176.4183 Moment M=-16.82905 Thrust N=-107.8254	
W=0 and P= 1	Normalized Moment =-.1457495 Normalized Thrust = .9282589	
W=0 and P= 5	Normalized Moment =-.3968279 Normalized Thrust = .1716213	
W=0 and P= 10	Normalized Moment =-.7088763 Normalized Thrust =-.7741642	

## Loads at loading point # 8

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	155.2643	-87.58283
C 2	6.092487	-4.654987
C 3	1.490189	-1.783374
W=5# and P= 0	Strain in top gage= 155.2643 Strain in bottom gage=-87.58283 Moment M=-9.486184 Thrust N=-126.9842	
W=5# and P= 1	Strain in top gage= 162.8469 Strain in bottom gage=-93.94631 Moment M=-18.83898 Thrust N=-129.1886	
W=5# and P= 5	Strain in top gage= 222.981 Strain in bottom gage=-153.5909 Moment M=-14.78984 Thrust N=-130.1865	
W=5# and P= 18	Strain in top gage= 365.2872 Strain in bottom gage=-385.0685 Moment M=-26.18264 Thrust N=-112.7682	
W=0 and P= 1	Normalized Moment =-.5447999 Normalized Thrust =-2.284341	
W=0 and P= 5	Normalized Moment =-1.044732 Normalized Thrust =.6484515	
W=0 and P= 18	Normalized Moment =-1.669646 Normalized Thrust =-1.414494	

Loads at loading point # 9

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	178.0604	-99.28589
C 2	9.151611	-10.4693
C 3	1.02813	-1.073227
W=5# and P= 0    Strain in top gage= 178.0604		
Strain in bottom gage=-99.28589		
Moment M=-10.83384		
Thrust N=-147.7023		
W=5# and P= 1    Strain in top gage= 188.2482		
Strain in bottom gage=-110.8284		
Moment M=-11.68237		
Thrust N=-145.1471		
W=5# and P= 5    Strain in top gage= 249.5217		
Strain in bottom gage=-178.4631		
Moment M=-16.71816		
Thrust N=-133.235		
W=5# and P= 10    Strain in top gage= 372.3895		
Strain in bottom gage=-311.3816		
Moment M=-26.70668		
Thrust N=-114.5399		
W=0 and P= 1		
Normalized Moment =-.8485264		
Normalized Thrust =-2.555206		
W=0 and P= 5		
Normalized Moment =-1.176863		
Normalized Thrust =-2.89345		
W=0 and P= 10		
Normalized Moment =-1.587284		
Normalized Thrust =-3.31624		

Loads at loading point # 18

Coefficients C1, C2 and C3 for equations of curve fitting

	Top gages	Bot. gages
C 1	160.5643	-80.66071
C 2	.4747315	-1.163086
C 3	-4.375077E-02	8.616257E-02

W=5# and P= 0 Strain in top gage= 160.5643  
 Strain in bottom gage=-80.66071  
 Moment M=-9.422851  
 Thrust N=-149.8192

W=5# and P= 1 Strain in top gage= 160.9953  
 Strain in bottom gage=-81.73763  
 Moment M=-9.481753  
 Thrust N=-148.6081

W=5# and P= 5 Strain in top gage= 161.8442  
 Strain in bottom gage=-84.32207  
 Moment M=-9.615869  
 Thrust N=-145.3539

W=5# and P= 10 Strain in top gage= 160.9365  
 Strain in bottom gage=-83.67531  
 Moment M=-9.535149  
 Thrust N=-144.8648

W=0 and P= 1  
 Normalized Moment =-.0589025  
 Normalized Thrust =-1.21128

W=0 and P= 5  
 Normalized Moment =-3.860355E-02  
 Normalized Thrust =-.8930511

W=0 and P= 10  
 Normalized Moment =-1.322985E-02  
 Normalized Thrust =-.4954434

EXPERIMENTAL AND THEORETICAL INVESTIGATION  
OF A SHALLOW FLEXIBLE ARCH

By

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AN ABSTRACT OF A MASTER'S THESIS

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requirements for the degree

MASTER OF SCIENCE

Department of Civil Engineering

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1984

This thesis presents a study of the experimental and theoretical investigation of a fixed ended flexible parabolic arch. The study is an attempt to test the applicability of a linearized deflection theory. The governing differential equation, based on the consideration of deflection of the arch, is derived and linearized for the construction of influence lines. A computer program in BASIC language, using the Runge-Kutta numerical integration method to construct the influence lines, through the technique of shooting method, is presented. Influence lines for the unit vertical force acting on the arch, for a given set of flexibility parameters, are constructed. The actual forces at the section of interest are then determined numerically, with the knowledge that the assumed and computed flexibility parameters must be equal. A series of experiments were conducted to verify the theoretical prediction. A model of steel arch, of span 60 inches and rise 8 inches, was built in the laboratory for this purpose. A comparison of the calculated stresses with the values obtained experimentally has been made at the end section as well as the central span section.